PARAMETER ESTIMATION IN BREAD BAKING MODEL

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Abstract

Bread product quality is highly dependent to the baking process. A model for the development of product quality, which was obtained by using quantitative and qualitative relationships, was calibrated by experiments at a fixed baking temperature of 200°C alone and in combination with 100 W microwave powers. The model parameters were estimated in a stepwise procedure i.e. first, heat and mass transfer related parameters, then the parameters related to product transformations and finally product quality parameters. There was a fair agreement between the calibrated model results and the experimental data. The results showed that the applied simple qualitative relationships for quality performed above expectation. Furthermore, it was confirmed that the microwave input is most meaningful for the internal product properties and not for the surface properties as crispness and color. The model with adjusted parameters was applied in a quality driven food process design procedure to derive a dynamic operation pattern, which was subsequently tested experimentally to calibrate the model. Despite the limited calibration with fixed operation settings, the model predicted well on the behavior under dynamic convective operation and on combined convective and microwave operation. It was expected that the suitability between model and baking system could be improved further by performing calibration experiments at higher temperature and various microwave power levels.

Keywords: *baking; bread quality; experimental validation; process design*

Abstrak

PERKIRAAN PARAMETER DALAM MODEL UNTUK PROSES BAKING ROTI. *Kualitas produk roti sangat tergantung pada proses baking yang digunakan. Suatu model yang telah dikembangkan dengan metode kualitatif dan kuantitaif telah dikalibrasi dengan percobaan pada temperatur 200°C dan dengan kombinasi dengan mikrowave pada 100 Watt. Parameter-parameter model diestimasi dengan prosedur bertahap yaitu pertama, parameter pada model perpindahan masa dan panas, parameter pada model transformasi, dan paramater untuk kualitas produk. Hasil percobaan menunjukkan bahwa model cukup untuk menggambarkan phenomena pada proses baking roti. Lebih lanjut, pada penelitian ini juga ditunjukkan bahwa mikrowave sangat bermanfaat untuk meningkatkan kualitas produk bagian dalam. Model dengan parameter yang telah diperoleh dapat digunakan untuk menggambarkan operasi proses secara dinamik. Meskipun kalibrasi ini menggunakan temperatur tetap, akan tetapi mampu memperkirakan dinamika operasi konveksi dan komibasi konveksi dengan mikrowave. Model dapat dikembangkan lebih lanjut dengan menggunakan variasi temperature dan level dari mikrowave.*

Kata kunci: *baking; kualitas roti; validasi percobaan; perancangan proses*

INTRODUCTION

The availability of accurate models to predict product quality is an essential requirement in quality driven food process design. Hadiyanto *et al.* (2007a) use a model to predict the development of product quality during bakery operations and they use the model also to generate design alternatives by calculating dynamic optimal operations (Hadiyanto *et al.*, 2007b). This model needs to be experimentally validated.

Baking is a main operation in bakery production which is performed by convective heating

system or by combined heating system using convective, microwave and radiation heating. Convective heating exposes the surface to a high temperature and the heat subsequently penetrates the product towards the center. This result in water evaporation and a corresponding increment of the internal pressure which creates a driving force for vapor transport to the environment of the product. In contrast to convective heating, microwave radiation will generate the heat directly inside the product, which results in different moisture and temperature profiles for products in comparison to convective heating. Radiation heating affects the product surface temperature and heat penetration to the product from this source is limited. Combined heating system with convective, microwave and radiation heating increases the flexibility of baking operation whereas the operation time is reduced and a wider range of product quality can be realized (Ni and Datta, 2002; Keskin *et al*., 2005; Hadiyanto *et al*., 2007b; Sumnu *et al*.,2006).

Important quality attributes of bakery products are color, texture, crumb and size. These attributes are the consequence of browning reactions, starch gelatinization, retrogradation and gas expansion. The associated transformations are ruled by the heat and mass transfer within the products which are a result of the imposed process conditions. The model proposed by Hadiyanto *et al*. (2007a) is a sequential model that includes the chain of phenomena starting from heat and mass transfer followed by the state transformations and finally the product quality formation. The heat and mass transfer part of the model was based on well recognized relationships for transport phenomena (Zhang and Datta, 2006). The state transformations and quality formation, however, were derived from qualitative expert knowledge. Several assumptions and simplifications that inevitably had to made, may reduce the reliability of the prediction. As a consequence, to prove the reliability and for the future use of the model, a check on the validity of the model prediction is required.

Several papers reported on model validation of baking processes (for example Zheleva and Kambourova, 2005; Zanoni *et al*., 1993; Lostie *et al*., 2002; Thorvaldson and Janestad, 1999). However, their researches were mostly focused on the heat and mass transfer phenomena during baking and missing the link with product quality. Some studies did consider quality aspects and parameter estimation. For example, Lostie *et al.* (2003) studied the effect of volume expansion, and Zanoni *et al.* (1995) reported about brownness development. Our challenge was to extend and put the previous work on a firmer basis by validation of the combined model for heat and mass transfer and a series of qualities.

The aim of this work is to evaluate the current model for the formation of bakery product quality (Hadiyanto *et al*., 2007a), and to adapt parameters in the model where necessary. Because the baking model is a sequential model, in the sense that the heat and

mass transport is not influenced by the product transformations, the validation can also be done in a sequential way; starting from heat and mass transfer related measurements, then the state transformations and finally the quality measurements. The model is calibrated against experiments with constant operational conditions and subsequently the validity of the model to predict quality for dynamic baking operations is tested.

MATERIALS AND METHODS
Experimental Set-up for Baking
Dough preparation

Dough was prepared from a mixture of 500 g flour (C1000 bread mixture for white and ciabatta, with composition per 100 g flour : 50% starch, 8.6% protein, 5% fat, 2% yeast, 0.5% salt) and 300 g water in a dough mixer (Inventum BM20) at medium speed for 3 minutes and 37$^{\text{o}}$C. Then the dough was kneaded for 5 min and the product was placed on the baking plate for 30 min to rise at room temperature. The initial weight of the dough and the height of the formed sample were measured before the sample was put in the oven. The initial size of the dough was the same for all experiments with diameter 0.08 m and height 0.04 m, the initial weight was 250 g.

Equipment set-up

An overview of the baking equipment is shown in Figure 1. The domestic oven was expanded with an external microwave source, which can provide an adjustable power. A monitoring and control system for oven and microwave heating was developed in Labview. This control system monitors the temperatures and allows for a dynamic operation of the convective and microwave heat sources. Here, input trajectories for convective and microwave heating were based on four intervals of piece-wise constant heating input for the oven and microwave system.

Temperatures in the oven and in the product were measured with optical temperature sensors using an optical slip ring (OSR) with multi probes (FISO Technology, Sainte-Foy, Quebec, Canada). The OSR system with four fiber-optic sensors was mounted on the oven such that it was possible to measure the temperatures during processing on a rotating table. The maximum temperature for the sensors was 250$^{\text{o}}$C with accuracy of 1$^{\text{o}}$C.

Baking experiment

Conventional oven baking was performed in the oven at a controlled temperature level (set up at 200°C) and time (set up at 30 minutes). The oven was preheated for 10 minutes to reach the setting temperature before the dough was placed in the oven. To follow the development of the product formation during baking, several bread samples with the same initial properties were baked for different time periods.
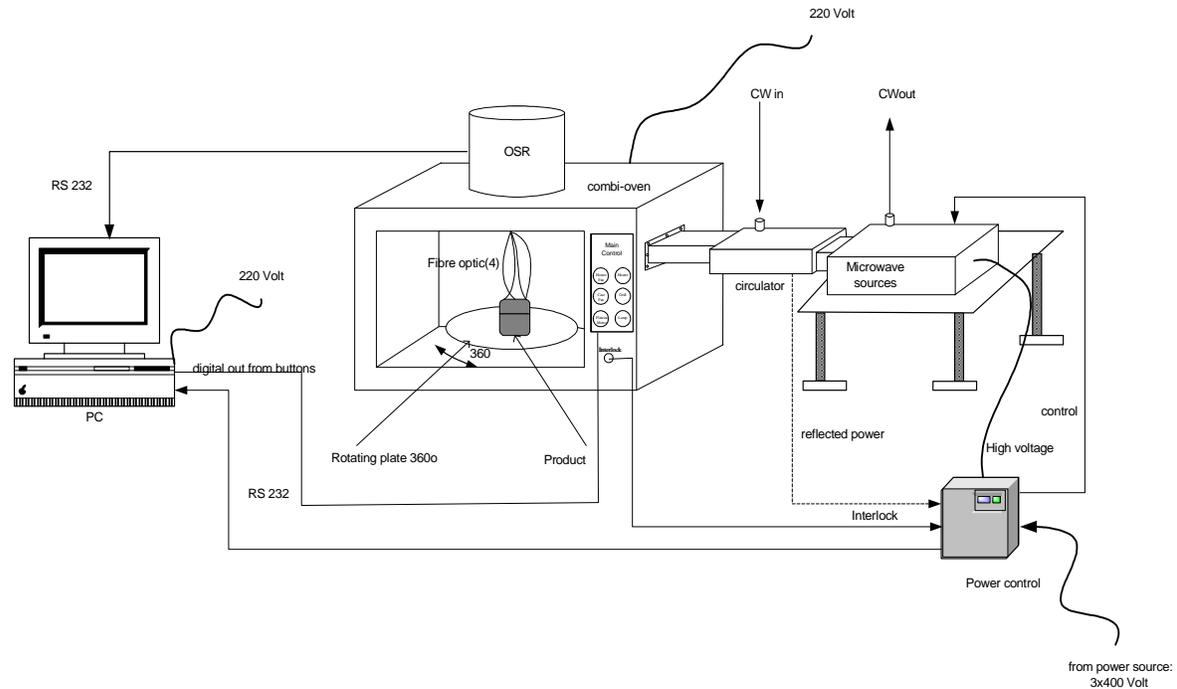
Figure 1. Equipment overview for baking

Other experiments were performed for a combination of convective and microwave heating with an adjustable microwave source. For experiments with constant microwave input the dissipated power level was set to 100W.

Quality Analysis

The color of the bread product was measured with a Minolta chromatometer (CR-200, Japan) using the *L*, *a,* and *b* color scale (Hunter method). Triplicate measurements were done at different positions on the bread surface and bread crumb, and then the mean value was calculated. The colour change (ΔE) compared to a calibrated reference was calculated from Eq .1 where the reference color is represented by L_0, a_0 and b_0.

$$\Delta E = \sqrt{(L - L_0)^2 + (a - a_0)^2 + (b - b_0)^2} \qquad (1)$$

A texture analyzer for food products (TA-XT Plus, Stable Micro Systems Ltd., Surrey, UK) was used for the instrumental analysis of the bread crust and crumb. Samples of crust and crumb with size 20x30x30 mm were subjected to a compression test using the SMS P/2 probe (test speed 1.7 mm/s, distance 6.2 mm). The measurements were done 2 hours after baking.

From the resistance of the probe encountered during penetration a force-deformation curve was constructed. Penetration of the crust occurred at about 3.8 s after the probe touched the sample surface and the force-deformation reached a maximum load of 370 g. These peak values are used to represent the crispness of the product surface (Dogan and Kokini, 2007).

The weight loss during baking was determined by weighting the product before and after baking. The relative weight loss was calculated as

$$w_L = \frac{w_0 - w_f}{w_0} \qquad (2)$$

Where w_o and w_f denoted the initial and final weight of product, respectively. Similarly, the volume extension (e) was obtained by measuring the height of the bread product before (h_0) and after (h_f) baking and was calculated as

$$e = \frac{b_f - b_0}{b_0} \qquad (3)$$

Model Development

Calculations for the product were done using a 2D spatial model, since the sample breads were much longer than their wide. As the bread samples were symmetric, it was satisfied to do the calculations for a half cross-sectional area. The geometry of the cross-sectional area of the product is given in Figure 2.
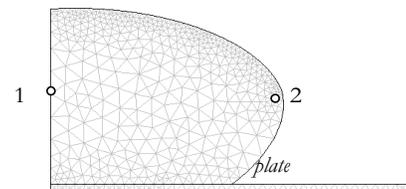

Figure 2. The product domain for simulation

The evaluated center and surface locations are indicated by point 1 and 2. A symmetry boundary was

applied along the center plane and flux boundary conditions were used along the surface of product. The bottom of product was contacted with plate, where it gave conductive heating to the product.

Point 1 and 2 represent the center and surface points of the product for which the results are discussed (height 0.04 m, radius 0.04 m).

The model is a combination of three sequential processes: heat and mass transfer, product transformation and translation to quality, which are explained separately in the following sections. The symbols are explained in the appended notation list.

Heat and mass transfer

Energy balance. The energy balance covers heat conduction, evaporation and condensation heat, and convection heat transport due to the fluxes of water vapor and CO_2 (eq. 4). The second term is due to the change of product height.

$$\rho_s c_p \frac{\partial T}{\partial t} + \frac{\rho_s \lambda \partial_e}{1+e} \frac{}{\partial t} = \nabla.(k\nabla T) - \lambda I_v - \nabla(m_v H_v) \\ - \nabla(m_c H_c) \quad (4)$$

Mass balances. The mass balances for liquid water, water vapor and CO_2 gas are given in Eqs. 5-7. The changes of liquid water in the product are the result of the rates of diffusion and evaporation (I_v). Water vapor is considered as an ideal gas which is in equilibrium with liquid water. The vapor concentration is a function of the rates diffusion and evaporation rate as well.

$$\rho_s \frac{\partial W}{\partial t} + \frac{\rho_s.W}{1+e} \frac{\partial e}{\partial t} = \nabla\phi_w - I_v \quad (5)$$

$$\rho_s \frac{\partial V_v}{\partial t} + \frac{\rho_s.V_v}{1+e} \frac{\partial e}{\partial t} = \nabla\phi_v + I_v \quad (6)$$

$$\rho_s \frac{\partial V_c}{\partial t} + \frac{\rho_s.V_c}{1+e} \frac{\partial e}{\partial t} = \nabla\phi_c + I_c \quad (7)$$

The flux equations. Flux equations for Eqs. 5-7 are

$$\phi_w = \rho_s D_w \nabla W \quad (8)$$

$$\phi_v = \rho_s D_{vc} \nabla V_v - m_v \quad (9)$$

$$\phi_c = \rho_s D_{vc} \nabla V_c - m_c \quad (10)$$

The convective mass fluxes of water vapor (m_v) and CO_2 (m_c) depend on local pressure differences, kinematics viscosity (v) and permeability (κ) of the product:

$$m_v = -\frac{\kappa}{v} \frac{V_v}{V_v + V_c} \nabla P \quad (11)$$

$$m_c = -\frac{\kappa}{v} \frac{V_c}{V_v + V_c} \nabla P \quad (12)$$

Hereby the pressure in the product is the sum of partial water vapor pressure and CO_2 pressure which follow from the gas ideal law.

Constitutive relations. Water vapor and CO_2 are considered as an ideal gas and their material balances are derived from Fick's law. The liquid water concentration and water vapor pressure are assumed to be in local equilibrium described by an experimentally derived sorption isotherm (Weijts, 1995) (Eq. 13).

$$\frac{P_v}{P_{sat}(T)} = \frac{1.05\,W}{0.09 + W} \quad (13)$$

The evaporation rate (I_v) can be eliminated by combining Eq. 4, 5, and 6 with Eq. 13. For the production of CO_2 by yeast or baking soda the empirical expression proposed by Zhang and Datta (2006) is used

$$I_c = R_{CO}\rho_s \exp\left(-\frac{(T - T_{ref})}{\Delta T_{CO}}\right)^2 \quad (14)$$

With R_{CO} is the CO_2 production at T_{ref}. and ΔT_{CO} determines the width of the Gaussian shape function.

The change of product size is represented by the relative extension (e) and is caused by the increasing pressure in the gas cells in the dough due to the release and expansion of water vapor and CO_2 from baking powder or yeast (Fan, Mitchell and Blanshard, 1999; Zhang and Datta, 2005). Hadiyanto *et al.* (2007a) considered bread as a Kelvin-Voigt visco-elastic material for which the rate of deformation is proportional to the pressure difference between the internal product pressure (P) and the ambient pressure (P_{atm}) minus the elastic strain. A similar expression was proposed by Lostie *et al.* (2002). The two parameters involve in this expression are viscosity (η) and the elasticity (E) of product.

$$\eta \frac{de}{dt} + Ee = P - P_{atm} \quad (15)$$

Initial and boundary conditions. The initial values for heat and mass transfer are given by:

$$T(0)=T_0 \; ; \; W(0)=W_0 \; ; e(0)=0 \; ; P_c(0)=P_{amb}-P_v(0) \quad (16)$$

The boundary conditions of model are given by Eq. 17-19. At the boundary, the evaporation is mainly caused by the moisture gradient due to convective heat.

• Fluxes at the surface

$$k\nabla T = b_c(T_{oven} - T_s) - \lambda.\rho_s.D_w \nabla(W_s) \quad (17)$$

$$D_{vc}\nabla V_v = h_v(V_{ext} - V_{v,s}) \quad (18)$$

• Symmetry at the center of the product

$$\nabla T=0 \; ; \; \nabla W=0 \; ; \; \nabla V_v=0 \; ; \; \nabla V_c=0 \quad (19)$$

The weight loss in the model was determined by calculating the average water content of product, as

$$w = \frac{\int W\,dV}{\int dV} \quad (20)$$

Where V is volume of product considered for the model calculations.

Product Quality Model
Brownness

The Brownness of bakery products is mainly the result of the Maillard reaction which produces melanoidins (m_e) as coloring compound. The Maillard reaction can be approximated as a zero order reaction of which the reaction rate depends on the temperature and the water content (Van Boekel, 2006; Hadiyanto *et al.*, 2007a). In the rate equation 21, k_{me} is the Maillard reaction constant and To=363 K.

$$\frac{dm_e}{dt} = k_{m_e} \frac{\exp(9a_w)}{2.10^3 + \exp(11.3a_w)}$$
$$\times \exp\left[\frac{-E_a}{R}\left(\frac{1}{T} - \frac{1}{T_0}\right)\right] \quad (21)$$

Hadiyanto *et al.* (2007a) used equation 22 to establish the non-linear correlation between the amount of melanoidins and the degree of brownness.

$$\text{brown} = 1 - (1 - \text{brown}_0)\exp(-k_{br}m_e) \quad (22)$$

Where brown_0 is the initial brownness of the dough and k_{br} is a brownness scaling factor. Both k_{me} and k_{br} are empirical values and therefore these two parameters will be adjusted by fitting the model in experimental data estimation.

Crispness

Crispness and softness of bakery products is related to the texture of the product during consumption and are complicated sensory qualities, depending on the product rigidity/elasticity and structure. However, to have an indication of the relative performance of these attribute in the total framework of the model, we propose to simplify the system and link the degree of crispness and softness only to the amount of gelatinization and the difference between the product temperature and the glass transition temperature of the starch in the product ($\delta T = T_r - T_g$.). The glass transition temperature depends on the moisture content and the sugar/starch ratio (S/Z) for which an empirical relation (Eq. 23) given by (Hadiyanto *et al.*, 2007a) is available.

$$T_{g/m} = 457.1 - 396.32\left(\frac{S}{Z}\right) - 853.21W + 716.76\left(\frac{S}{Z}\right)W$$
$$+ 430.27\left(\frac{S}{Z}\right)^2 + 778.44W^2 - 1424.71\left(\frac{S}{Z}\right)^2 W^2$$
$$(23)$$

Products with a negative value for δT are crispy products and crispness reaches a maximum normalized value (crispness=1) when all water is evaporated which occurs for $\delta T = -\delta T_{max}$. For the degree of crispness between $\delta T = 0$ to $\delta T = -\delta T_{max}$ a linear expression is used. The parameter, $-\delta T_{max}$ will be adapted to fit the maximally encountered texture range.

$$\text{crispness} = \begin{cases} 0, & \text{if } \partial T > 0 \\ -\partial T/\partial T_{max}, & \text{if } -\partial T_{max} < \partial T < 0 \\ 1, & \text{if } \partial T < -\partial T_{max} \end{cases} \quad (24)$$

RESULTS AND DISCUSSIONS
Optimized Parameters

The results of parameter estimation are listed in Table 1. The obtained parameter values are compared to literature values. Thermal conductivity is 0.373 W/m K and corresponds to the values obtained by Jury *et al.* (2007) who reported thermal conductivity values for bread in the range 0.1-0.4 W/m K. The value of the heat transfer coefficient, which is strongly linked to the bread surface temperature, is 26.09 W/m^2 K and is close to the value obtained by Zanoni *et al.* (1995) and also in the range (20-50 W/m^{2}K) for natural convection heating reported by Demirkol *et al.* (2006). This parameter depends on equipment characteristics (like air circulation around the product) and therefore may differ from oven to oven. Rask (1989) reported for bread with water content in the range 33-45% specific heat values between 2151-2626 J/kg K. The estimated the value from our experiments falls in the middle of this range.

The parameters for the quality model are also presented in Table 1. For the Maillard reaction (k_{me}) and brownness constants (k_{br}) are estimated from □E measurements. The obtained values for these parameters are slightly below the previously reported values, just as the maximum temperature difference for the glass transition temperature (∇T_{max}). The estimated elasticity coefficient (E) is above the literature value for a cake type of product.

Table 1. Estimated parameters value and literature references

Parameter	Estimated value	Literature/start value	References
c_p [J/kg.K]	2361.2	2151-2626	Rask,(1989)
k [W/m K]	0.373	0.1-0.4	Jury *et al.*(2007)
h_c [W/ m^2.K]	26.09	20-50	Demirkol *et al.*(2006)
		30	Zanoni *et al.*(1994)
D_w [m/s]	1.7×10^{-10}	$1.3-3.5 \times 10^{-10}$	Karathanos *et al.*(1995)
k_{me} [-]	0.0039	0.0049	Hadiyanto *et al.*(2007)
k_{br} [-]	0.2241	0.23	Hadiyanto *et al.*(2007)
E [N/m^2]	1.09E6	1.5E5	Marcotte and Chen (2004)
∇T_{max} [°C]	138.9	150	Hadiyanto *et al.*(2007)

Evaluation of the Temperature Trajectories
        Figure 3 shows the development of the temperature at the crust and in the product center for convective baking and the combination of convective-microwave baking.
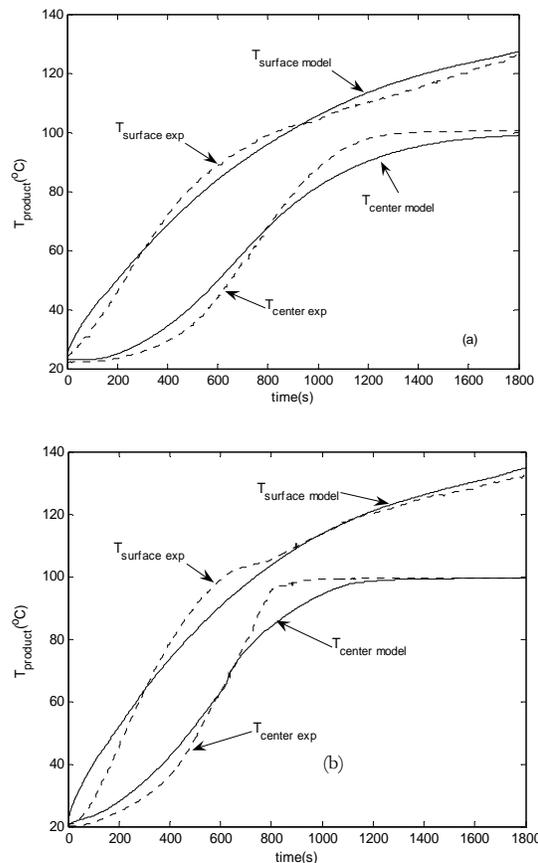

Figure 3. (a) Product temperature during baking experiments (dashed line) and for model calculations (solid line) with convective heating and (b) the combination of convective and microwave heating

        Both experiments show that the product temperature at the surface increases rapidly at the beginning. This implies that evaporation at the surface is quick and the surface temperature goes quickly towards the oven temperature. During the full baking time there is enough water available in the product center to sustain a water activity near 100% and therefore the product temperature in the center increases only slowly to the boiling temperature (100°C). Application of combined microwave and convective heating enhances the water evaporation in the product and results in a faster temperature rise in the center than with only convective baking (compare Figures 3a and 3b).
        The agreement between experiments and model is in line with the results reported in the literature (Thorvaldsson and Janestad, 1999; Zheleva and Kambourova, 2005; Zhang and Datta, 2006). However, there is systematic deviation between the

model and the experiments. This indicates that there is potential for further model improvement; for example to include the temperature and moisture dependency of parameters for specific heat coefficient, thermal conductivity and diffusivity as shown by work of Lostie *et al*. (2003) and Zheleva and Kambourova (2005). Furthermore it should be noted that the gas permeability was assumed to be constant, which should actually be a function of the product porosity, which changes during the baking process.

Evaluation of Weight loss
        The weight loss is due to the amount of water evaporated from the product during baking and depends on the baking processes. The weight loss for the two distinct baking operations is given in Figure 4.
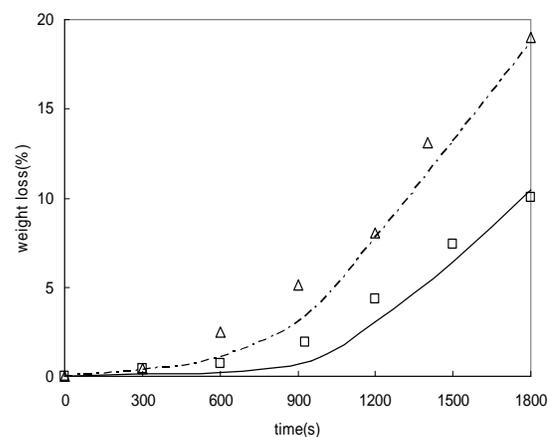

Figure 4. Product weight loss during baking with convective heating (□ : experiment; solid line: model) and combined microwave–convective heating (Δ: experiment; dashed line: model)

        In total 10-20% of water is evaporated during baking. The weight loss for convective heating is small in the initial phase and increases exponentially after 900 seconds when the temperature in the product center exceeds 70°C. During combined heating baking water evaporation is enhanced. After already 600-700 seconds the temperature in the center of the product is around 70°C, after which the weight loss starts to increase. Microwave heat accelerates the evaporation of water in the product and might be used to control the water content inside the product.
        There is a good correspondence between experiment and model after adjustment. However, the evaporation rate is overestimated for product temperatures in the range 70-95°C (600-1200 s), which is the same period where the temperature is overestimated by the model.

Evaluation of Height Extension
        The product size was measured for different baking times (see Figure 6). The size increases gradually until 1000 seconds of baking. The extension is result of the increase of internal pressure caused by

the CO_2 gas production and the evaporation of water. Model predictions and experimental results are reasonably well. After 1200 seconds, the size of product starts to decrease as a result of the decreasing pressure in the product and other non-modeled factors such as the change in gas permeability, but the results are not accurate enough to conclude that this is an essential effect.

Figure 5 shows that combined heating gives a faster development of product size, which is possible due to the increased water evaporation rate (see also section of weight loss). For convective heating at 200^oC the product size increases up to 1.2 times above the initial size, while the microwave heating 100 W yields a size around 1.4 times above the initial size.
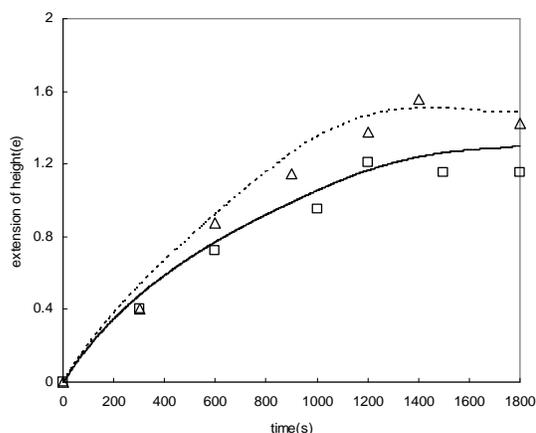
Figure 5. Height extension during baking with convective heating (□: experiment; solid line: model) and combined microwave–convective heating (Δ: experiment; dashed line: model)

Brownness Development

Product brownness is mainly the result of the Maillard reaction. The intensity of the color, which ranges from pale yellow to very dark brown, depends on the intensity of this reaction (Henares *et al*., 2006). Measured brownness values are in the range of ΔE = 24.35 for the initial dough color (pale), to ΔE = 67.12 for the highest value for a black product (Figure 6).

Figure 7 shows the correlation between the predicted brownness from the model and color measurement based on the Hunter method (Zanoni *et al*., 1995). The fair correlation implies that after parameter adjustment brownness is predicted satisfactorily and that the proposed relations (Eq. 21 and 22) can be considered valid.
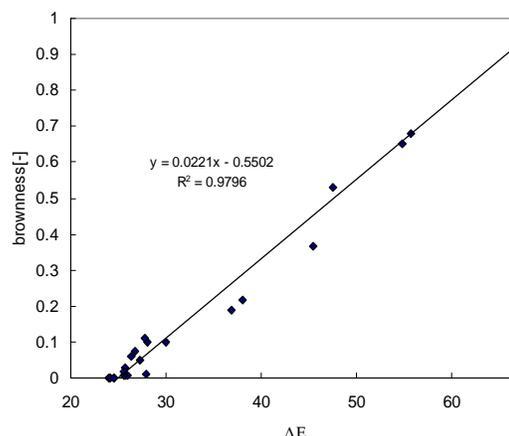
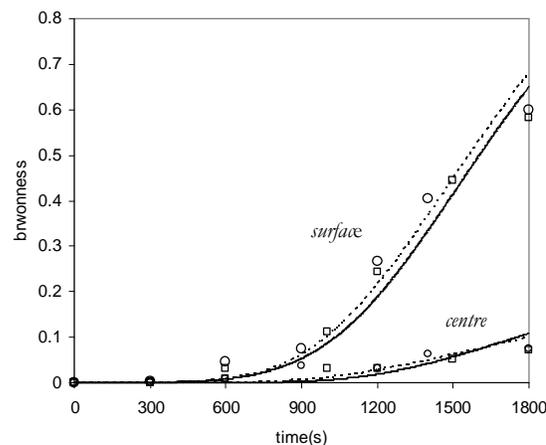Figure 7. Correlation between brownness and measured ΔE values

Figure 8. Color developments during baking in the center of the product and at the crust. Results for convective heating (□: experiment; solid line: model) and combined microwave–convective heating (O: experiment; dashed line: model)

In Figure 8 the brownness development during baking is given. The color development for the surface is significant; in the center the color changes are small. The difference in color formation between convective and combined heating operations is minimal. These results are in agreement with the observations reported by Icoz *et al*. (2004) and Sumnu *et al.* (2001).

ΔE = 24.35　　27.37　　37.19　　43.57　　57.0　　67.12
Figure 6. Formation of color during conventional baking. The ΔE value is indicated.

Crispness

The degree of crispness is in this study directly coupled to the maximum force required to break bread samples by the texture analyzer. Loads in the range 27 g to 512 g are linearly mapped to a crispness range from 0 to 1 (see Figure 9).
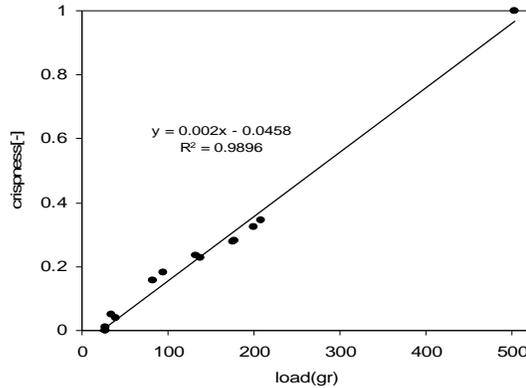

Figure 9. Correlation between crispness and load values

The scaling is obviously dominated by one extreme loading, but the high correlation with the other measurements indicates that the use of the glass transition temperature in equations 23 as a predictor for the penetration force is a proper choice.
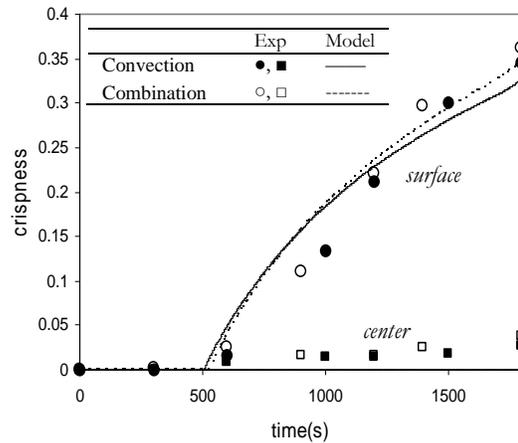

Figure 10. Crispness as a function of baking time. Experimental results (marker) and model simulation (line) for convective heating and combined heating inputs in the surface and center of product

The crispness as a function of baking time is given in Figure 10. Compared to convective heating, the combination of convective heating and microwave gives only a small difference in crispness. This effect is result of the use of the microwave which generates heat inside the product and only partly affects the surface.

CONCLUSIONS

The calibration set was obtained from baking experiments performed under constant baking temperatures and constant input of microwave power during 30 minutes and for a dynamic operation for 2.5 hours including a cooling period. The product quality was measured as a function of baking time at different positions (center and near surface) in the product.

With adjustment of the key parameters in the heat and mass transfer formulation, the model could predict the internal and surface temperatures well. The volume extension could be predicted well for most of the baking process, but still showed some deviation on the observed volume reduction in the final stage of the process. The product quality attributes brownness (based on zero order production of melanoïdines) and crispness (based on the offset of the predicted glass transition temperature) could be well correlated with color and penetration (texture analyzer) measurements, respectively. Moreover, it was shown that microwave heating hardly affects surface properties as color and crispness, but is an effective tool to control the water content of products.

Nevertheless, the calibration and validation results show that it is possible with an integrated model, which encompasses the heat and moisture transfer and some important transformation, to predict the relative change and absolute value of some key product qualities, as function of the imposed process conditions. The main benefit is that such a model can thus be used to explore the all the degrees of freedom which are offered by the dynamic variation of process conditions and process design, and to directly show the consequences on the product quality attributes.

ANNOTATIONS

a_w = water activity, [-]
C = other water binding components, $kg\ kg^{-1}$
c_p = heat capacity, $J\ kg^{-1}.K^{-1}$
D_{vc} = gas diffusivity, $m^2\ s^{-1}$
D_w = liquid diffusivity, $m^2\ s^{-1}$
e = extension of height, [-]
f = fusion factor, [-]
E = elasticity modulus, Pa
E_a = activation energy, $J\ mol^{-1}$
G_0 = reference retrogradation rate, s^{-1}
I_v = evaporation rate, $kg\ m^{-3}s^{-1}$
I_c = production rate of CO_2, $kg\ m^{-3}s^{-1}$
h_c = convective heat transfer coefficient, $W\ m^{-2}K^{-1}$
h_v = mass transfer coefficient, $m\ s^{-1}$
k = thermal conductivity of product, $W\ m^{-1}K^{-1}$
K_g = constant, [-]
k_{me} = reaction rate of Maillard reaction, s^{-1}
m_v = mass flux of water vapor, $kg\ m^{-2}s^{-1}$
m_e = melanoidins, [-]
m_c = mass flux of CO_2 gas, $kg\ m^{-2}s^{-1}$

M_w = molecular weight of water, kg mol^{-1}
P = total pressure, Pa
$P_{v,sat}$= saturated pressure of water vapor, Pa
R = gas constant, J mol^{-1}K^{-1}
R_{C0} = CO_2 generation rate, kg kg^{-1}s^{-1}
S = sugar content, kg kg^{-1}
T_∞ = hypothetical temperature, K
U^* = activation energy for product during recristalization, J.mol^{-1}
V_c = CO_2 gas concentration, kg kg^{-1}
V_v = water vapor, kg kg^{-1}
W = water content, kg kg^{-1}
Z = starch content, kg kg^{-1}
T_g = glass transition temperature, K
T_m = melting temperature, K
T_α = gelatinization temperature, K
S/Z = ratio sugar to starch, [-]

Greek letters
α = total degree of starch gelatinization, [-]
α_{max}= degree of maximum starch gelatinization, [-]
λ = evaporation heat, J kg^{-1}
ε = porosity, [-]
υ = kinematics viscosity, m^2 s^{-1}
ρ = density of solid matrix, kg m^{-3}
κ = permeability, m^2
η = dynamic viscosity, Pa s
ϕ = flux, kg m^{-2}s^{-1}

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