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Stability Analysis for Hand-arm-forearm Dynamic System

In this paper we propose a model with four degrees of freedom for hand-arm-forearm dynamic system. Using experimental data from [9] by means of the Simulink program, is built block diagram to simulate the dynamic system motion and phase diagrams are drawn by using Matlab. From the interpretation of these diagrams result, for a set of parameters (m, c, k, F_{Or}, ω), stable moves for the hand-arm-forearm dynamic system.

Keywords: stability, dinamic system, Simulink, Matlab

1. The dynamic model proposed

For the dynamic hand-arm-forearm system is proposed, in Figure 1, a model with four degrees of freedom.



 m_1 -thumb; m_2 -palm and four fingers; m_3 -forearm; m_4 -arm

2. Determination of differential equations of motion

Using Lagrange's equations (II), the differential equations of motion in matrix form are:

$$[M]{\ddot{x}} + [C]{\dot{x}} + [K]{x} = {F}$$
(1)

where:

$$[M] = \begin{bmatrix} m_1 & 0 & 0 & 0 \\ 0 & m_2 & 0 & 0 \\ 0 & 0 & m_3 & 0 \\ 0 & 0 & 0 & m_4 \end{bmatrix}$$
 is the matrix of inertia (2)

$$\begin{bmatrix} K \end{bmatrix} = \begin{bmatrix} k_1 & -k_1 & 0 & 0 \\ -k_1 & k_1 + k_2 & -k_2 & 0 \\ 0 & -k_2 & k_2 + k_3 & -k_3 \\ 0 & 0 & -k_3 & k_4 \end{bmatrix}$$
 is the stiffness matrix (3)

$$[C] = \begin{bmatrix} c_1 & -c_1 & 0 & 0 \\ -c_1 & c_1 + c_2 & -c_2 & 0 \\ 0 & -c_2 & c_2 + c_3 & -c_3 \\ 0 & 0 & -c_3 & c_4 \end{bmatrix}$$
 is the damping matrix (4)

$$\{F\} = \begin{cases} -F_o \\ 0 \\ 0 \\ 0 \\ 0 \end{cases} sin \, \omega t \qquad \text{is the column vector of the} \\ excitation force \qquad (5)$$

Matrix differential equation (1) is developed being obtained the system:

$$\begin{cases} m_1 \ddot{x}_1 + c_1 \dot{x}_1 + k_1 x_1 - c_1 \dot{x}_2 + k_1 x_2 = F_0 \sin \omega t \\ m_2 \ddot{x}_2 - c_1 \dot{x}_1 - k_1 x_1 + (c_1 + c_2) \dot{x}_2 + (k_1 + k_2) x_2 - k_2 x_3 \\ m_3 \ddot{x}_3 - c_2 \dot{x}_2 - k_2 x_2 + (c_3 + c_4) \dot{x}_3 + (k_3 + k_4) x_3 - c_3 \dot{x}_4 + k_3 x_3 \\ m_4 \ddot{x}_4 - c_3 \dot{x}_3 - k_4 x_3 + c_4 \dot{x}_4 + k_4 x_4 \end{cases}$$
(6)

To determine the motion and speed laws, in order to analyze the dynamic stability of the system, will use Simulink.

For this purpose the differential equations system (6) to rewrite as follows.

3. Using Simulink software

By rewriting the system of equations (6) result:

$$\begin{vmatrix} \ddot{x}_{1} = \frac{1}{m_{1}} \left[-c_{1}\dot{x}_{1} - k_{1}x_{1} + c_{1}\dot{x}_{2} + k_{1}x_{2} - F_{0}\sin\omega t \right] \\ \ddot{x}_{2} = \frac{1}{m_{2}} \left[c_{1}\dot{x}_{1} + k_{1}x_{1} - (c_{1} + c_{2})\dot{x}_{2} - (k_{1} + k_{2})x_{2} + k_{2}x_{3} \right] \\ \ddot{x}_{3} = \frac{1}{m_{3}} \left[c_{2}\dot{x}_{2} + k_{2}x_{2} - (c_{3} + c_{4})\dot{x}_{3} - (k_{3} + k_{4})x_{3} + c_{3}\dot{x}_{4} - k_{3}x_{3} \right] \\ \ddot{x}_{4} = \frac{1}{m_{4}} \left[c_{3}\dot{x}_{3} + k_{4}x_{3} - c_{4}\dot{x}_{4} - k_{4}x_{4} \right]$$
(7)

For each of the four differential equations of the system (7), will compose one subsystem with predefined blocks from Simulink library. For example, the differential equation:

$$\ddot{x}_{1} = \frac{1}{m_{1}} \left[-c_{1} \dot{x}_{1} - k_{1} x_{1} + c_{1} \dot{x}_{2} + k_{1} x_{2} - F_{0} \sin \omega t \right]$$
(8)

in Simulink have a block diagram shown in Figure 2.



Figure 2. Simulink block diagram of the subsystem m₁-thumb

We obtain similar block diagram for the other three differential equations.



All these block schemes it encapsulates and connects in a block diagram of the whole hand-arm-forearm system dynamic, shown in Figure 3.

Figure 3. Block diagram of the hand-arm-forearm dynamic system

4. The simulation results

Next figure was drawn the speed variation depending on displacement under a sinusoidal disturbance forces acting on the thumb, using experimental data from [9].

Four graphics were obtained, namely:





Figure 5. The arm state space diagram



5. Conclusions

From the analysis of four displacement speed charts under the force $F_0 sin\omega t$ and considering into account all the elements that make up the damping system finds that all these representations are cyclic closed curves.

From the analysis of four diagrams, displacement speed under the disruptive force F_0 sin ω t and taking into account the damping of all the elements that make up system, notes that all these representations are cyclic closed curves.

According to chaos theory, if a representation in space of states (velocity, displacement) is a closed cycle curve, then the system is stable.

This method of simulation has a future application the study of manipulators stability installed or mounted on a vehicle carrier similar to those shown in the figure below:





Figure 8. Exemples of manipulators

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