

# Comparison of ANN, CF and LR Methods for Harmonic Estimation

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**Abstract** - Power quality is an important criterion in electrical power systems. Harmonics negatively affect the power quality. Harmonic analysis and estimation have been made with various methods in the literature. In this study Artificial Neural Network (ANN), Curve Fitting (CF) and linear regression (LR) models have been developed for the estimation of the  $THD_1$  values. Some of the measured data have been used to generate models, the remaining part have been used to test the model. Estimation results obtained from the ANN, CF, LR models are compared to each other. Estimated  $THD_1$  values obtained from ANN, CF, LR models were close to real  $THD_1$  values so that ANN, CF, LR models can be used for the  $THD_1$  estimations. With this way, planning of the power systems can be made to increase the power quality in electrical power systems.

**Keywords** – Artificial Neural Network, Curve Fitting, Harmonic, Linear Regression, Power Quality, Power Distribution System, THD

## 1. INTRODUCTION

The power quality term has become one of the most important term in the power systems. There are many types of equipment that causes power quality problems. Computer, television, air conditioning, UPS, speed control device, welding machine, can be given as example to this type of non-linear loads. These loads generate the harmonics and negatively affect the power quality. Harmonic distortion is the most significant power quality problem. Total Harmonic Distortion (THD) is used as an indication of current and voltage distortion values. Harmonic limitations are described in the IEEE 519 standard [1], [2]. ANN's are used for harmonic estimates and signal analysis in literature [3], [4], [5], [6]. ANN has been

used to estimate the nonlinear harmonic loads [7]. ANN estimation method has been proposed for the current estimation of nonlinear loads which contains harmonic components in reference [8]. On the other hand, in some papers [9-15] curve fitting methods have been used. In reference [16], estimation of multivariate regression functions has been made with LR method. Modeling and estimation of the propagation loss in wireless systems with LR method proposed in reference [17]. For improving performance in heterogeneous Networks (hetnets), LR estimation method was proposed in reference [18]. In reference [19], linear regression-based estimation method was proposed to identifying sound. In reference [20], for defining the foreground of computer systems, LR based modeling method has been used. In reference [21], LR estimation method has been used for channel estimation in wireless networks. For estimating the growth trend of THD estimation, LR method has been used in reference [22]. In reference [23], LR method has been used for the frequency estimation. In reference [24], LR method has been used for the estimation. In this study, values were

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measured with devices connected to the grid. These values have been used in ANN, CF, LR models for training and testing purposes.

## 2.HARMONICS IN POWER SYSTEMS

Nonlinear devices cause harmonic distortion in the power system. The most commonly indices used for measuring the harmonic content of a waveform are the total harmonic distortion (THD).

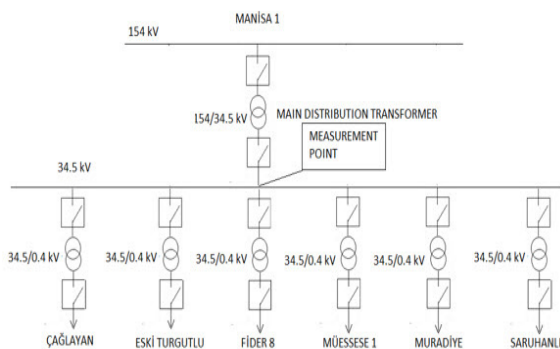
Total current harmonic distortion can be expressed as,

$$THD_I = \frac{\sqrt{\sum_{n=2}^{\infty} I_n^2}}{I_1} \quad (1)$$

Total voltage harmonic distortion can be expressed as,

$$THD_V = \frac{\sqrt{\sum_{n=2}^{\infty} V_n^2}}{V_1} \quad (2)$$

Studied energy distribution system is supplied from different transformer centers. The input voltage of distribution system is 154 kV. 154 / 34.5 kV transformer is used to turn voltage. values have been measured at the 34.5 kV side of the transformer. values measured from the system were used in the models for harmonic estimation. Single-line diagram of the distribution system is given in Figure 1.



**Figure1.** Single-line diagram of the energy distribution system

**Table1.** Measured Load Current and values for modeling and testing.

Measurement Number	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Load current ( $I_L$ )	370	330	270	250	240	220	290	365	447	465	470	480	490	475
Measured THD <sub>I</sub>	8,4	8,7	11,2	12	13	18	11,8	8,8	7	6,8	6,6	6,7	6	5,8

Measurement Number	1	2	3	4	5	6	7	8	9	10
Load current ( $I_L$ )	465	425	440	477	448	410	360	260	300	380
Measured THD <sub>I</sub>	6,2	7	7,1	5,8	6,8	7,8	9	12,2	11,8	8,4

## 3. SIMULATION STUDIES

### 3.1. ANN METHOD

Artificial neural networks include three parts.

1. Input Layer
2. Hidden Layer
3. Output Layer

Input layer neurons receive the input data and send this data to the hidden layer neurons. ANN was used for estimation purposes, the most important performance is the accuracy of estimation. Estimation error values were determined by the following formulas [25]. Y describes the value of the real measuring data; F describes value generated by the model,

Estimation Error can be defined as below.

$$e=Y-F \quad (3)$$

The average error is calculated as following

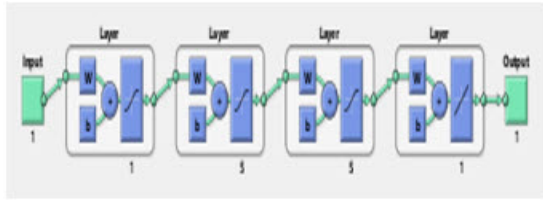
$$\frac{1}{n} \sum_{i=1}^n e_i \quad (4)$$

The average absolute error can be written as below.

$$\frac{1}{n} \sum_{i=1}^n |e_i| \quad (5)$$

The percentage error can be written as below.

$$\frac{e_t}{Y_t} * 100 \quad (6)$$



**Figure 2.** ANN model with one input layer, two hidden layer, one output layer.

ANN model has been shown in Figure 2. ANN model has 1-input, 2 hidden layers and one output layer. There is no connection between hidden layer. estimation has been done with the proposed ANN model.

### 3.2. CURVE FITTING

For determining a polynomial equation of the unknown intermediate values of data set curve fitting methods are used. Polynomial equation obtained from the curve fitting can't pass through the data points. Appropriate of polynomials are searched in different degrees [26].

Given the  $(n + 1)$  points:  $(x_0, y_0), (x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$ , There is more similar  $n^{\text{th}}$  degrees of polynomial passing through this point.

$$y = P_n(x) = b_0 + b_1x + b_2x^2 + \dots + b_n x^n \quad (7)$$

This coefficients  $(b_0, b_1, b_2, \dots, b_n)$  are achieved by solving linear equations.

$$b_0 + b_1x_0 + b_2x_0^2 + \dots + b_nx_0^n = y_0 \quad (8)$$

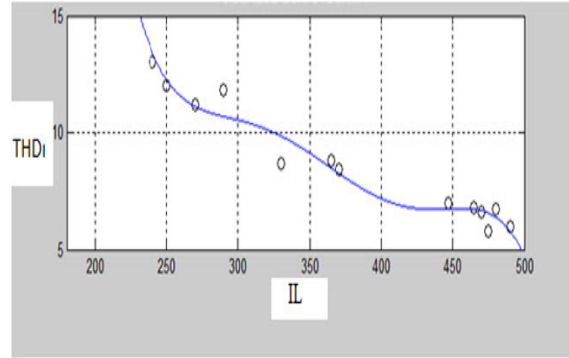
$$b_0 + b_1x_1 + b_2x_1^2 + \dots + b_nx_1^n = y_1$$

$$b_0 + b_1x_2 + b_2x_2^2 + \dots + b_nx_2^n = y_2$$

$$\dots \dots \dots \dots \dots \dots$$

$$b_0 + b_1x_n + b_2x_n^2 + \dots + b_nx_n^n = y_n$$

There is an error if the degree of the polynomial is chosen too small. If the degree of the polynomial is chosen too big unexpected fluctuations in the interpolation functions occur. Therefore choosing of the degree of polynomial is very important.



**Figure 3.** CF graph.

CF graph is shown in Figure 3.  $THD_1$  estimations were made by using this 5<sup>th</sup> degree equation curve.

### 3.3.LINEAR REGRESSION METHOD

Linear regression attempts to model the relationship between two variables by fitting a linear equation to measuring data. One variable is considered to be an explanatory variable, and the other is considered to be a dependent variable.

Simple linear regression is a statistical method for obtaining a formula to predict values of one variable from another where there is a causal relationship between the two variables.

In simple linear regression, we predict scores on first variable from the scores on a second variable. The variable we are predicting is called the *criterion variable* and is referred to as Y. The variable we are basing our predictions on is called the *predictor variable* and is referred to as X.

The formula for a regression line is

$$Y = bX + A \quad (9)$$

where Y is the predicted score, b is the slope of the line, and A is the constant.

Linear regression consists of the best-fitting straight line through the points. The best-fitting line is called a *regression line*.

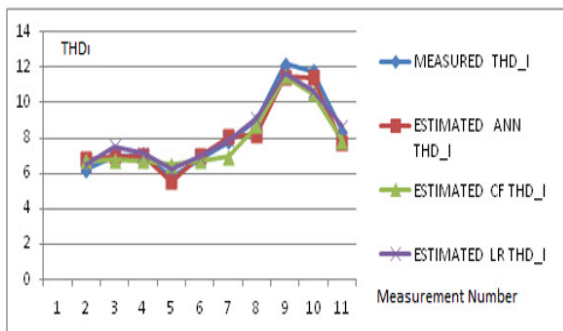
## 4. COMPARISON OF THE ESTIMATION RESULTS

Table 2 gives the information about percentage error, the measured and estimated  $THD_1$  via ANN, CF and LR methods The  $THD_1$  values in this table are used for testing

the ANN, CF and LR methods. % error value is expressed as percentage of the difference between the measured  $THD_i$  and estimated  $THD_i$ .

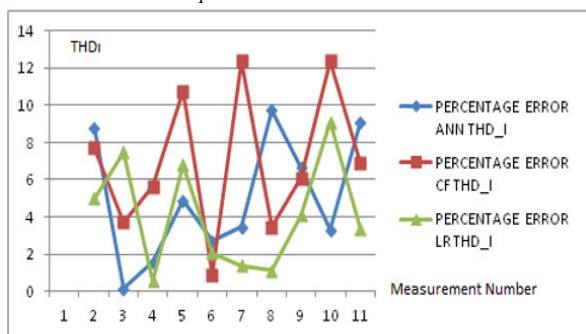
**Table 2** % error; measured  $THD_i$ , estimated  $THD_i$  values.

MEASUREMENT NUMBER	MEASURED $THD_i$	ESTIMATED ANN $THD_i$	ESTIMATED CF $THD_i$	ESTIMATED LR $THD_i$	PERCENTAGE ERROR ANN $THD_i$	PERCENTAGE ERROR CF $THD_i$	PERCENTAGE ERROR LR $THD_i$
1	6,2	6,8	6,72	6,51	8,82	7,73	5
2	7	7,01	6,75	7,53	0,14	3,7	7,5
3	7,1	6,99	6,72	7,14	1,57	5,65	0,56
4	5,8	5,53	6,5	6,2	4,88	10,76	6,8
5	6,8	6,99	6,74	6,94	2,71	0,89	2,05
6	7,8	8,08	6,94	7,91	3,46	12,39	1,4
7	9	8,2	8,7	9,1	9,75	3,44	1,11
8	12,2	11,44	11,5	11,7	6,64	6,08	4,09
9	11,8	11,42	10,5	10,7	3,32	12,38	9,1
10	8,4	7,7	7,86	8,68	9,09	6,87	3,33



**Figure 4** The measured  $THD_i$  and estimated  $THD_i$  values.

Figure 4 illustrates the measured  $THD_i$  and estimated  $THD_i$  values. As seen from the figure, estimated  $THD_i$  values are close to measured  $THD_i$  values.



**Figure 5.** The percentage error between measured  $THD_i$  and estimated  $THD_i$  values

Figure 5 shows the % error between measured and obtained from ANN, CF and LR  $THD_i$  values. First estimation error values for ANN, CF and LR are 8,82 %, 7,73 %, 5 %, respectively . In second estimation error values are 0,14 %, 3,7%, 7,5 %, respectively. In third estimation error values are 1,57 %, 5,65%, 0,56 %, respectively. Estimated error values in the 4th estimation are 4,88 %, 10,76%, 6,8 %, respectively. Estimated error values in the fifth estimation are 2,71%, 0,89%, 2,05%, respectively. In sixth estimation error values are 3,46 %, 12,39%, 1,4 %, respectively. Estimated error values in the seventh estimation are 9,75 %, 3,44%, 1,11 %, respectively. In eighth estimation error values are 6,64 %, 6,08%, 4,09 %, respectively. Estimated error values in the 9th estimation are 3,32 %, 12,38%, 9,1 %, respectively. Estimated error values in the tenth estimation are 9,09 %, 6,87%, 3,33 %, respectively.

Test phase; the average errors are 5,03% for ANN, 6,98% for CF and 3,99 % for LR .

## 5. CONCLUSION

In this study,  $THD_i$  values in the electrical power systems were estimated by using ANN, CF and LR methods. With this proposed method, harmonics which is one of the power quality problems can be estimated previously to improve power quality. Especially harmonic analysis and the estimation are very important in the distribution system. Because of the harmonic distortion the losses and the various defects occur. Harmonics adversely affects power quality. Harmonic values are estimated approximately 95% accuracy by ANN algorithm, 93% by CF and 96% by LR algorithm. This accuracy values indicate that proposed ANN, CF and LR models can be used to estimate  $THD_i$  values. According to this estimated  $THD_i$  values, the required filter parameters can be determined and applied to the power distribution system. In this way, by reducing the harmonic values, a considerable increase in power quality can be provided. ANN, CF and LR  $THD_i$  estimation models, can be used in other power distribution systems for the  $THD_i$  estimation.

## 6. REFERENCES

- [1] IEEE Guide for Harmonic Control and Reactive Compensation of Static Power Converters, ANSIIEEE Std. 519-1981, 1981.
- [2] IEEE Recommended Practices and Requirements for Harmonic Control in Electrical Power

- Systems, IEEE Std. 519-1992, 1992.
- [3] U.Arumugam ,N.M. Nor,M.F. Abdullah “A Brief on Advances of Harmonic State Estimation Techniques in Power Systems.” International Journal of information and Electronics Engineering Vol.1,No.3,November 2011
- [4] Sachin K. Jain and S. N. Singh, “Harmonics Estimation in Emerging Power System: Key Issues and Challenges,” *Electr. Power Syst. Res.*, vol.81, pp. 1754-1766,2011.
- [5] Ibrahim El-Amin, Ihab Arafah “Artificial Neural Network for Power System Harmonic Estimation” 0-7803-5105-3/98 1998 IEEE
- [6] Sachin K. Jain ,D.Saxena,S.N. Singh “Adaptive Wavelet Neural Network Based Harmonic Estimation Single –Phase Systems” 978-1-4673-6008-1 2012 IEEE
- [7] Chen Ying,Lin Qingsheng “New Research on Harmonic Dedection Based Neural for Power System” 978-0-7695-3589-4/09 2009 IEEE
- [8] Mario Oleskovicz,Marcelo A.A. Lima,Etienne Biassoto,Denis V. Coury “Estimation of Harmonic Currents Injected by Nonlinear Loads for a Distorted Power Supply Scenario Using Artificial Neural Networks” 978-1-1673-1943-0/12 2012 IEEE
- [9] Yingxiang Li,Weiwen Tang ,Yujun Kuang “3-order Polynomial Phase Signal Parameter Estiamation Algorithm Based on Instantaneous Frequency Curve Fitting Method” 978-0-7695-4031-3/10 2010 IEEE
- [10] Roman Z. Morawski ,Andrzej Barwicz “3 Curve Fitting Algorithms Versus Neural Networks When Applied for Estimation of Wavelength and Power in DWDM Systems ” 0018-9456/2005 IEEE
- [11] Yang Jian,Zhou Qiang,Qu Chang-wen “Fast Estiamation of Multilook K-Distribution Parameter s via the Least-Squares Nonlinear Curve Fitting ” 978-1-4673-2197-6/12 2012 IEEE
- [12] Lisha Chen, Matteo Laffranchi, Nikos G.Tsagarakis,Darwin G.Caldwell “A Novel Curve Fitting Based Discrete Velocity Estimator for High Performance Motion Control ” 978-1-4673-2576-9/12 2012 IEEE
- [13] XU Guo-sheng “The Application of Curve Fitting Technique in Fabric Detection ” 978-1-4244-6893-5 2010 IEEE
- [14] M. Babita Jain, Manoj Kumar Nigam, Prem Chand Tiwari “Curve Fitting and Regression line method Based Seasonal Short Term Load Forecasting. ” 978-1-4673-4805-8/12 2012 IEEE
- [15] I. B. Aris, L.N. Hulley, N.B. Mariun, R.K.Z. Sahbudin “Using Curve Fitting Optimization Technique to Estimate Power Mosfet Model Parameters for Pect II system” 0-7803-4971-8/98 1998 IEEE
- [16] Elias Masry “Local Linear Regression Estimation Under Long-Range Dependence: Strong Consistency and Rates ” 0018-9448/01 2001 IEEE
- [17] Mohamed Kadhem Karray, Bartłomiej Błaszczyszyn “Linear-Regression Estimation of the Propagation-Loss Parameters Using Mobiles’ Measurements in Wireless Cellular Networks” 978-3-901882-45-6/2012 IEEE
- [18] Sudeepta Mishra, Anik Sengupta, and C. Siva Ram Murthy “Enhancing the Performance of HetNets via Linear Regression Estimation of Range Expansion Bias” 978-1-4799-2084-6/13 2013
- [19] Jen-Tzung Chien, Chih-Hsien Huang “Online Speaker Adaptation Based on Quasi-bayes Linear Regression ” 0-7803-7041 -4/01 2001 IEEE
- [20] Gengjian Xue, Li Song, Jun Sun “Foreground Estimation Based on Linear Regression Model With Fused Sparsity on Outliers ” 1051-8215/2013 IEEE
- [21] Benoit Le Saux , Maryline H’ elard “Iterative Channel Estimation based on Linear Regression for a MIMO-OFDM system” 1-4244-0495-9/06/2006 IEEE
- [22] Chi-Jui Wu, Chung-King Hu, ChinChung Yin, Ching-Chuan Chiu “Application of Regression Models to Predict Harmonic Voltage and Current Growth Trend from Measurement Data at Secondary Substations’ ’0885-8977/98 1997 IEIEE
- [23] STEVEN A. TRETTER, “Estimating the Frequency of a Noisy Sinusoid by Linear Regression ” 0018-9448/85/1100-0832 1985 IEEE
- [24] Gonzales S.”Neural Networks for Forecasting:A Compleantry Approach to Linear Regression Methods ,Working Paper 2000-07,Canada,26-33 (2000)
- [25] Hamzaçebi C.,”Yapay Sınır Ağları”, Ekin, 4-104, 2011
- [26] Ahmet ALTINTAŞ Matlab ve Uygulamaları, 2006.
- [27] S.Ozdemir , M. Demirtas, S. Aydın ‘Artificial Neural Network Based Power Distribution System Modelling and Harmonic Estimation” Volume7 Issue11 ISSN: 1305-9130 ,163-172 Girne American University Journal of Social and Applied Sciences

