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Abstract. In physics and chemistry, the development of problem-solving skills is necessary to become an expert. A simple cognitive model to analyse such development is proposed and tested. An exploratory research was conducted with expert professors and students in initial and advanced years. A think aloud procedure was used to obtain relevant data while the participants tried to solve undefined, open problems. Solving these problems required a particular skill representative of expertise: modelling reality using science. More than 1350 solving actions were collected and related to the mental representations elaborated, developed and inter-related by solvers. The proposed model was able to account for expert-novice differences in terms of the respective distributions of solving actions among the mental representations. Large differences appeared in the mental representation of Conceptual scientific Model. In addition, advanced and initial students showed similar and significant averages of unproductive actions, while experts took very few. Experts showed high convergence in their distributions of actions among the mental representations. If the outcomes were replicated with higher external validity, the model could help researchers to analyse the cognitive mechanisms in problem-solving, and teachers to better focus their efforts on specific students' lacks.

Keywords: cognitive model, expertnovice differences, mental representations, problem-solving skills, solving actions

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A COGNITIVE MODEL TO ANALYSE PHYSICS AND CHEMISTRY PROBLEM-SOLVING SKILLS: MENTAL REPRESENTATIONS IMPLIED IN SOLVING ACTIONS

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Introduction

In physics and chemistry, the development of problem-solving skills is necessary to become an expert. Experts can be distinguished from less experienced individuals for their competent behaviours in problematic situations, which are based on the amount of accumulated domain-specific knowledge and how this knowledge is used in these situations (Ericsson et al., 2018). Experts differ from novices not only in the amount of accumulated (correct) knowledge, but also in the way that knowledge is structured in their minds (Bogard et al., 2013). Experts create larger and more interconnected mental representations than novices, which have deeper and more detailed hierarchy levels and are easily oriented to action (Björklund, 2013), in form of schemata.

This organized knowledge can be used at once when activated by singular 'triggering elements in a problematic situation. Thus, experts tend to show a schema-driven behaviour when dealing with new problems, as pointed out by Larkin et al. (1980) in an early research with physicists. On the other hand, novices tend to be more case-driven; in other words, they tend to be influenced by surface similarities of some prior and familiar cases (Ball et al., 2004). Therefore, novices show more dispersion than experts in the type of mental or physical actions taken to solve a problem. Mental actions of experts tend to converge in the analysis to tackle problems, while mental actions of novices are more divergent (Hong & Liu, 2003), which is probably due to the novices' trial-and-error procedures. Experts' convergent thinking makes possible students' guidance toward a defined goal of expertise in particular tasks.

Problem-solving by Experts and Novices in Physics and Chemistry

This research addresses the differences between experts and novices in problem-solving behaviour in the subjects of physics and chemistry. Problem-solving is a usual task used often in academic contexts for teaching and evaluating learning. It is also the main task in carrying out scientific research. Solving a problem implies the combination of several skills usually attributed to experts, such as focusing on key features to classify a problem as a situation that involves a specific well-known phenomenon (coding), or

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using schematized scientific and strategic knowledge to take the actions needed in order to find a solution. Thus, solving 'difficult', non-straightforward problems is an indicator of acquired expertise.

Chi et al. (1982) have summarized important differences between experts and novices in physics problemsolving. Despite the obvious differences in the amount of scientific knowledge, two other differences have been found:

I) Coding and problem representation: Experts and novices create different mental representations of the same problem (Chi et al., 1981). Knowledge organization in the minds of experts implies the perception of certain structural problem elements bearing categorical relevance (Boshuizen et al., 2006). Experts categorize problematic situations according to basic science principles and laws, which determine specific relations among magnitudes and quantities, while novices tend to focus on surface explicit features (e.g. slopes and springs). Thus, it is difficult for novices to take advantage of previously studied worked-out analogues and use them as source-examples in analogical transfer (Gomez-Ferragud et al., 2013). Coding differences imply differences in the mental representation of a new problem, different knowledge forms activated, thus leading to different solving actions that result in success or failure in the task (Gomez-Ferragud et al., 2014).

II) Solving strategies: Novices frequently show a lack of strategic knowledge, in addition to little science knowledge. When compared to experts, novices have difficulties in selecting and applying useful strategies, and making key inferences necessary to progress in the task. In physics, Larkin et al. (1980) found that experts usually perform a qualitative analysis of a new problematic situation in terms of some scientific conceptual model before dealing with mathematical equations. Similar findings were gained by Randles and Overton (2015) in chemistry. Among experts, the scientific model was coherently used to understand the problem statement, perform a qualitative analysis, and formalize the scientific model into equations to be solved.

In contrast, novices frequently carry out the process of searching-and-selecting for an equation in which the givens of a problem fit. Novices mix their (alternative) ideas based on the daily-life world with ideas from physics instruction so creating incoherent models that usually cause a lack of deep understanding. Thus, they rely on mathematics (Champagne et al., 1983; Randles & Overton, 2015). In chemistry, similar differences were observed. While experts address new problems using conceptual knowledge and qualitative analysis in order to achieve the solution, novices use less successful mean-ends procedures with vague and partially wrong qualitative analyses (Heyworth, 1999). The initial qualitative analysis implies that experts take relatively longer than novices to re-define the problem in terms of the scientific knowledge (Brand-Gruwel et al., 2005).

Finally, the schema-driven solving procedure permits experts to avoid their working memory being overloaded by irrelevant data (Randles & Overton, 2015). Therefore, they can focus their efforts on crucial points and manage more cognitive resources than novices via monitoring and self-regulation (Brand-Gruwel et al., 2005).

Research Focus

Previous studies described distinctive behaviours between experts and novices in solving physics or chemistry problems. However, unveiling the underlying mental processes that cause these differences is more challenging. The present exploratory research aimed at testing a simple cognitive model proposed to analyse the development of problem-solving skills in university students' way towards expertise. The model is based on the idea that solving actions highlight important content of the mental representations the solver has to build, develop and relate in order to understand and solve a problem. Therefore, each solving action can be related to some mental representation. Solving actions have been studied and classified into different taxonomies. On the other hand, the mental representations needed to understand and solve physics problems have been also described in different cognitive models, as the one by Greeno (1989) or the model proposed by Truyol, et al. (2014). In this way, the proposed model implies a step beyond with respect to previous research based on solving actions only (Meijer et al, 2006; Randles & Overton, 2015), and with respect to other studies based solely upon the mental representations elaborated when performing academic tasks (Ibrahim & Rebello, 2013).

In the university context, expertise is frequently assessed by the ability to solve difficult problems in new contexts. Hence, the focus in the present research is to test the ability of the proposed model to capture possible differences in the content of the mental representations that expert and novice solvers have to build, develop and inter-connect in order to understand and solve physics or chemistry problems at the university. If the model accounted for the expected expert-novice differences, then it would shed some light on the origin of previously documented students' ineffective problem-solving behaviours. The long-term processes for expertise acquisition

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within the university setting could be accelerated by professors, as expert performers, if they were able to realize where students' lack of knowledge and inefficient use of skills are localized when solving academic problems.

Undefined physics and chemistry problems were used in the present research because they are more demanding than defined ones (which sometimes seem to be mere exercises) and they present a potential to maximize experts-novices differences, especially in the skill of modelling reality with science.

The Model

As stated previously, the proposed model is based on the relation between solving actions and mental representations. The following lines elaborate on these two components.

Mental Representations

Solving a problem implies understanding the situation posed and the question asked, planning the way from the actual initial state to the final state, navigating in the problem space towards the goal, and reflecting on the coherence and correctness of the solution achieved (Polya, 1945). Understanding provided information implies the elaboration of mental representations capable of integrating the solver's prior-to-new knowledge in a coherent way (Kintsch, 1998). In the case of problems, understanding information given in the statement and navigating in the problem space implies being able to develop and coherently link several mental representations (Greeno, 1989). In the present research, we assume the model proposed by Truyol, et al. (2012; 2014) for problem-solving in physics.

This model considers that understanding and solving a problem implies the construction of three levels of mental representations: Situation Model (SM), Conceptual Model (CM), and Formalized Model (FM). Furthermore, it implies the coherent link and transitions between the three models (see also the model proposed by Greeno, 1989). There are forward nature transitions: Building CM from SM (BCM) and Building the FM from CM (BFM). There are also transitions of backward nature: Interpreting the formal outcomes in terms of science laws (IN) and connecting scientific results to particular real-life situations, or Instantiation (IS).

In the present research this model has been assumed as valid for chemistry problems as well, although chemistry and physics have been recognized as having epistemological differences (Jensen, 1998; Taber, 2013). Assuming that problematic situations can be conceptualized and represented in physics or in chemistry using elements of different ontological and epistemological nature, it seems that problem-solving in chemistry requires, as in physics, modelling reality using chemical principles, laws, and concepts, as well as formalizing conceptual chemical models and linking outcomes with reality in order to check the proposed solutions.

Table 1 describes the mental representation components and their characteristics as postulated in the model. It also includes some specific examples.

Table 1

Mental representations components and characteristics in the model of Truyol et al. (2014)

Characteristic	Situation Model	Conceptual Model	Formalized Model		
Components	Real-life: people and their actions, objects and their attributes, and events and their characteristics. Examples: iron (hard; rusted), butane (gas; burning), car (moving fast on a road).	Scientific models of real-life objects, events and their features and characteristics. Examples: iron \rightarrow Fe; oxidation-reduction, standard reduction potential; burning \rightarrow combustion: mixing with O_2 and energy obtained; Car moving \rightarrow point-like particle Galilean kinematics, velocity.	Logical and mathematical representation of scientific entities: quantities, relationship among magnitudes, laws for events expressed as equations or geometric relations, etc. Examples: reduction potential $Fe \rightarrow Fe^{2*}(aq)$ $*2e^{-} \rightarrow Fe(s); E_0 = -0.41$ volts; butane combustion $\rightarrow 2C_4H_{10} + 13O_2 \leftrightarrow 8CO_2 + 10H_2O;$ point-like particle kinematics $\rightarrow v = v_0 + (1/2)at^2$		
Guided by	Everyday rules on how the world is and works. Common sense, logics. Examples: The screw is red, it has rusted; With the stove fire you can cook; Using the car you will arrive sooner.	Principles and scientific laws expressed in conceptual terms. Conditions of application or validity. Conditions of applicability of scientific models. Examples: Electrochemistry; Law of con- servation of mass; Galilean Kinematics and Newtonian mechanics.	Mathematical rules and formal Logics. Examples: $\Delta G=nFE_{cell}$; Σ mass reactants= Σ mass products; t ² = 2(v-v ₀)/a		



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Characteristic	Situation Model	Conceptual Model	Formalized Model
Ontological categories	Concrete category (non- abstract): components percep- tible through senses.	Concrete and abstract categories.	Only abstract categories
Language	Natural language, figurative images and pictures.	Technical-scientific language.	Logical and mathematical symbolic language. Graphs, tables, equations, geometry.
Utility	Informal estimations; qualita- tive descriptions, analyses and prediction in the real-life world.	Estimations of orders of magnitude in attributes and characteristics of scientific phenomena.	Quantitative, more precise descriptions, explana- tions and predictions in scientific phenomena.

Source: elaborated from Truyol, et al. (2014; p. 884), Table 1.

Actions Taken when Solving a Problem

The use of specific solvers' skills can be observed by means of the actions taken in the process of solving particular problems. Research on the solving processes has been often addressed using think-aloud technique: the solver voices what they are thinking to experimenters and justifies the actions taken. Therefore, the greater ability to think about one's thinking, the richer data provided to experimenters. When using the think-aloud technique, the solvers' perceived skills are mixed with their metacognitive abilities (Desoete, 2008; Schellings, et al., 2013). In other words, the observed actions taken are triggered by the solver's metacognitive activity.

In the present research, Meijer, et al.'s (2006) taxonomy for the actions taken while solving a problem was used. This taxonomy was chosen for three reasons: a) Its elaboration and validation processes, specifically for the analysis of think-aloud protocols in problem-solving and its high reliability; b) Its metacognitive and cognitive foundation, as the observable data obtained in think aloud procedures are triggered by the subject's metacognitive activity; and c) Its hierarchical structure, which allows for a macro-analysis based on over-arching, main categories, and also for a micro-analysis based on embedded minor categories when necessary. Actions are classified in 6 main categories: orientating (OR), planning (PL), executing (EX), monitoring (MO), evaluation (EV) and elaboration (EL). Each of these main categories includes specific subordinate categories (see the Appendix in Meijer et al., 2006).

Other taxonomies for the solving activity have been proposed in the literature (Ali et al., 2018; Rosenzweig et al., 2011). In a think-aloud research developed with undergraduate students, industrialists, and academic chemists, Randles and Overton (2015) elaborated a taxonomy of positive (made/useful) and negative (absent/ useless) actions of experts in solving open-ended problems. Although this taxonomy was based on pragmatic foundations (rather than purely cognitive), it was useful for the research purposes and specific differences in solving actions taken by each of the groups, were found. According to the study, academics, acting as experts, focused on identifying the information needed, planning how to tackle the problem, identifying and framing the problem, making approximations and estimations, evaluating the strategy as well as the solution achieved, applying a logical scientific approach to their solution, and not becoming distracted by the lack of details in the question. In turn, the behaviour of undergraduates mainly involved identifying and framing the problem, using approximations, and developing a useful strategy. However, drastic differences were not found in what they do for solving the problems. Nonetheless, academics showed subtle differences in the time and effort devoted to certain specific actions that students took less frequently.

Defined and Undefined Problems in Physics and in Chemistry

Johnstone (1993) has provided a useful classification of problems in eight different types (2x2x2) according to the data given (complete/incomplete), the methods to achieve the solution (familiar/unfamiliar to the solver) and the unknowns (clearly defined/undefined, and open). In this classification, most problems used in university-level physics and chemistry instruction can be classified as algorithmic exercises; these are: 'wellstructured', 'closed' or 'single-possibility' problems (Shekoyan & Etkina, 2007). In physics and chemistry, a defined (or well-defined/well-structured) problem has a statement that defines a situation in terms of an explicit scientific model (e.g. redox or Galilean kinematics) and poses specific questions (the unknowns) in terms of numerical

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values for some magnitude coherent with the model. The necessary data to achieve the solution is provided and also fits the scientific model. Solving a defined problem usually implies the skill of building and developing the formalized model from the given scientific model. It also involves the interpretation of the mathematical outcomes in the light of the scientific model.

More interesting for students' acquisition of expert skills are problems those statements neither suggest the scientific model, nor provide the givens necessary to reach a solution. These are 'undefined', 'open-ended', or 'multiple possibilities' problems (Ringenberg & van Lehn, 2008; Shekoyan, 2009), and have been pointed up as the only problems able to develop scientist skills (Becerra-Labra et al., 2012; Gil-Pérez & Torregrosa, 1983). In an undefined problem, the problematic situation is defined in terms of the real-world. Then, solving the problem requires the skill of modelling reality by using science. This involves several actions as creating and developing a scientific conceptual model, building the formalized model from the conceptual model, and navigating this formalized model. Navigating the problem space usually means performing qualitative reasoning to link magnitudes in causal chains that obey scientific laws and principles and elaborating estimations with magnitude orders. For experts, solving an undefined problem also entails making assumptions to constrain the degrees of freedom in order to convert the ill-defined, open-ended, multiple-possibilities problem into a well-defined one (Fortus, 2009). These actions are associated with building and developing a conceptual scientific model. The final step is an instantiation process in which the expert establishes a backward connection of the science outcomes with the reality described in the statement of the problem (Truyol, et al., 2012).

In an empirical exploratory research Truyol (2012) found that university students showed significant differences in their success solving defined or undefined physics problems. Looking for the causes of these differences she first analysed the worked-out examples and the problems posed to the students along the university degree. The author concluded that undefined problems were clearly infrequent compared to the defined ones. Second, Truyol et al. (2014) investigated the possible different skills needed to solve defined or undefined problems. They conducted a case study with several expert university professors. The analyses used the aforementioned model (Table 1). Results showed differences between defined and undefined problem-solving regarding the distribution of solving effort in the mental representations and transitions. However, the differences did not appear in building or navigating the FM, or when interpreting the numerical outcomes. Hence the authors concluded that the skill "modelling reality with physics" could be poorly developed even at university.

Research Questions

The present research sought to answer the following research questions:

- Q1: Can the proposed model classify all the data provided by the informants?
- Q2: How are the solvers' solving actions distributed among mental representations when undefined physics or chemistry problems are solved by experts and novices with different levels of knowledge?
- Q3: Does the model account for problem-solving differences between experts and novices with different levels of knowledge?

Research Methodology

General Background

The present research was exploratory in nature and based on the analysis of the information provided by a group of problem-solvers in individual interviews conducted by two of the researchers. Qualitative (coding) as well as quantitative techniques (proportions; non-parametric statistics) were used.

Participants

Eleven experts, eleven 2nd year university students (initial students onwards) and 7 advanced university students in the final year (5th) of their respective degrees participated in this exploratory research. Although this is a small sample in terms of participants, they provided a high number of information units required to test the proposed model in a first approach. Experts were physicists or chemists, and university teachers with more

than 5 years of professional experience. Students were enrolled in Physics or Chemistry university degrees. The initial students had studied the topics implied in the experimental problems already.

The solving sessions took place outside the classroom time. Before starting, all of them were individually informed of the only academic purpose of the research and invited to participation as anonymous volunteers. Each student was informed of the total absence of academic consequences of his/her performance in the problem-solving session. When a participant asked for the outcomes, he/she was informed of the global results, preserving the anonymity of the participants. Although this small sample of participants lacks sufficient external validity, it can provide data suggesting further research.

Instrument and Procedures

Two physics and two chemistry undefined problems were defined following the procedure described in Truyol et al. (2014). The Appendix shows examples of the problems used. For each participant, the relevant data were: their level of expertise (low for initial students, intermediate for advanced students, and high for expert professors); the types of actions taken (6 superordinate categories defined in Meijer et al.'s taxonomy), usefulness of the actions (productive or unproductive in order to solve the problem) and the mental representation or transition associated to the action taken according to the model described in Truyol et al. (2014). An action was considered as "productive" when it led the solver to a better understanding of the problematic situation, or when it placed the solver closer to the problem goal (i.e. the action was profitable). Otherwise, the action was classified as "unproductive". Unproductive actions included incorrect actions.

Data collection was carried out along two years, according to the participants' availability. The interviewers made individual appointments with the informants respecting their work and classroom schedules. Individual interviews were conducted in a quiet room. A video camera was placed in a zenithal position to record the participants' solving actions on a paper and their speech, but not their faces to preserve anonymity. Each participant solved only one problem in their academic field (physics or chemistry). It was considered enough in the present exploratory research, as more than 1350 information units were collected and analysed in three different ways (i.e. more than 4000 classifications) to test the proposed model. Participants were as far and deep in the solving task as they could, and the process was time-consuming: 30-40 min per session.

Data Analysis

Protocols were segmented into units, each unit corresponding to a single action. Thus, a particular category of action was assigned to each unit (see previous subsection): ORientating, PLanning, EXecuting, MOnitoring, EValuation or ELaboration. Next, the action was associated to a specific mental representation or transition between them (see previous subsection): Situation Model, Building the Conceptual Model, Conceptual Model, Building the Formalized Model, Formalized Model, Interpretation or InStantiation. Finally, the action was considered as productive or unproductive to solve the problem. Therefore, each action was classified three times, according to their typology, then implied mental representation and its usefulness.

Two raters independently classified the units and the corresponding Cohen's *kappas* were computed for a 30 percent of the units selected at random. Disagreements initiated a discussion and improvement of the classification rules. Next, a second 30 percent of the units were classified. The final kappa values obtained were .78 for types of action (p<.001; substantial agreement) and .85 for mental representations or transitions (p<.001; almost perfect agreement) and the same value was obtained for the usefulness of the actions taken.

Examples of codified information units are given in the Appendix.

As the participants' sample was small in the present research, we used non-parametric statistics in order to support some observed trends in the data (Mann-Whitney and Wilcoxon tests).

Research Results

As the solutions achieved concerns, the levels of success were diverse. Only one initial student was able to deal with the experimental problem and achieved a correct, but incomplete, solution. The remaining initial students abandoned the solving procedure at an intermediate point. The advanced students attained partial

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solutions to the problem, with only one exception who gave up after feeling stuck. Experts found a complete and correct solution for their respective problems, as expected.

Type of Actions Taken

One initial student was considered as an outlier as their total amount of actions exceeded 3 standard deviations from the global mean value. This participant was excluded from the analyses.

Experts took a higher total amount of actions (n= 634) with a higher average (M= 57.6, SD= 17.8) than Advanced students (n= 370; M=52.9; SD= 26.9) or Initial students (n= 361; M= 36.1; SD= 18.0).

Experts showed significantly higher averages of productive (M= 52.6) than of unproductive actions (M= 5.0; Wilcoxon test: Z= -2.934; p= .003), and the same happened for advanced students (37.0 and 15.9; Z= -2.371; p= .018). However, in initial students the averages of productive (M= 19.2) and unproductive actions (M= 16.9) were statistically similar (Z= -1.425; p= .154). Initial and advanced students significantly differed in the average of productive actions taken (Mann-Whitney: U= 9.0; p= .011) but showed comparable averages of unproductive actions (U= 32.0; p= .769). Experts showed significantly higher average of productive actions than initial (Mann-Whitney; U= 4.0; p< .001) or advanced students (U= 16.5; p= .044), and significantly lower average of unproductive actions (U= 6.5; p< .001; U= 2.5; p< .001). In terms of percentages, 91.2% of the actions taken by experts were productive, compared to 53.2% and 69.9% for initial and advanced students, respectively. Experts took few unproductive actions and the rare errors made were immediately corrected because of their effective monitoring.

According to the types of actions considered, the averages are shown in Table 2.

Table 2

Average of actions taken per participant according to the level of expertise

	OR	PL	EX	МО	EV	EL
2 nd year-Students	5.4	7.4	12.2	5.6	2.6	2.9
Advanced-Students	9.3	12.1	14.3	8.9	4.3	4.0
Experts	7.7	8.6	20.9	5.2	6.0	9.2

Comparisons for the amounts of each type of action taken were performed. Initial and advanced students showed no significant differences (Mann-Whitney: U> 17.0; p> .075 in any type of action). Experts obtained a significantly higher average of Elaboration actions than advanced students (U= 0.5; p< .001) and also higher averages of Executing, Evaluation and Elaboration actions than initial students (U< 22.0; p< .020 in these types of actions).

Mental Representations Associated with the Actions Taken

Actions were associated to one mental representation (SM, CM, FM) or to one transition between mental representations (BCM, BFM, IN, IS). Some actions (personal comments, feelings, self-evaluations of the own abilities, anecdotal comments, etc.) could not be associated to any mental representation concerning the experimental problem and were classified as "no mental representation implied" (NM). Table 3 shows in some detail the mean values of the actions taken by experts, advanced and initial students in each of the mental representations and transitions (except for the NM category), when they try to solve the undefined problem. Table 3 also shows those comparisons achieving significance.

Table 3

Mean amount of actions implied in each mental representation or transition, according to the level of expertise. Pair comparisons with significant differences are shown

Actions taken in each mental representation and transition		Ave	rage per parti	cipant
		Initial	Advanced	Experts
Elaborating a useful Situation Model (SM)	тот	7.20	10.29	1.64
PRO: Experts < Initial << Advanced	PRO	4.30	7.86	1.64
UNP: Experts << Initial = Advanced	UNP	2.90	2.43	0.00
Recognition of objects and events as part of the real world; understanding; Making sense; Giving meaning to the ideas in the statement (OR);	PRO	2.50	5.14	1.36
Looking for particular information in the statement; Self-questioning (PL)	UNP	0.50	1.14	0.00
(Colf) Explanations on the problematic situation of the domand (EV)	PRO	1.30	1.00	0.27
(Self)-Explanations on the problematic situation or the demand (EX)	UNP	1.20	0.43	0.00
Claiming (nortial) understanding Commenting on teak demands (MO)	PRO	0.10	0.29	0.00
Claiming (partial) understanding; Commenting on task demands (MO)	UNP	0.40	0.14	0.00
Finding similarities with other real situations (EV);	PRO	0.40	1.43	0.00
Elaborations and inferences from ideas in the statement (EL)	UNP	0.80	0.71	0.00
Building the Conceptual (scientific) Model (BCM)	тот	10.00	10.00	6.18
PRO: Initial = Advanced = Experts	PRO	7.00	7.86	5.45
UNP: Experts << Initial	UNP	3.00	2.14	0.73
Identifying an underlying phenomenon; Determining characteristic properties and magnitudes of objects and events; Hypothesizing (OR)	PRO	4.10	5.00	2.00
Determining a specific magnitude as associated with the problem demand; Discriminating relevant features to be modelled from distracting details; Outlining a solving schema (PL)	UNP	0.90	0.14	0.19
Transferring from one representation to another; Outlining, drawing a diagram; Associating magni-	PRO	2.40	2.71	2.73
tudes to features (EX)	UNP	1.10	0.71	0.00
Monitoring aloud the process; Noticing lack of knowledge or retrieval failure; Troubles about	PRO	0.20	0.14	0.73
information provided (MO)	UNP	0.40	0.14	0.27
Finding differences and analogies with previous problems (EV)	PRO	0.30	0.00	0.00
Inferring (EL)	UNP	0.60	0.14	0.27
Developing the Conceptual (Scientific) Model (CM)	тот	6.10	8.71	23.00
PRO: Initial < Advanced << Experts	PRO	2.90	6.29	21.64
UNP: Initial = Advanced = Experts	UNP	3.20	2.43	1.36
Identifying scientific principles and laws; Activating scientific conceptual knowledge (OR)	PRO	0.50	3.29	7.91
Imposing restrictions; simplifying; Explaining how a scientific model can solve the problem (PL)	UNP	1.00	0.86	0.64
Connecting magnitudes using scientific laws and principles; Science-based reasoning to describe, explain and predict events; Performing estimations of the unknown magnitude; Running the model	PRO	2.00	2.43	7.55
qualitatively; Analysing extreme situations; making approximations (EX)	UNP	1.30	1.00	0.00
Checking the model; Making amendments or corrections; Noticing retrieval failure or lack of knowl-	PRO	0.10	0.14	2.09
edge; Inconsistency detection; Comprehension failure (MO)	UNP	0.70	0.43	0.45
Inferring; Evaluating the model when running it (EV)	PRO	0.30	0.43	4.09
Model-based explanations; Connecting the model with (ideas in) the statement (EL)	UNP	0.20	0.14	0.27
Building the Formalized Model (BFM)	тот	3.40	4.29	4.45

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PRO: Initial < Experts	PRO	1.40	3.14	4.45
UNP: Experts < Initial = Advanced	UNP	2.00	1.14	0.00
Giving values to magnitudes; Hypothesizing (OR) Jsing information sources to find suitable numerical values for the magnitudes when necessary:	PRO	1.20	1.43	1.18
looking for tables or graphics; Choosing units; Giving meaning to graphs, axes, setting up a coordinate system (PL)	UNP	0.40	0.14	0.00
Writing algebraic (equations or inequations) or arithmetic or graphical connections among magni-	PRO	0.10	1.71	3.27
tudes or quantities or chemical reactions in symbolic terms (EX)	UNP	0.50	0.43	0.00
Numerical quantities required but not found; Noticing retrieval failure of formulae associated with a	PRO	0.10	0.00	0.00
scientific law; Giving meaning to symbols or formulae (MO)	UNP	0.70	0.57	0.00
Justifying and evaluating the chosen numerical values or the written algebraic relations (EV)	PRO	0.00	0.00	0.00
	UNP	0.40	0.00	0.00
Developing the Formalized Model (FM)	тот	3.30	7.57	8.55
PRO: Initial = Advanced < Experts	PRO	2.00	5.29	8.55
UNP: Experts < Initial = Advanced	UNP	1.30	2.28	0.00
Activating knowledge on mathematical expression of laws, functional inter-dependence of magni- tudes, geometrical shape of entities, etc. (OR)	PRO	0.30	2.00	0.55
Formulating a plan to formally solve the problem (outlining the formal trans-formations); Sub- goaling; Using books, tables, internet to explain formal trans-formations (PL)	UNP	0.00	0.43	0.00
Performing only some algebraic transformations or arithmetic computations; Elaborating tables or	PRO	1.50	2.57	6.27
graphics; Charge and mass balancing in chemical reactions (EX)	UNP	0.70	0,57	0.00
Obtaining an specific algebraic or arithmetic or graphical relationship for the unknown, used to	PRO	0.00	0.00	1.00
answer the problem (EX)	UNP	0.10	0.00	0.00
Nonitoring the correctness and usefulness of the formal transformations; Noticing inconsistencies	PRO	0.20	0.71	0.73
or errors (MO)	UNP	0.50	1.29	0.00
Interpretation (IN)	тот	1.40	3.42	3.55
PRO: Initial << Advanced = Experts	PRO	0.30	2.71	3.55
JNP: Experts << Initial = Advanced	UNP	1.10	0.71	0.00
nconsistency or Error detection and correction when trying to make sense out of the quantities and	PRO	0.00	0.29	0.18
relationships (MO)	UNP	0.20	0.14	0.00
Jsing science to evaluate the obtained or chosen numerical values, or to assess the relationship	PRO	0.30	2.43	3.37
among magnitudes (EV)	UNP	0.90	0.57	0.00
nstantiation (IS)	тот	1.10	2.14	4.82
PRO: Initial = Advanced << Experts	PRO	0.40	1.00	4.82
JNP: Experts < Initial = Advanced	UNP	0.70	1.14	0.00
Elaborations to explain the meaning of the obtained outputs in the real world: connecting back to	PRO	0.40	1.00	4.82
the objects and events in the statement; Concluding, trying to satisfy the problem demand (EL)		0.70	1.14	0.00

The notation "<; <<; =" respectively mean p<.05; p<.01; p>.05 according to Mann-Whitney tests.

Figures 1 and 2 show the data in a visual format for easier comparison. In productive actions implied developing the conceptual model (CM), in building and developing the formalized model (BFM and FM), and in back transitions (IN and IS) there was a progression from initial to advanced students, and to experts as shown in Figure 1. Differences between initial and advanced students achieved significance only in SM (U= 11.5; p= .020), CM (U= 12.0; p= .024) and IN (U= 8.0; p= .005). However, when BFM and FM actions were considered together, advanced students showed significantly higher averages of Executive formal actions than initial students (U= 14.0; p= .037). In turn, experts-advanced students' differences in productive actions were significant in SM (U= 3.0; p< .001), CM (U= 1.5; p< .001), FM (U= 15.5; p= .036) and IS (U= 5.0; p= .02).



Figure 1

Mean amounts of productive actions taken by Experts, Initial and Advanced students according to type and mental representation and transition involved

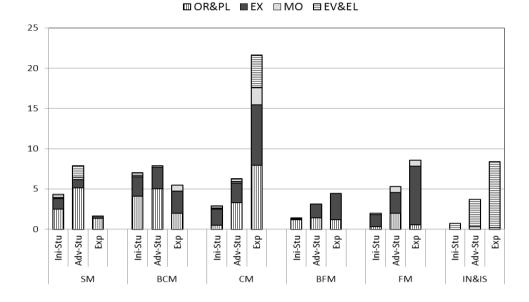
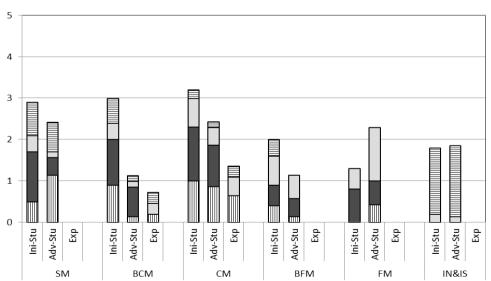


Figure 2

Mean amounts of unproductive actions taken by Experts, Initial and Advanced students according to type and mental representation and transition involved



□ OR&PL ■ EX □ MO ■ EV&EL

In unproductive actions, the opposite progression was obtained, as depicted in Figure 2. However, differences between initial and advanced students did not reach significance in any mental representation or transition. Experts showed significantly smaller averages of unproductive actions than students in every mental representation, except in CM. In this mental representation, the amount of actions taken by experts was so large that the low proportion of unproductive actions in CM (only 6%) implied an average comparable to the students' averages.



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Finally, the individual distributions of actions among mental representations were compared within each group using the SD/Mean ratios for productive and unproductive actions in each mental representation and transition considered in the model. The respective ranges for these ratios in productive actions were 0.33-1.07 for experts, 0.42-1.73 for advanced students and 0.44-2.41 for initial students. Correlations between pair of participants were computed using the 16 values for the productive and unproductive types of actions. The mean value of the correlations between pairs of advanced students was 0.57 (ranging 0.14-0.93) and a similar mean value was obtained for initial students 0.54 (0.07-0.89). However, the mean correlation between pair of experts was 0.90 (0.69-0.98): in this case, unproductive actions were not considered due to the frequent 0 value. Hence, the agreement among experts seemed to be higher than the agreement among initial students or advanced students. The distributions were averaged for experts, and for initial and advanced students, and the 16 averages were then compared using the Pearson correlations. Experts' averages were moderately correlated with the ones of advanced students (r(16) = .52), but the correlation was clearly lower with the initial students' averages (r(16) = .15). Initial and advanced students' averages were highly correlated (r(16)= .75).

Discussion

First, the proposed model to analyse experts' and novices' problem-solving skills accounted for all the information provided by the participants. The inter-rater reliability in the different classifications reached satisfactory values.

Second, the model accounted for expert-novice differences and described these differences in terms of the content (the solving actions) of the different mental representations elaborated and inter-related by solvers. Experts showed a higher global average of solving actions than initial (2nd year) and advanced (5th year) students. Experts took more productive actions than advanced students, and the latter took more productive actions than initial students. However, the average of unproductive actions of advanced students was equivalent than the one of initial students, and higher than experts' average.

In the present research a certain progression with the university year was observed in terms of productive actions taken, as expected. Despite this, an expected decrease of unproductive actions did not appear: the differences between advanced and initial students almost vanished when the averages per participant were compared. In addition, advanced students' averages showed a medium strength correlation with experts' averages and a medium-high strength correlation with initial students' averages. Advanced students showed similarities with experts mostly in productive actions, and similarities with initial students regarding unproductive actions. Thus, university students seemed to learn suitable solving procedures along the years, but the learning was insufficient to solve undefined problems with an implicit scientific model. In fact, in the present research significant differences in problem-solving actions were found between experts, advanced students, and initial students in all types of actions taken to elaborate and develop the conceptual (scientific) model.

Slight differences in problem solving actions between initial students and graduates were observed in Kohl and Finkelstein's (2008) study on problem-solving in physics. Using a different taxonomy, Rosenzweig et al. (2011) also differentiated productive from unproductive metacognitive actions when comparing problem-solving of middle-school students with learning disabilities, low-achieving students, and average-achieving students. When the problem stated was difficult, the mean number of verbalized productive actions decreased as the group ability increased, and the amount of verbalized unproductive actions decreased as the group ability increased. Results in the present research show a similar trend.

According to the types and amounts of actions associated with each mental representation or transition, initial students, advanced students and experts showed different behavioural patterns. A summary is provided in the following lines.

Elaboration of a useful Situation Model (SM): Although the experimental problems were selected to avoid lack of understanding at SM level, students in general elaborated this representation by dealing with features and by activating prior experiences in the real world. Initial and advanced students showed significant percentages of orientating and planning actions while developing the SM. Moreover, in initial and advanced students nearly 20% and 25% of these actions respectively were unproductive. This is coherent with previous findings in the sense that novices tend to be disturbed by surface details instead of structural information (Boshuizen et al., 2006; Chi et al., 1981; Randles & Overton, 2015). Conversely, experts took fewer actions associated with the SM (3% of the total actions).

Building the Conceptual (scientific) Model (BCM): Students took relative high amount of actions in BCM

trying to identify the appropriate scientific model and the relevant magnitudes implied. Most advanced students succeeded in this effort, but most initial students did not. Experts built the scientific model more quickly: in a hypothesizing process, they activated a previously known conceptual model and then tested their suitability by running it. Experts did not encounter obstacles transferring from the situation model to the conceptual model. Their quick and efficient coding allowed them to choose the physics or chemistry model efficiently and to activate a vast prior knowledge to go ahead. In agreement with previous outcomes (Ball, et al., 2004), experts showed a schema-driven behaviour, and the schema was a well-known scientific model.

Developing the Conceptual Model (CM): Experts elaborated a broader conceptual scientific model in comparison to the one elaborated by advanced or initial students. Most of experts' solving actions (40%) were taken in order to develop this mental representation. As said before, experts tested the hypothetic scientific model built before by running it in their minds, considering extreme situations and using approximations instead of specific numerical values for the magnitudes. The pre-eminence of CM over other mental representations when solving undefined problems was also observed by Truyol et al. (2014) in their analysis of expert physicists. In comparison, advanced and initial students devoted lower percentages out of the total actions taken in the CM mental representation (advanced students 17%; initial students 13%). The main difference in productive actions between experts and students was given in this mental representation. Most initial students were unable to elaborate and/or run a suitable scientific model in their minds. Particularly, most of them were unable to identify the appropriate magnitudes to describe the situation in the problem, and only a few were able to determine the appropriate magnitude for the unknown. Although some advanced students found similar difficulties, they were able to move on and elaborate connections among magnitudes.

Building the Formalized Model (BFM): Most initial students expressed wrong or inappropriate relations among magnitudes. They also failed at identifying appropriate data in tables or graphs or interpreted these data wrongly. All of them failed to address the absence of quantities and were unable to assign appropriate quantities to the relevant magnitudes. Most gave up and quit in this phase. Some advanced students also used ineffective equations although none wrote incorrect equations. Advanced students also claimed for specific quantities to achieve a solution for the problem. In fact, they were able to assign reasonable numerical values to the magnitudes in order to advance with the problem-solving process. Randles and Overton (2015), and years before Gil-Perez and Torregrosa (1983), found that novices tend to go quickly on mathematical equations when solving chemistry or physics problems respectively. Therefore, when numerical data for the relevant and well-defined magnitudes were not provided in the problem statement, novices showed difficulties to advance. In the present research all the students, advanced or initial, quit the problems without achieving a correct and complete solution in formal terms.

From this stage on, only experts were able to correctly perform the last solving steps: developing the Formalized Model (FM), Interpretation (IN) and finally Instantiation (IS) to connect the problem outcomes to real world. Novices showed troubles to correctly interpret what they were computing, the graphs or the numerical data they were looking for. In fact, the unproductive actions associated with Interpretations doubled the productive ones. In addition, novices provided few correct elaborations connecting science to the real world.

As the analysis of solving actions taken concerns, the results obtained in the present research are comparable to the ones reported in Randles and Overton (2015). Although categories in both studies cannot be related in a univocal way, quantitative results show that professor/student differences in percentages were of the same sign in both studies. Qualitatively, this means that experts overcome students in the same types of actions and *vice versa*, although the respective percentages were different. One disagreement between the present research and Randles and Overton's was observed in the category related to '*dealing with equations and calculations*'. In Randles and Overton (2015), undergraduates showed a higher mean percentage over professors, but in the present research they showed similar mean percentages. This difference might be explained by the nature and difficulty of the experimental problems posed to the undergraduates. In the present research, novices were unable to develop the formalized model due to a lack of numerical data in the problem statement. Thus, they dealt with equations in a lesser amount than experts.

Additional outcomes support and describe previous findings in terms of a cognitive basis. Experts showed higher similarity among their individual behaviours than did initial or advanced students, in agreement with the outcomes obtained by Hong and Liu (2003). These authors concluded that experts used a similar schema-like piece of knowledge to analyse and solve the posed problem. This might explain the high agreement among experts, as compared with students. This schema-driven behaviour has been also exposed by Larkin et al. (1980)

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in expert physicists. In the present research, the mean agreement among pairs of initial students or among pairs of advanced students was similar. This suggests that in academic problem-solving the state of expertise is quite homogeneous regarding the solver's behaviour, while intermediate states show greater levels of heterogeneity due to the variability in individual's knowledge and learning rhythms.

The students were able to elaborate, use and connect all the mental representations and transitions considered, as experts did. However, when the content and quality of the representations were analysed, large differences emerged. These results are in agreement with Kohl and Finkelstein's (2008) conclusions in their study on the way experts and novices use multiple representations in physics problem solving. The links between different mental representations while solving design problems were the focus in Björklund's (2013) research, and also in Kohl and Finkelstein's (2008) research on physics problem-solving by initial university students and graduates. In the present research, explicit connections between representations necessary to solve the problem, or to make sense of the outcomes, were coded as: a) EXecuting actions associated to Building the Conceptual Model or to Building the Formalized Model; and also as: b) EValuation and ELaboration actions, associated to INterpretations and InStantations respectively. Experts' average and percentage of these explicit productive connections were clearly higher (12.2 actions/expert; 19.3% out of total actions taken by experts) than the novices' corresponding values (3.5; 8.4%). Indeed, experts successfully linked different mental representations more frequently than novices, which is in line with evidence reported by the previously mentioned studies.

Conclusions, Limitations and Possible Implications

The present exploratory research aimed at answering three research questions. The answers to these questions implied using the proposed model to describe and compare the experts' and students' distributions of solving actions in the different mental representations necessary to understand and solve undefined physics or chemistry problems, i.e. problems in which the statement does not provide the scientific model or data, but only a problematic situation in the real world.

Naturally, differences between experts and students were evident in the solutions achieved, as well as in the distributions of solving actions among mental representations. These distributions pointed out specific students' lack of expert knowledge. The main shortfalls were detected in the development of the mental representation Conceptual (scientific) Model, where the expert-student differences were large, even for advanced students. This suggests that university physics and chemistry curricula should help students develop the important skill of modelling reality with science in a more effective way. In addition, advanced students' distributions were similar to experts' distributions in some productive actions, but they were very similar to initial students' distributions in unproductive actions. However, differences between advanced and initial students were observed in productive actions associated with the Conceptual and Formalized Models. This implies that throughout the university degrees students acquire new important skills, but it also draws attention to the effectiveness of university curricula to correct students' erroneous conceptions present at the initial courses and to provide them with applied knowledge.

In addition, experts' distribution of actions in the mental representations showed high level of agreement, whereas the respective levels of agreement among initial or advanced students were clearly lower. This suggests that experts share a similar knowledge and that it is used in a schema-driven way and, therefore, expertise is characterized by knowledge-in-action schemata.

As said before, these provisional results lack enough external validity and a larger volume of data from more representative samples are needed before a strong suggestion can be made to teachers regarding what needs to be done. The experimental problems should be more varied as well. Notwithstanding, the present research showed convergence with similar previous studies in their qualitative results, which encourages future research in this direction. If the obtained differences between experts, advanced and initial students were replicated, university teachers could improve students' education by focusing on these outcomes.

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Appendix. Examples of problems and selected fragments of the interviews

Physics problem: Two identical racing cars arrive at the same time to the last corner of the circuit, after which is the finish line. Both cars describe a perfect semi-circular curve on the track without sliding, one moving "inside" with a smaller radius, and the other "outside" with a larger radius. Please reason which car will win.

Units (Expert's protocol. Units are not necessarily in order)	Action	Mental Repres	Utility
() One of the cars is moving "inside" and, the other one, it moves "outside" in parallel trajectories	OR	SM	PRO
The described curves are perfect semi-circles of 180 degrees for both carsThen, this is a case of circular motion.	OR	BCM	PRO
The centripetal force equals the mass times the speed squared, divided by the radius (writes Fc= m1 v12 / R1).	EX	BFM	PRO
Here, v1 is the speed of car 1 when it is describing the curve without sliding.	MO	СМ	PRO
v1 will be the higher when the friction force is the maximum possible for the car without sliding.	EX	СМ	PRO
From here I will obtain the speed of the car 1, v1.	PL	FM	PRO
() As the radius R1 is greater than R2, then the speed v1 is greater than v2	EV	IN	PRO

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Units (Student's protocol. Units are not necessarily in order)	Action	Mental Repres	Utility
Here, the statement says that both cars arrive at the same time (he/she underlines the sentence in the statement),	PL	MS	PRO
this means that speed 1 is equal to speed 2 (writes v1 = v2)	EX	CMC	UNP
Here it says that the cars handle the curve without sliding (he/she underlines the sentence in the statement), \dots	PL	MS	PRO
does this mean that there are no other forces acting on the cars?	EX	CMC	PRO
As the distance is larger for one car than for the other one, the car moving "inside" will arrive first.	EL	IS	UNP
Interviewer: Can you suggest a solution from the information provided in the problem? (Thinks for a few seconds) No, because I do not remember the equations for the circular motion.	MO	CMF	UNP

Chemistry problem: A clean steel wok is sprinkled with some drops of water. Some time later, a reddish-yellowish substance appears under a water drop. Using your knowledge in chemistry, please explain the observed change.

Units (Expert's protocol. Units are not necessarily in order)	Action	Mental Repres	Utility
Probably it is a redox reaction. I mean, the iron has to be oxidized because its colour has changed.	OR	BCM	PRO
Obviously for the iron to oxidize there must have been a reduction process in the other way. (Writes while speaking Fe: oxidation; H2O: reduction).	EX	СМ	PRO
(He/she schematically draws the reduction process on the paper). The electrons that go from one side to the other obviously came out of the iron, and there is some species here (he/she points to the water half-reaction he/she just wrote) that must have taken the electrons.	EX	BFM	PRO
(He/she writes the equality of concentrations between protons and oxydryl: [OH-]= [H+] while speaking) The concentration of oxydryls is equal to the concentration of protons	EX	FM	PRO
This diagram (a Pourbaix diagram deliberately searched for and found in internet) indicates that if I go up this line (points to the y-axis) what is there (the wok's oxide) must be more or less in this region.	EV	IN	PRO
If this (he/she refers to the reddish-yellowish substance in the wok) is soluble, probably we have a Fe2O3 oxide with n water molecules.	EL	IS	PRO

Units (Student's protocol. Units are not necessarily in order)	Action	Mental Repres	Utility
Can I look up [the information] in books?	OR	NM	PRO
Let me think, because this thing that looks black (he/she points the image), isn't it the soot that gets formed in the pot when it reacts with heat? The pot goes bad.	OR	SM	UNP
Can't it be like an oxidation or something that the water produces on the pot's steel?	PL	BCM	PRO
I'm going to look up (in the book) the value of the oxidation potential of water to find out whether it is an oxidant or not.	PL	BFM	PRO
I'm sorry, but I haven't started studying physical chemistry yet () I feel that I'm lost; I'm not going anywhere.	MO	NM	UNP
I know there is water: (He/she writes 2H2O + 2e- →H2 + 2OH-)	EX	FM	PRO
(He/she looks at the reduction potentials table) The potential for iron is negative.	PL	BFM	PRO
Let's write it down. (He/she writes: Fe \rightarrow Fe2+ + 2e-; E°= -0.44V)	EX	FM	PRO

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Units (Student's protocol. Units are not necessarily in order)	Action	Mental Repres	Utility
If the potential is negative, it means that the reaction does not take place, or that for taking place it needs energy, or temperature. Because I believe that it happens anyway, but it is not favourable (sic).	EV	IN	UNP
But if the delta of the cell redox potential is a positive value, it is true that every time you put a drop of water, the pot stains like this.	EL	IS	UNP

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