Available online www.jsaer.com

Journal of Scientific and Engineering Research, 2017, 4(9):1-14



Research Article ISSN: 2394-2630 CODEN(USA): JSERBR

Application of Linear Programming Solver in Optimal Production Cost

Ezemuo DT, Ofor IC

Department of Mechanical Engineering Technology, Federal Polytechnic, Oko, Anambra State, Nigeria

Abstract This study is focused on the optimal production cost of raw materials to its production output. Linear programming solver was applied to solve and to optimize its monthly production output. Based on the result, the monthly optimal production output is 1.2252E-08. The company has to budget at least the optimal result to achieve their monthly cost of production. The result will help the company to eliminate excess waste that incurs in their cost of production.

Keywords Bottle Glass, Optimization, Cost, Production output, Linear Programming, Sodium sulphate, Selenium, Cobalt Oxide, Feldspar, Soda Ash, Limestone and Silica sand

Introduction

The work drives to the optimization of the monthly production output of the case company. Having looked at the case study critically, the researcher begins to observe that there is excess waste of cost of production during the time the product is undergoing its production processes. With this in mind the researcher starts to gather the production process data from the raw material to the finished products over a given period of three years. According to Akbari & Taha (1992), reveals how linear programming and its application was used to determine the feed mix that will maintain a balanced proportional ratio which includes calcium, protein, and fiber in the right proportion by the Ozark Poultry Farm [1]. Adam et al (1993), shows the application of linear programming model and with its Multi-Band Enterprises. Finding the best mix of citizens band radio (CBs) and portable radio (PRs) to produce is a typical blending and mix determination problem. The application of linear programming to this problem gives a solution values which show that the Multi-Band Enterprises will produce 632.31 of CBs, 126.15 PRs and this will give the maximum profit of \$36,661.06. On the resources side, some hours of sub assembly are unused while the assembly and inspection hours are extensively utilized [2]. Andre et al., (2003) applied linear programming to predict nutrients that are potentially low in a child's diet during the complementary feeding period in the sense that the information gathered can be used to direct nutrition intervention programme initiatives because it suggests that foods rich in (foods fortified with) these limiting or problem nutrients should be introduced into local diets. Having gone through several research works, the researcher observes that linear programming solver can help to optimize the best possible cost that can solve the company's monthly production output at any given time of the year [3].

In solving the case study problem, the objective of the study was developed with the application of linear programming model that will reveal the optimal cost of monthly production of bottle glasses in the case company.

Linear programming (LP; also called linear optimization) is a method to achieve the best outcome (such as maximum profit or lowest cost) in a mathematical model whose requirements are represented by linear relationships. Linear programming is a special case of mathematical programming (mathematical optimization). More formally, linear programming is a technique for the optimization of a linear objective function, subject to linear equality and linear inequality constraints. Its feasible region is a convex polytope, which is a set defined

Journal of Scientific and Engineering Research

as the intersection of finitely many half spaces, each of which is defined by a linear inequality. Its objective function is a real-valued affine (linear) function defined on this polyhedron. A linear programming algorithm finds a point in the polyhedron where this function has the smallest (or largest) value if such a point exists. Linear programs are problems that can be expressed in canonical form as

Maximum cTx

Subject t $Ax \le b$ and $x \ge 0$

Where x represents the vector of variables (to be determined), c and b are vectors of (known) coefficients, A is a (known) matrix of coefficients, and (\cdot)T is the matrix transpose. The expression to be maximized or minimized is called the objective function (cTx in this case). The inequalities $Ax \le b$ and $x \ge 0$ are the constraints which specify a convex polytope over which the objective function is to be optimized. In this context, two vectors are comparable when they have the same dimensions. If every entry in the first is less-than or equal-to the corresponding entry in the second then we can say the first vector is less-than or equal-to the second vector. Linear programming can be applied to various fields of study. It is widely used in business and economics, and is also utilized for some engineering problems. Industries that use linear programming models include transportation, energy, telecommunications, and manufacturing. It has proved useful in modeling diverse types of problems in planning, routing, scheduling, assignment, and design.

History of Linear programming

The problem of solving a system of linear inequalities dates back at least as far as Fourier, who in 1827 published a method for solving them [4], and after whom the method of Fourier-Motzkin elimination is named. First linear programming formulation of a problem that is equivalent to the general linear programming problem was given by Leonid Kantorovich in 1939, who also proposed a method for solving it [5]. He developed it during World War II as a way to plan expenditures and returns so as to reduce costs to the army and increase losses incurred by the enemy. About the same time as Kantorovich, the Dutch-American economist T. C. Koopmans formulated classical economic problems as linear programs. Kantorovich and Koopmans later shared the 1975 Nobel prize in economics [4]. In 1941, Frank Lauren Hitchcock also formulated transportation problems as linear programs and gave a solution very similar to the later Simplex method [5].

During 1946-1947, George B. Dantzig independently developed general linear programming formulation to use for planning problems in US Air Force. In 1947, Dantzig also invented the simplex method that for the first time efficiently tackled the linear programming problem in most cases. When Dantzig arranged meeting with John von Neumann to discuss his Simplex method, Neumann immediately conjectured the theory of duality by realizing that the problem he had been working in game theory was equivalent. Dantzig provided formal proof in an unpublished report "A Theorem on Linear Inequalities" on January 5, 1948. Postwar, many industries found its use in their daily planning. The theory behind linear programming drastically reduces the number of possible solutions that must be checked .

The linear programming problem was first shown to be solvable in polynomial time by Leonid Khachiyan in 1979, but a larger theoretical and practical breakthrough in the field came in 1984 when Narendra Karmarkar introduced a new interior-point method for solving linear-programming problems [6-10].

Uses of Linear programming

Linear programming is a widely used field of optimization for several reasons. Many practical problems in operations research can be expressed as linear programming problems. Certain special cases of linear programming, such as network flow problems and multi commodity flow problems are considered important enough to have generated much research on specialized algorithms for their solution. A number of algorithms for other types of optimization problems work by solving LP problems as sub-problems. Historically, ideas from linear programming have inspired many of the central concepts of optimization theory, such as duality, decomposition and the importance of convexity and its generalizations. Likewise, linear programming is heavily used in microeconomics and company management, such as planning, production, transportation, technology and other issues. Although the modern management issues are ever-changing, most companies would like to maximize profits or minimize costs with limited resources. Therefore, many issues can be characterized as linear



programming problems.

The research method is the use of linear programming solver as a tool in Goal programming software was applied to observe the optimal cost necessary to achieve monthly glass production output.

Table 1: Production Data for Bottle Glass Monthly Production Record

Soda	Sand	FeldsparLimeston	eSalt cakeSeleniu		Total Amount
Ash			m	Oxide	of Monthly
					production
1.09E+0	0831024	10615507757455698	25753561381794	444628.	1125285217
1.01E+0	0828601	18914297006873603	2374288 1273912	241143.	8115503716
1.08E+0	0830574	14315283007347645	25380321361768	843981.	3123469489
1.03E+0	0829153	30414572507006056	2420040 1298460	041936.	6117729447
1.06E+0	0830124	48115058257239591	2500708 1341742	243334.:	5121653762
1.06E+0	0830240	08415116257267476	25103401346910	043501.4	4122122336
1.11E+0	0831473	36815732507563752	26126801401820	045274.	9127100945
1.1E+08	3 31248	38715620137509725	2594018139180	744951.:	5126193082
1.06E+0	0830240	08415116257267476	25103401346910	043501.	4122122336
1.08E+0	0830799	92415395387401672	2556694137178	144304.	7124377354
1.06E+0	0830023	32815007507215192	2492280 1337220	043188.:	5121243759
1.09E+0	0831024	40615507757455698	25753561381794	444628.	1125285217
1.09E+0	0831024	10615507757455698	2575356138179	444628.	1125285217
1.01E+0	0828630	09014311506880574	2376696 1275204	441185.:	5115620860
1.02E+0	0829000	07514496386969457	2407398129167	741717.	6117114443
1.06E+0	0830023	32815007507215192	2492280 1337220	043188.:	5121243759
1.09E+0	0831024	40615507757455698	25753561381794	444628.	1125285217
1.07E+0	0830458	34015225007319760	25284001356600	043814.	4123000914
1.08E+0	0830574	14315283007347645	2538032136176	843981.	3123469489
1.08E+0	0830574	14315283007347645	2538032136176	843981.	3123469489
1.08E+0	0830574	14315283007347645	2538032136176	843981.	3123469489
1.09E+0	0831024	40615507757455698	25753561381794	444628.	1125285217
1.09E+0	0830893	35215442507424328	25645201375980	044440	3124758070
1.11E+0	0831473	36815732507563752	26126801401820	045274.	9127100945
1.12E+0	0831698	34915844887617779	26313421411833	345598.	3128008809
986092	8028021	17314007006734179	23261281248072	240309.	2113160841
1.09E+0	0831024	40615507757455698	25753561381794	444628.	1125285217
1.07E+0	0830458	34015225007319760	25284001356600	043814.	4123000914
1.11E+0	0831473	36815732507563752	26126801401820	045274.	9127100945
1.06E+0	0830023	32815007507215192	2492280 1337220	043188.	5121243759

1.08E+08	3079924	153953874016722556694137178144304.7124377354
1.09E+08	3102406	155077574556982575356138179444628.1125285217
1.06E+08	3002328	150075072151922492280133722043188.5121243759
1.02E+08	2900075	144963869694572407398129167741717.6117114443
98762400	2806524	140287567446362329740125001040371.8113336557
1.08E+08	3079924	153953874016722556694137178144304.7124377354

Source: Bottle glass Company BATCHES/DAY WITH PRICES

1.Sand #925/ton 2.SodaAsh #110,000/ton



3.Limestone #7,700/ton 4.Feldspar #12,500/ton 5.Salt Cake #86,000/ton 6.Solenuim #19,000/kg 7.Cobalt Oxide#2,608/kg

Cost of Raw Materials per Production Batch

Sand (Silica sand)

1 ton = #925

1batch = 784kg

Cost of sand per batch = $784 \div 1000 \times #925 = #725.2$ Limestone

1 ton = #7,700 1batch = 224 kg

Cost of limestone per production batch = $224 \div 1000 \times \#7,700 = \#1724.8$

Soda Ash

1 ton = #110,000 1batch = 232 kg

Cost of soda ash per batch = $232 \div 1000 \times #110,000 = #25,520$ Feldspar

1 ton = #12,500 1batch = 29 kg

Cost of Feldspar per production batch = $29 \div 1000 \times \#12,500 = \#362.5$ Salt cake (Sodium sulphate)

1 ton = #86,000

1batch = 7kg

Cost of salt cake per production batch = $7 \div 1000 \times \#86,000 = \#602$ Selenium

1kg = #19,000 1batch = #17g

Cost of Selenium per production batch = $17 \div 1000 \times #19,000 = #323$ Charcoal Cobalt (Cobalt Oxide)

1 kg = #2,608

1batch = 4g

Cost of charcoal cobalt per batch = $4 \div 1000 \times #2,608 = #10.432$

Total Cost of Raw Materials per Production Batch

Soda Ash = #25,520

 Sand
 = 725.2

 Feldspar
 = 362.5

 Limestone
 = 1,742.8

 Salt cake (Sodium sulphate)
 = 602

 Selenium
 = 323

 Charcoal cobalt
 = 10.43

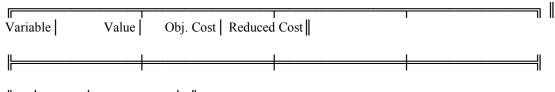
 Total cost
 = 29,267.932

Monthly production data were collected for three years production. The data were collected and analyzed to observe and to advice the case company on the optimal cost to budget every month for their production

Analysis and Results

```
>> Optimal solution FOUND >> Maximum = 1.2252e+008
```

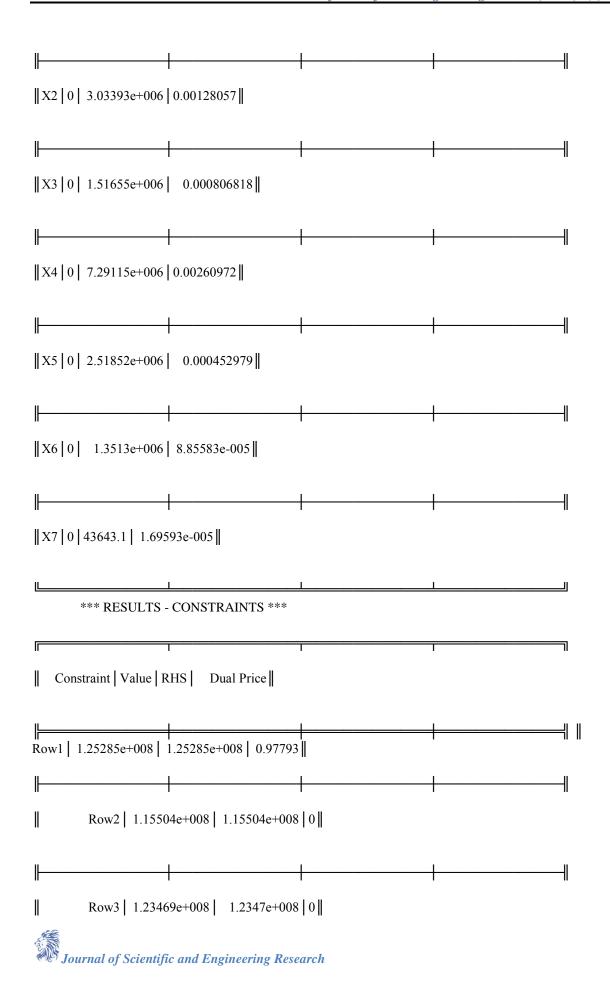
*** RESULTS - VARIABLES ***

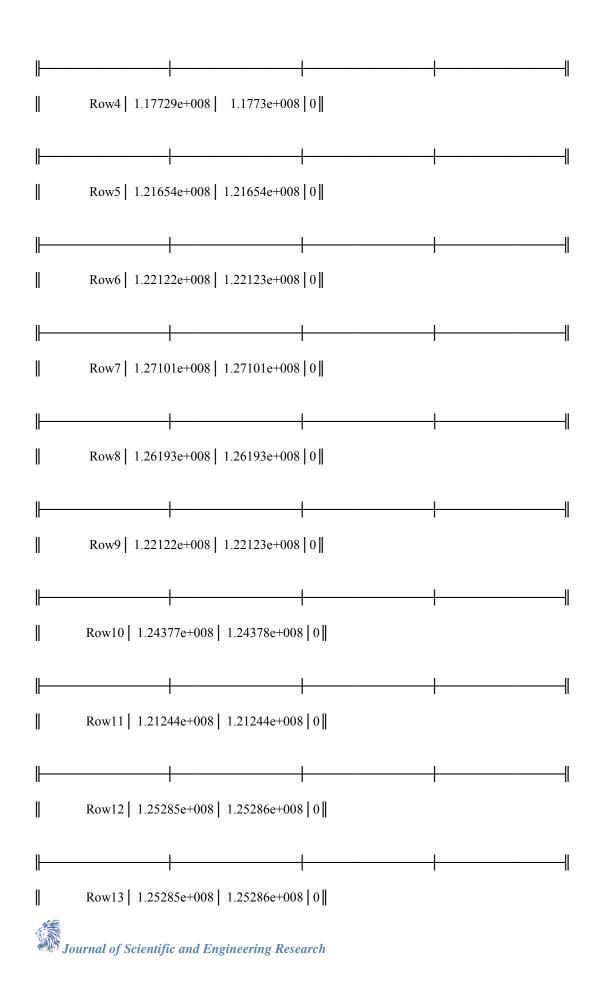


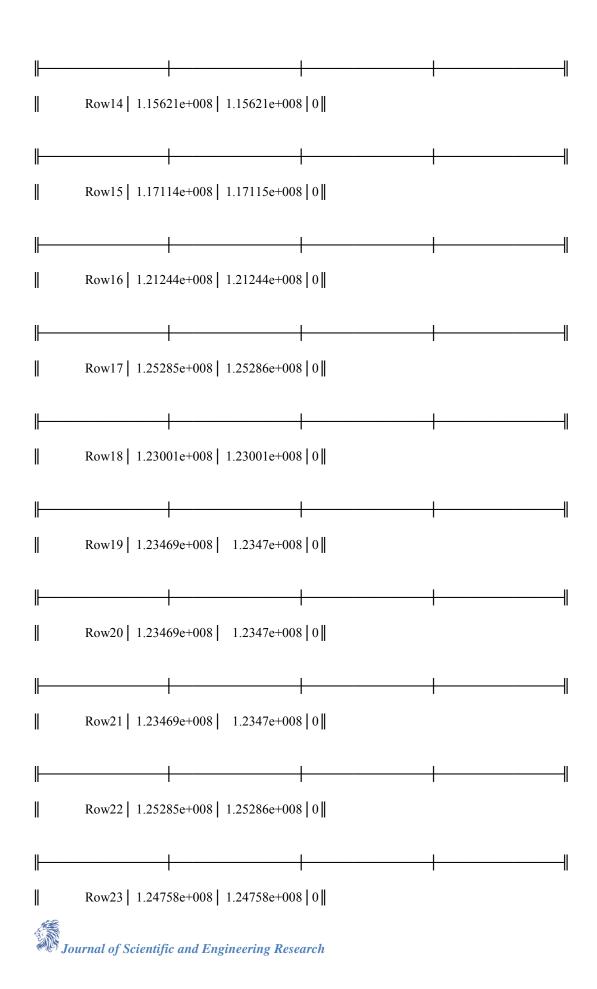
|| X1 | 1.14757 | 1.06765e+008 | 0 ||

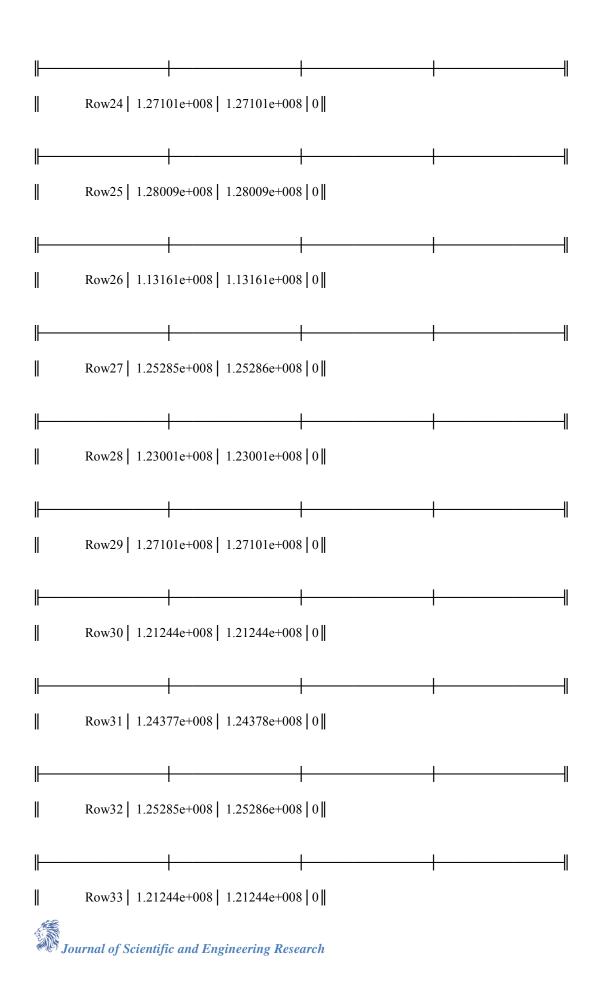


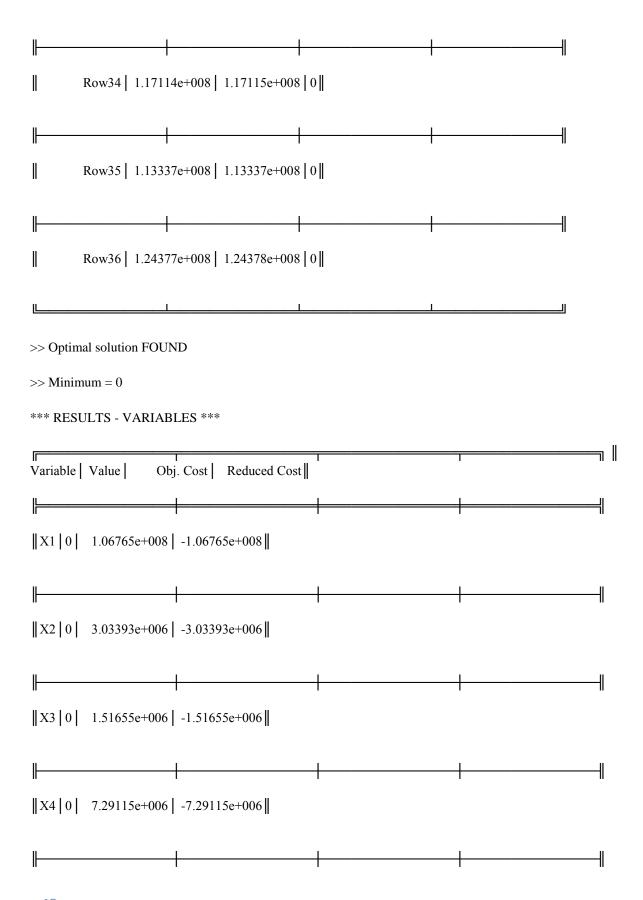
Journal of Scientific and Engineering Research



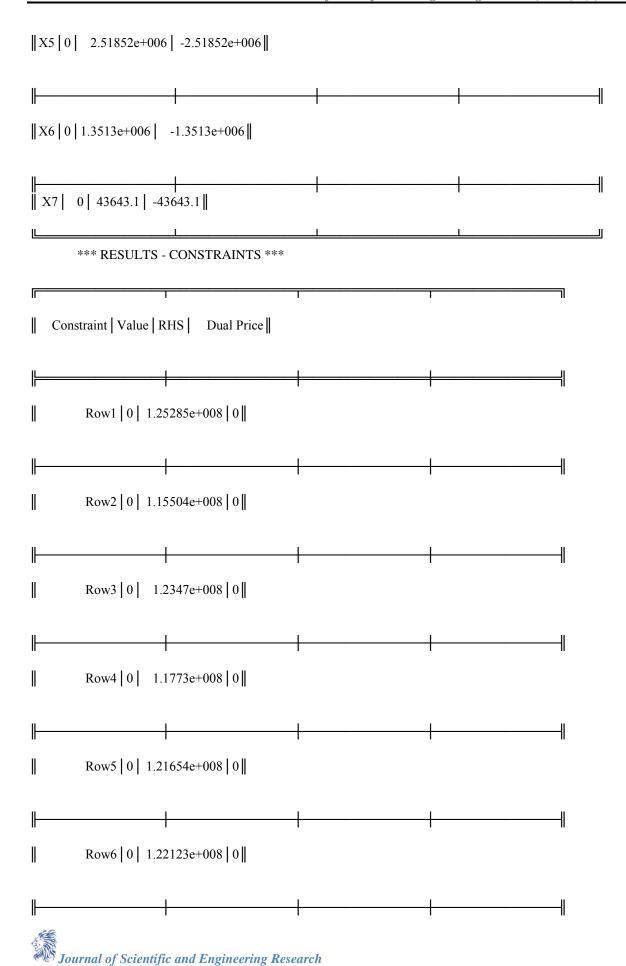


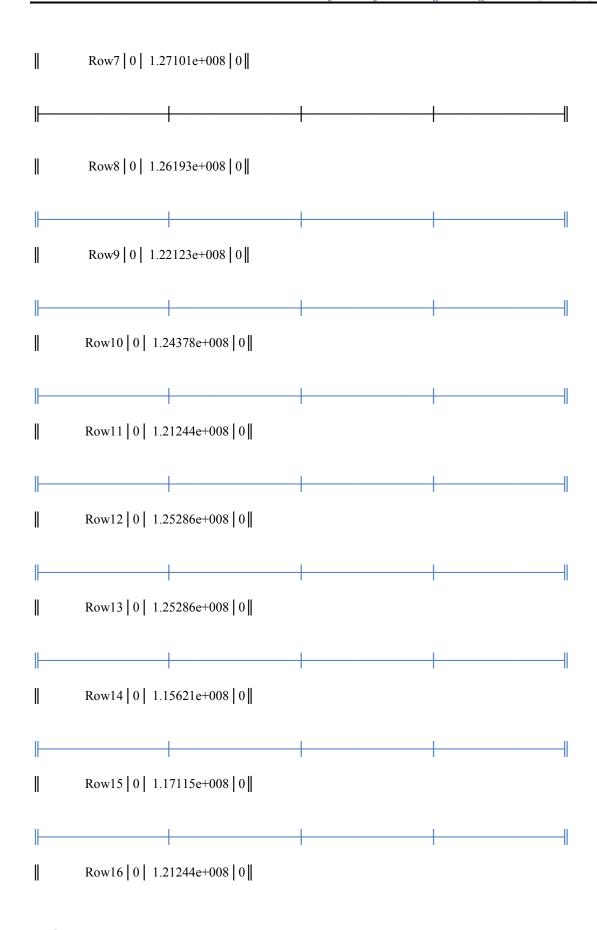




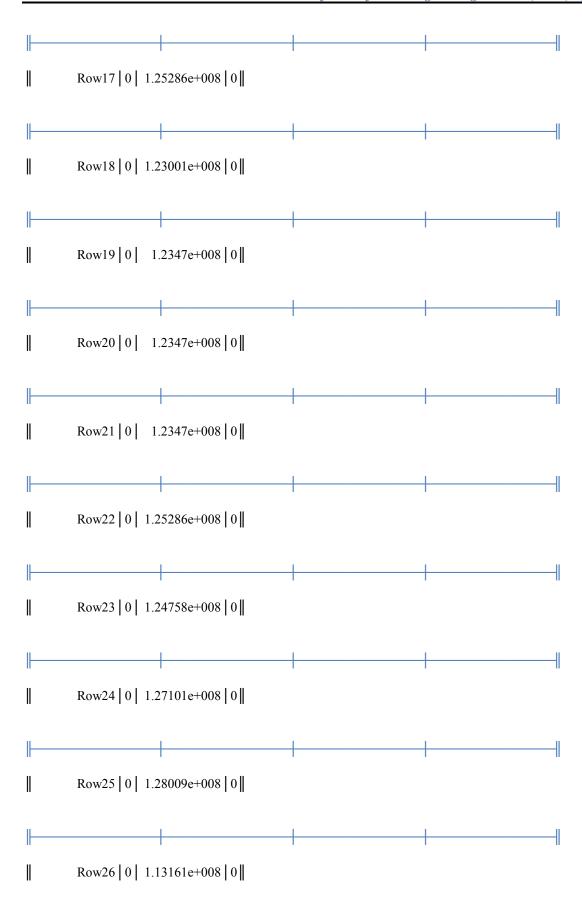




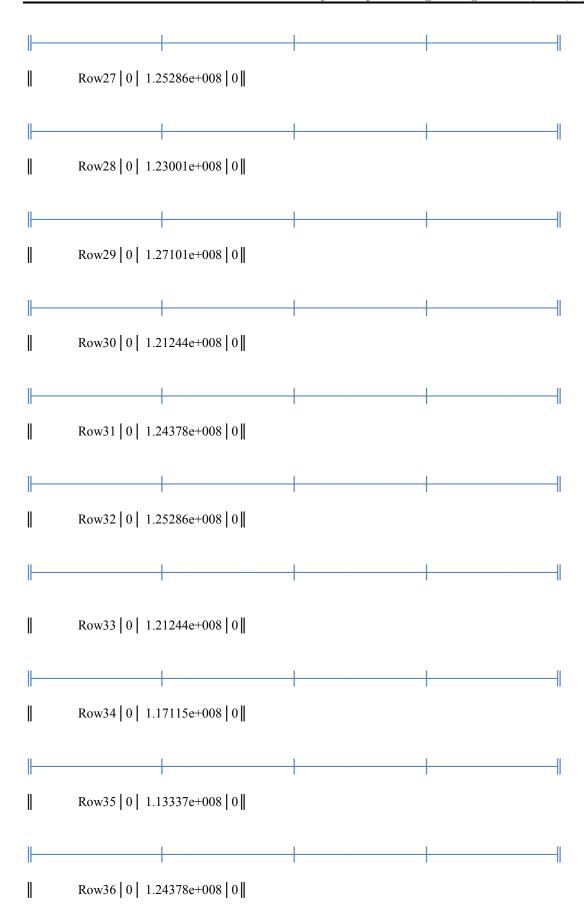














Discussion and Conclusion

Goal programming software was used analyze and to appraise the cost of production output of the company. The linear programming solver applied as a tool in goal programming was used to model and to optimize the cost thereby reducing wastes that occurs in the production process. From the result, the maximum cost of producing bottle glasses at any given month in any year if wastes were eliminated in the cost of production is 1.2252E0.8. Having found the result, the researcher concludes that in some certain months, there are excess wastes of cost of production and also the stability of the company's economy is at stack. To solve the problem found in the work, the researcher recommend the result to the case company and also recommend that there is a need to resolve the production process and also recommend the use of axiomatic model and its traditional method to solve the problem of production process.

References

- [1]. Akbari, H. and Taha, H. 1992. "The Impact of Trees and White Surfaces on Residential Heating and Cooling Energy Use in Four Canadian Cities", Energy, the International Journal, Vol. 17, No. 2 (1992), pp. 141-149.
- [2]. Adams, D. A; Nelson, R. R.; Todd, P. A. (1992), "Perceived usefulness, ease of use, and usage of information technology: A replication", MIS Quarterly 16: 227-247, doi: 10.2307/249577
- [3]. Andre et al, 2003, "Linear Programming: A Mathematical Tool for Analyzing and Optimizing Children's Diets during the Complementary Feeding Period", Journal of Pediatric Gastroentrology and Nutrition, issue 36, pp.12-22
- [4]. Kantorovich, L V. (1940). A new method of solving some classes of extremal problems. Ободномэффективномметодерешениянекоторыхклассовэкстремальныхпроблем". DokladyAkadSci USSR 28: 211-214.
- [5]. Hitchcock F. L. (1941): The distribution of a product from several sources to numerous localities, Journal of Mathematics and Physics, 20, 224-230.
- [6]. Beasley J. E. (1996), editor. Advances in Linear and Integer Programming. Oxford Science, (Collection of surveys).
- [7]. Dantzig G.B (1951): Maximization of a linear function of variables subject to linear inequalities, 1947. Published pp. 339-347 in T.C. Koopmans (ed.):Activity Analysis of Production and Allocation, New York-London (Wiley & Chapman-Hall)
- [8]. Dantzig George B. and Mukund N. Thapa. (1997). linear programming 1: Introduction. Springer-Verlag.
- [9]. Dantzig George B. and Mukund N. Thapa. 2003. Linear Programming 2: Theory and Extensions. Springer-Verlag. (Comprehensive, covering e.g. pivoting and interior-point algorithms, large-scale problems, decomposition following Dantzig-Wolfe and Benders and introducing stochastic programming).
- [10]. Karl-Heinz Borgwardt, (1987): The Simplex Algorithm: A Probabilistic Analysis, Algorithms and Combinatorics, Volume 1, Springer-Verlag, (Average behavior on random problems).