

# Optimal Low Switching Frequency Pulsewidth Modulation of Fifteen-Level Hybrid Inverter

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**Abstract**—The object of this paper is to operate a fifteen-level Hybrid inverter of an induction motor drive at an average device switching frequency limited to rated fundamental frequency by using Synchronous optimal pulse width modulation(SOP) technique. To reduce the number of separate dc sources, a three-level transistor clamped inverter was used as a cell in the fifteen-level hybrid inverter. Using SOP technique, optimal fifteen-level waveforms were obtained by offline optimization assuming steady-state operation of the induction machine. The switching angles for each semiconductor switch are then obtained from optimal fifteen-level waveforms based on the criteria to minimize the switching frequency as well as unbalance in dc-link capacitor voltages. Simulation results obtained from the 1.5-kW induction motor drive show THD <5% for stator currents. The results indicate that SOP technique reduces the switching frequency of operation without compromising on THD.

**Keywords**— Transistor clamped, H-bridge, medium-voltage ac drives, synchronous optimal pulse width (SOP) modulation.

## I INTRODUCTION

Multilevel inverters are now well-established and standard solution for medium and high-voltage, high power applications and power-quality demanding solutions. The advantages of multilevel inverters over two-level inverters are higher voltage operating capability with medium voltage semiconductor devices, improved output voltages with less harmonic distortion, lower common-mode voltages, less  $dv/dt$  stress, near sinusoidal input currents, smaller input and output filters, increased efficiency due to possibility of low switching operation, reduced electromagnetic interference problems and possible fault-tolerant operation [1]–[9]. In addition, the torque ripple also reduces as number of levels increases in case of multilevel inverter fed ac drives. In high-power applications, the switching losses contribute to major portion of total device losses and thus low switching frequency operation is necessary to achieve higher efficiency. However, minimizing switching frequency increases the harmonic distortion. Therefore, the challenge is to minimize the harmonic distortion while reducing the switching frequency. Presently, the most popular topologies are diode-clamped or neutral-point-clamped (NPC), capacitor-clamped or flying capacitor (FC) and cascaded H-Bridge (CHB) [3]. The CHB topologies are preferred for higher-level inverters due to requirement of least number of components and ease of control compared to other topologies. In addition, modularized circuit layout and packaging is also possible with CHB topology because each level has similar structure [10]. However, one major drawback of this topology is requirement of multiple numbers of dc-sources, which is not feasible in many applications. One of the methods for reducing the number of dc sources is to replace H-Bridge cell with NPC or FC inverters [11]. However, an important issue with the topologies having NPC or FC inverters is voltage unbalance of dc-link capacitors that further adds to harmonic distortion of output voltage waveforms. An auxiliary capacitor-based balancing approach has been proposed to equalize the dc-link capacitor voltages for NPC five-level inverter [12]. Several low switching frequency modulation techniques have been proposed for high-power applications. A new modulation method for modular multilevel inverter operating at fundamental switching frequency while successfully eliminating fifth harmonic was proposed in [13]. A novel switching sequence design for the space-vector modulation (SVM) of high-power multilevel inverters optimized for the improvement of harmonic spectrum and the minimization of device switching frequency was proposed in [14]. A new control method for seven-level cascaded inverter operating at fundamental switching frequency was proposed by Zhong Du *et al.* [15]. Model predictive current control algorithm has been demonstrated for CHB nine-level inverter with switching frequency between 425 to 500 Hz [16]. Also, an adaptive duty-cycle modulation algorithm that reduces the switching frequency by using the slope of the voltage reference to adapt the modulation period was proposed by Kouro *et al.* [17]. By using this method, the switching frequency of operation has been maintained between 285 to 785 Hz for fifteen level asymmetric CHB inverter. The selective harmonic elimination (SHE) method is one of the low-switching frequency control techniques which eliminates  $(n - 1)$  lower order harmonic components,  $n$  being the number of switching angles. Generalized SHE technique in Fourier domain for two-level single phase and three phase inverters has been proposed by Patel *et al.*

[18], [19]. Programmed PWM technique for minimizing the harmonics has been reported. [20], [21]. A new method for SHE based on six-step symmetry[22] and by use of Walsh functions to obtain Fourier spectral equations has been reported [23], [24]. A new solution to convert the transcendental equations into polynomial equations for SHE has been proposed [25]. The general problem formulation and selected solutions for both unipolar and bipolar switching patterns to eliminate the fifth and seventh harmonics are presented by Wells *et al.* [26]. A novel method to achieve fast transient response and efficient harmonic (disturbance) filtering has been achieved by using signal processing methods [27]. A minimization method to derive multiple sets of solutions for the bipolar SHE PWM method for both single-phase and three phase inverters has been presented in [28]. A real-time method by using modified triangle carrier has been proposed instead of conventional offline solution of switching angles [29]. In this method, initial guess is not required as well as switching frequency is not restricted to integer multiple of fundamental frequency [30]. SHE is also extended for multilevel inverters. A unified approach to solving the harmonic elimination equations in multilevel inverter to obtain the switching angles in the lower range of modulation indices has been reported [31]. A Bee algorithm for SHE has been reported by Kavousi *et al.* for cascaded multilevel inverter [32]. In steady-state operating conditions, SOP method for controlling five-level inverters [33], [34] and dual three-level inverters [35], [36] with maximum switching frequency of 200 Hz have been demonstrated. In case of high performance drives which are subjected to frequent transient conditions, using traditional closed-loop control techniques with SOP technique intervenes with optimal switching patterns and hence, a real-time optimization is required. Thus, initially optimal stator current trajectory tracking method has been proposed [37], [38]. Then, trajectory of an optimal stator flux vector which is independent of machine parameters or load conditions has been suggested as tracking agent [39]–[42]. Nonetheless, the application of SOP has not been reported for multilevel inverters with more than five-levels. Therefore, the objective of the present study is to demonstrate SOP technique for operating nine-level cascade inverter of induction motor drive at an average device switching frequency limited to rated fundamental frequency (50 Hz) in open loop ( $v/f$ ) control mode. It should be pointed out that proposed SOP technique can be used for any fifteen-level inverter topology by modifying the method of assigning switching angles for each power semiconductor switch based on optimal fifteen-level waveforms.

## II HYBRID MULTI LEVEL INVERTER TOPOLOGY

The hybrid multilevel inverter is a series connection of cascade half bridge cell and H-bridge inverter. In recent years multilevel inverters have been paying attention on and preferred as high power and high voltage ones [5]. Use of multilevel inverters is becoming popular for high power applications especially in the distributed generation where a number of batteries, fuel cells, solar cell, and micro-turbines can be connected through a multilevel inverter to feed a load or the ac grid without voltage balancing problems. Another major advantage of hybrid multilevel inverters is that their switching frequency is lower than a traditional low-level inverter, which leads to reduced switching losses. The topologies for high power multilevel inverters are classified into three types as shown in Fig 1. The transistor clamped inverter, the flying capacitor inverter and the H-bridge inverter.

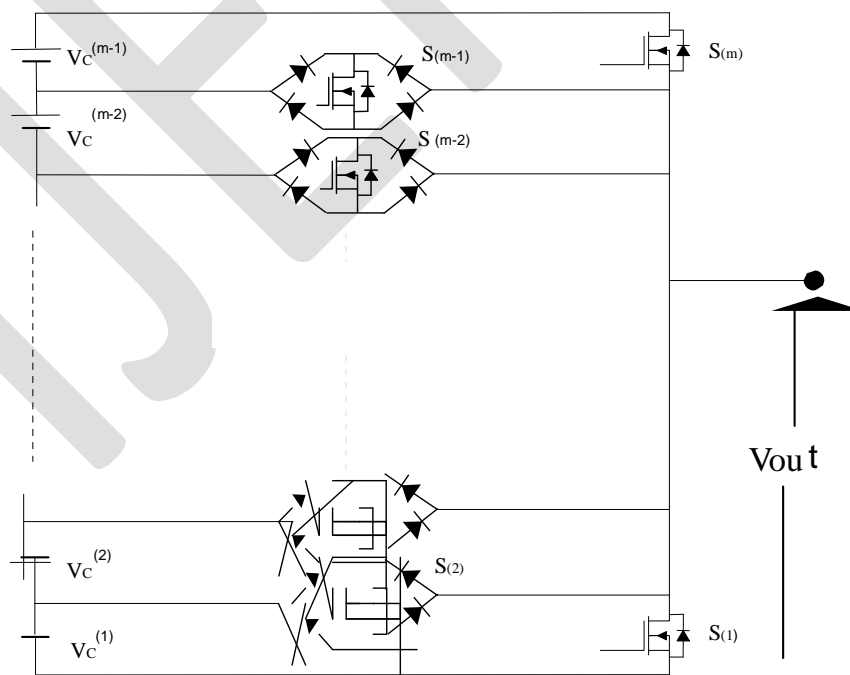


Fig 1: Multilevel Inverter Topologies

Among these inverters, the cascaded inverter has the advantages that the DC-link voltage is balanced, circuit layout flexibility, Cascaded multilevel inverter architecture has the ability to tolerate a fault for several cycles but if the fault type and location can be detected and identified, compared with the diode-clamped and flying capacitor inverters it requires the least number of components to achieve the same number of voltage levels, switching patterns and the modulation index of other active cells can be adjusted to maintain the operation under abalanced load condition.

Multilevel PWM and harmonic eradication are techniques that can be used in cascade multilevel inverters in order to achieve voltage waveforms with low total harmonic distortion (THD) with minimum switching losses and low filtering necessities. Using a multilevel layout, an effectual high switching frequency can be achieved in the output voltage waveform with each of the H-bridge modules having a relatively low switching frequency as shown in Fig 2. This approach will facilitate increased converter efficiency. Tumbling the filtering requirements would help to reduce the cost and improve the reliability and dynamic performance of the wholesystem.

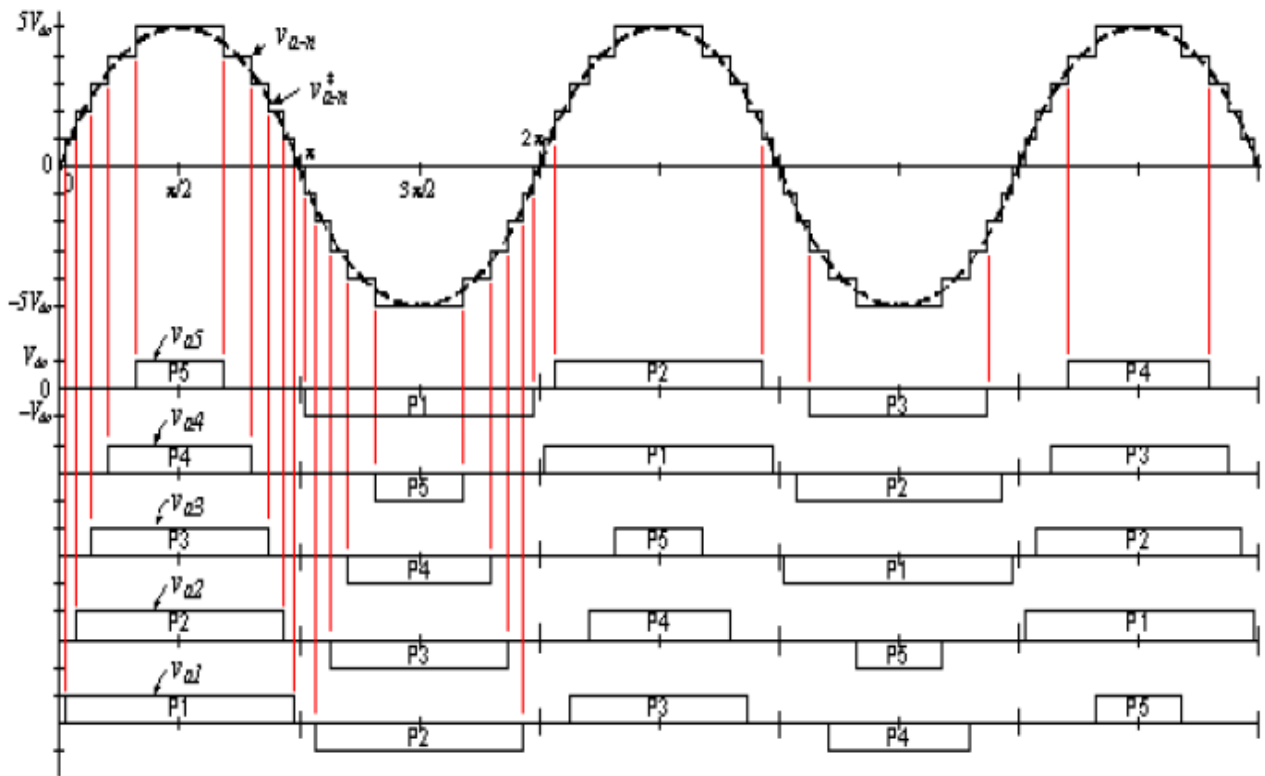


Fig2:Low loss low switching frequency multilevel inverter waveforms.

### III. SYNCHRONOUS OPTIMAL PULSEWIDTHMODULATION (SOP)

SOP generates optimal switching pulse patterns of semiconductor devices in a multilevel inverter [43]. Synchronized PWM is used in low-switching frequency applications where carrier signal at frequency ( $f_s$ ) and sinusoidal control signal at frequency ( $f_i$ ) are synchronized with each other, i.e.,  $f_s/f_i$  is an integer in order to eliminate sub harmonic frequencies which are undesirable in many applications. Synchronized PWM results in lower number of switching instants per fundamental period and even a little variation in these switching angle values will have considerable influence on the harmonic distortion of output voltage [44]. Optimization methods are suggested to predetermine switching angles offline to reduce harmonic distortion [45]. The precalculated switching angles are stored and retrieved during real-time operation.

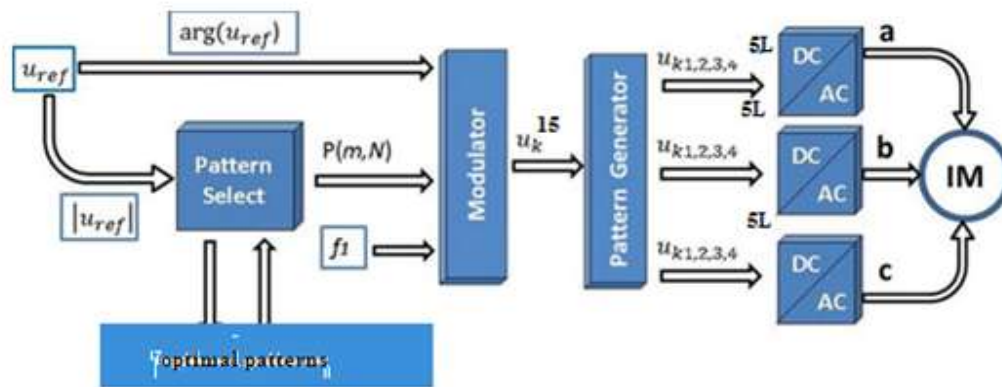


Figure 3.1 Signal Flow Graph of Fifteen level Inverter

### 3.1 Optimization Method

The goal of optimization is to generate optimal switching patterns for each steady state operating point  $(m, N)$  in order to minimize DF. The flowchart of optimization algorithm is shown in Fig. 5. The constraints of optimization are as follows [33]:

- 1) Sufficient gap ( $10 \mu s$ ) between consecutive switching angles to allow for minimum ON times and OFF times of the power semiconductor devices;
- 2) In order to maintain current modulation index value, it is mandatory to satisfy the relation (9);
- 3) Continuity of switching angles for a given pulse number over its associated modulation index range in order to avoid transients in machine currents.

In the beginning, all the possible structures for  $N = 4$  to 13 are obtained in the form of switching transitions  $s(i)$ . For each pulse number  $N$ , modulation index range is determined and then for each operating point  $(m, N)$ , MATLAB function “random” is used to generate the initial values of switching angles for further optimization while satisfying the relation (9).

We are performed computer-aided simulations to prove availability of the proposed multilevel inverter. The simulations are implemented using Matlab and it was considered to a pure resistive load. The conventional method simulation output has been obtained by using the carriers. In this proposed method the output has been obtained by using the Matlab/Simulink.

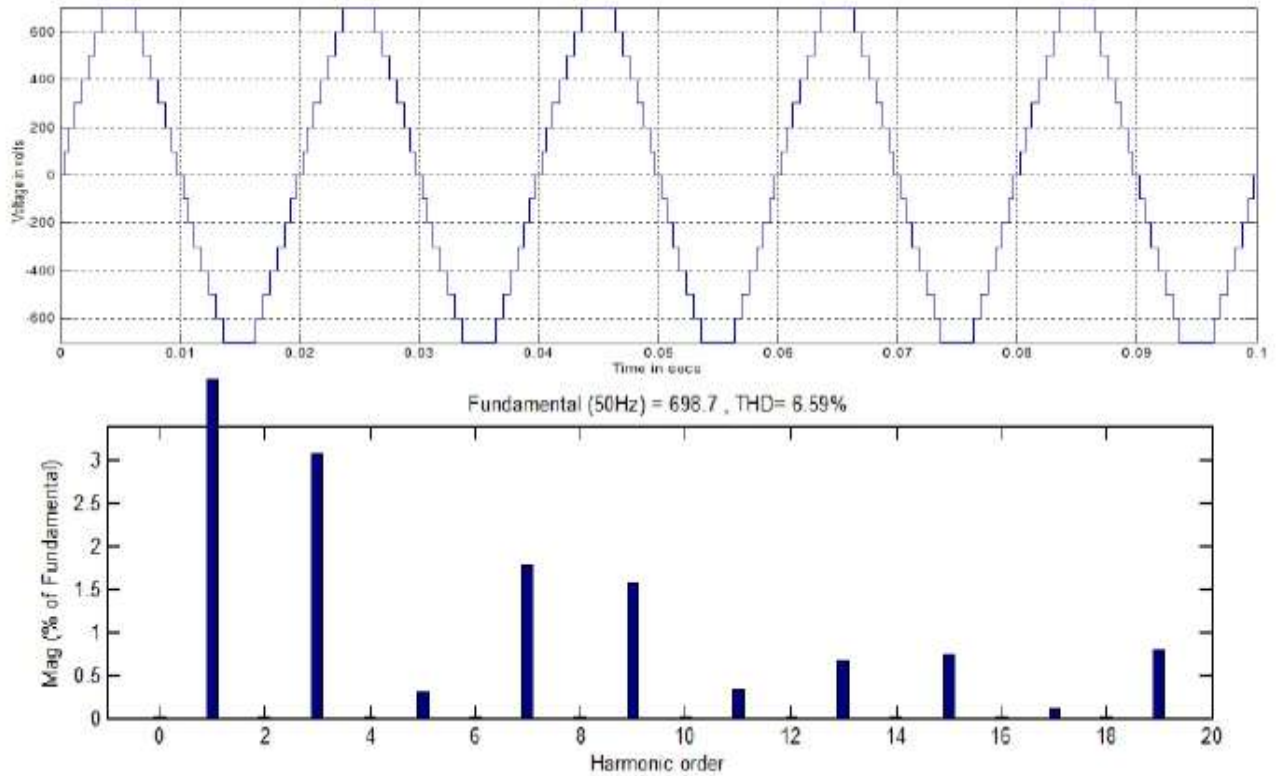


Figure 3.2 Model Simulation Results

#### IV SIMULATION RESULTS

Simulation of a 15-level multilevel inverter uses four variable dc sources to minimize the harmonics. Four variable dc sources are  $V_1=81.5$ ,  $V_2=81.5$ ,  $V_3=81.5$  &  $V_4=163$ . This simulation achieves a speedup of 500x and the execution time range is 20 milliseconds. The output voltage of 15 levels multilevel inverter as shown in Fig 5. The solution of this approach is 4.81% of THD by using genetic algorithm as shown in Fig.6.

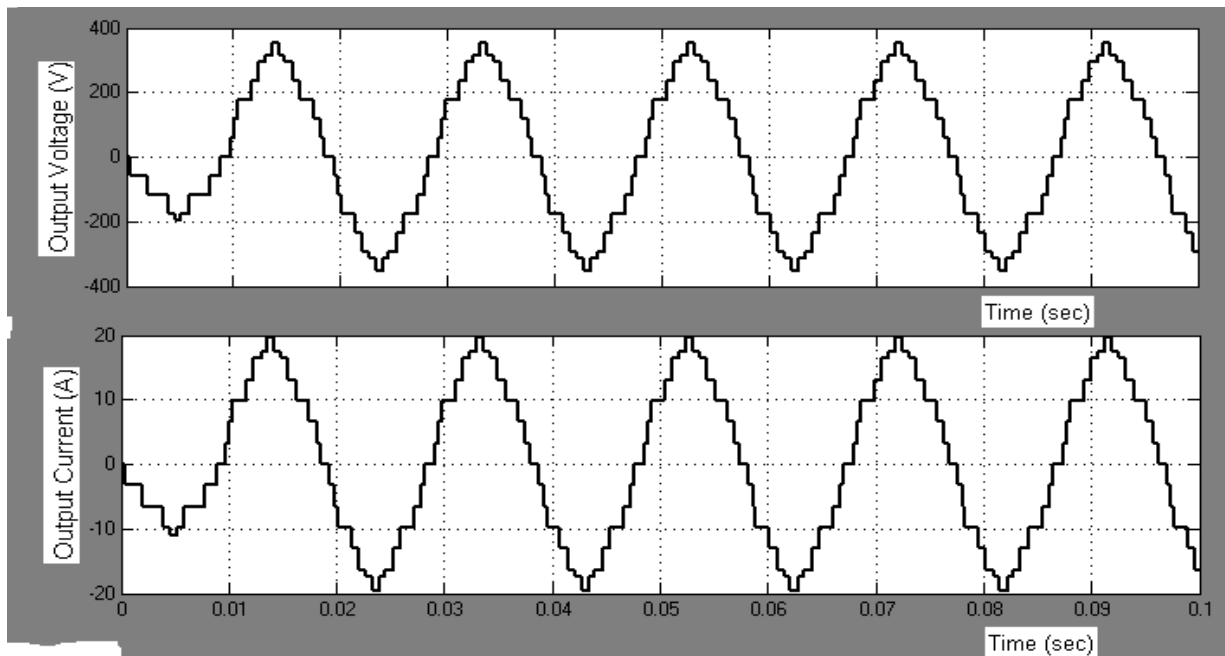


Fig 5: Output of 15 Levels multilevel Inverter

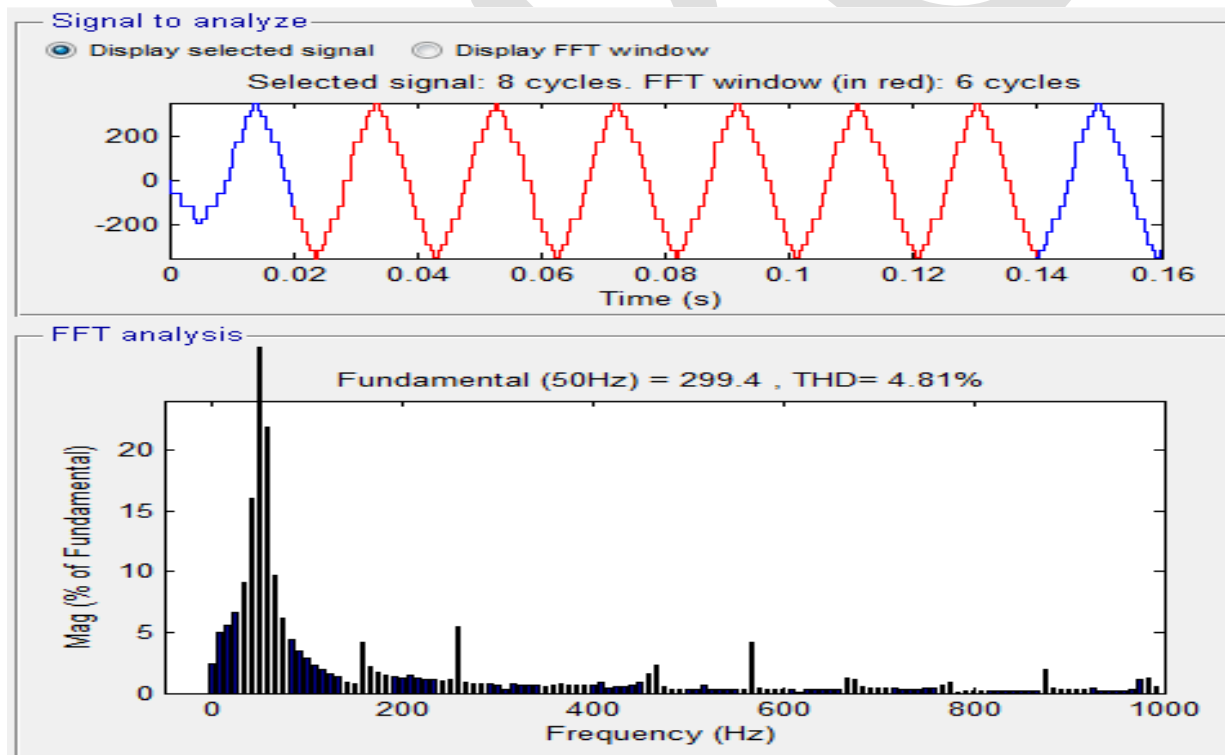


Fig 6: FFT Analysis of 15 Levels Multilevel Inverter



## VI. CONCLUSION

Cascade NPC H-bridge topology is selected for implementing FIFTEEN-level inverter due to limitations of NPC and FC topologies. Low-switching frequency operation of multilevel inverters is essential to reduce the switching losses in medium voltage high power applications. Proposed SOP technique permits multilevel inverter to operate at an average device switching frequency limited to rated fundamental frequency without compromising on harmonic distortion. Optimal nine-level waveforms are produced using SOP technique and then switching instants for each semiconductor device is determined based on the criteria to reduce device switching frequency as well as to ensure minimal unbalance in the dc-link capacitor voltages. Experimental results for four different operating points demonstrate effectiveness of the proposed modulation in limiting average device switching frequency to rated fundamental frequency without compromising on THD as well as resulting in low ripple at dc-link voltages. Compared to other low-switching frequency control algorithms for nine-level inverter like model predictive control ( $f_s = 425$  to  $500$  Hz) [16] and adaptive duty-cycle modulation algorithm ( $f_s = 285$  to  $785$  Hz) [17], the switching frequency of operation has been reduced more than five times without compromising on THD of current waveforms.

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