

Abstract. Graphs are often used to represent mathematical functions, to illustrate data from social and natural sciences, or to specify scientific theories. With increasing emphasis on the development of scientific research skills, the work with graphs and data interpretation are gaining in importance. The research involved an eye-tracking experiment conducted to evaluate student work with graphs in physics. Eye-movement data were recorded using the GazePoint eye-tracker. A total of 40 third-year grammar school students participated in the research. These students were allocated into three groups by a physics teacher. These groups were called PLUS, AVERAGE and MINUS. The PLUS group showed excellent results in education and included gifted physics students. The MINUS group was composed of the opposite end of this cognitive spectrum, whose members made the most mistakes in graph reading. The aim of the experiment was to find the differences between students allocated to these three groups and to evaluate whether the allocation based on the teacher's experience, long-term observations and the students' previous achievements was sufficient. The results showed that students from all three groups had problems with reading graphs in physics. According to the eye-movement data, several students who had been incorrectly assigned to groups were identified. Keywords: education in physics, gifted children, graph, eye-tracking, experimental studv.

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# STUDENTS' ABILITY TO WORK WITH GRAPHS IN PHYSICS STUDIES RELATED TO THREE TYPICAL STUDENT GROUPS

# Jana Skrabankova, Stanislav Popelka, Marketa Beitlova

# Introduction

Education at school in the Czech Republic follows a Framework Educational Programme (FEP) (Jeřábek et al., 2016). In the context of this programme, each school, including grammar schools, creates its own School Educational Programmes (SEP), which may include studies in physics. The content of studies in physics is given by the curriculum, while the extent and arrangement of education, to a certain extent, is the teacher's responsibility. Theoretical schoolwork accompanies experiments, and solving examples and tasks is followed by practical exercises. The main aim of studies in physics at secondary school is to present physics to students as an exact science through suitable forms and using appropriate methods to achieve knowledge, understanding, skill and habits for future study and practice. Grammar school education of physics is preceded by primary school education. Students acquire knowledge step by step, usually through observation and simple measurements, and thereby their relationship to the subject begins. A grammar school course of four years, sometimes three, is more difficult than the primary school course, and for some students, it is the final education in physics offered by schools. Grammar schools in the Czech Republic are seen as schools which prepare their graduates for university studies, not entry into practice. Physics taught at Grammar schools includes studies of mechanics (kinematics and dynamics), molecular and thermal physics, electricity and magnetism, optics, oscillation and waves. Students are also introduced to the basics of astronomy and the special theory of relativity. They encounter graphs in all of these disciplines. Graphs "assault" students even in mathematics, chemistry, biology, and other subjects, not only natural sciences.

Science subjects are generally less popular with students. However, this statement is not necessarily always valid. For example, concerning students interested in physics, Pöschl (2007) mentioned that students who perceive physics more as a scientific field have a more positive attitude towards it than those who perceive it simply as a subject.

Coleman and Cross (2005) offered 12 principles for teachers for the basis of their decisions in the classroom. Applying all the principles is a complicated task since the teacher must make many decisions according to situation. Teachers rarely use one principle at a time, and they make more than one



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decision during an active teaching period. A "teaching system" is a much broader concept than a "teaching method", which is a common description in the literature (Coleman & Cross, 2005).

#### Gifted Students

The topic of talented and gifted students is currently important in the Czech Republic. The Ministry of Education, Youth, and Sports of the Czech Republic consider the support and development of gifted students one of its main priorities, especially in the fields of natural sciences and technology. An important official step in supporting talented students was Decree No. 27/2016 Coll. and testifies to the social need of supporting gifted students in the Czech education system (MŠMT, 2019).

Gifted children and students with special educational needs in the Czech Republic are currently addressed in the context of an inclusion process. Populations with special needs, which is the area gifted children fall under, are included in the majority education system while taking into account the educational needs of all children.

In the inclusion process, children meet each other in class, and the teacher determines how to manage the situation. If the exact diagnoses of the children are available, this process is done by psychologists and special educators in a special environment. Teachers may also designate children for diagnosis. Through teacher training, we can infer that allocating a child to a group relies on excellent observation of the child's behaviour and performance and that the main aim is to establish the best possible educational strategies in order to identify and eventually diagnose a child. Diversification of children into groups according to their abilities is always demanding and sensitive.

Identifying gifted children is a challenging and perplexing problem for people interested in promoting the development of high ability (Coleman & Cross, 2005). It is interesting when children are identified; they implicitly have a higher probability of behaving like gifted adults than other children do, although this is an assumption, because the data relating to childhood and adult performance are inconsistent (McClelland et al., 1958). Coleman and Cross (2005) stated that it is easier to make statements about groups than individuals.

The process of identifying gifted individuals is unique (Clark, 1988; Tuttle Jr, 1988). Davis and Rimms (1989) suggested four stages of identification. This distribution is accepted by other authors; for example, Renzulli (1990). Standardized tests are still the most frequently mentioned technique for measuring abilities (Alvino et al., 1981).

#### **Reading Graphs**

Graphs included in common software (e.g. Microsoft Excel) can be used by scientists or politicians and can also express the results of research conducted by companies or the media. The ability to read graphs and understand them should be a basic skill of every person. After all, most primary school and secondary school graduates need this skill for their vocations or further studies, even if their studies were not in natural sciences. In physics, graphs are used as a visual image of the mutual dependencies between physical quantities. Students already encounter graphs in physics at primary schools. At grammar schools, graphs are commonly included in physics studies, and students should not have any problems reading them. Graduates leave secondary schools for university studies, and the ability to read graphs is usually taken for granted. The population in the modern world is awash with data. But as anyone who has ever opened up a spreadsheet filled with seemingly infinite lines of data knows, numbers aren't enough: people need to know how to make those numbers talk (Page, 2018). Each of these areas contains more specific issues that cause problems for students. Glazer's (2011) study states that with the growing emphasis on developing scientific inquiry skills, the display and interpretation of data are becoming increasingly important. In fact, competence in graph interpretation is essential to understanding the today's world and being scientifically literate. However, interpreting graphs is a complex and challenging activity. Competence in interpreting graphs is affected by many factors, including the characteristics of the graph, its content, and the reader's prior knowledge (Glazer, 2011).

The subject of physics has difficult aspects that students struggle with, and reading graphs is indisputably one of them (Leinhardt et al., 1990):

- Students often perceive graphs as pictures or sketches of a given situation, not as abstract mathematical representations.
- Students often do not know whether the required information is acquired from the direction or the slope.
- Students have problems with determining direction (they often count it as a value from a single point).
- Students do not recognize whether an interval or point value is required and tend to interpret from a
  pointwise perspective.

Why is it appropriate to select only graphs used in physics for this research? Reading graphs of functions is more likely encountered in mathematics, but mathematics also serves a numerical apparatus for physics, and no choice exists to work without graphs or without the ability to use them, especially not if teachers want to give students a complete idea of the phenomena and processes described and interpreted in physics. Experiments are an inseparable part of most scientific research, and graphs are very important in their evaluation, because a graph displaying a physical phenomenon, at first glance, enables a trend of development not recognizable in a table of the same values to be seen (Beichner, 1994). According to some external studies published in the past 20 years or so, students of all ages have demonstrated problems in reading and understanding graphs. It is therefore invaluable to discover how Czech students at grammar schools process work with graphs.

The results of some research conducted in the field of mathematics is inspiration. This research has confirmed the hypothesis that using the formal notation characteristics of a programming language for presenting algorithms is often a practical difficulty in the process of solving even simple tasks. The research has also shown that eye-tracking technology can be used to optimize the educational process of learning programming (Andrzejewska et al., 2016).

#### Eye-Tracking in Education

Eye-tracking technology has been used to allocate (not identify) gifted students. According to Shayan et al. (2017), the special contribution of eye-tracking to educational research has been in combining the data of students' physical movements and verbal utterances. There are two basic approaches to using eye-tracking in education and didactics: evaluation of created materials and user evaluation. Jarodzka et al. (2017) presented the theoretical framework and research agenda for this area. Eye-tracking has also been studied by Bolden et al. (2015), Škrabánková and Trnová (2015) and Rosengrant et al. (2009) to examine how students solved problems in physics and mathematics.

Eye-tracking can also be used directly during class time. The first option would be equipping the teacher with eye-tracking glasses and assessing his or her responses to students. An alternative would be watching a video of the lesson. Such a study was conducted by Yamamoto & Imai-Matsumura (2013).

The differences between expert and novice teachers were analysed using the eye-tracking method in a study by Wolff et al. (2017).

Eye-tracking has also been previously used in a study with gifted children. Eye-tracking glasses PupilLabs were used in a study to examine creativity in mathematics (Schindler et al., 2016). Mathematical stimuli were also used in a study (Sajka & Rosiek, 2015) comparing the differences between the problem-solving processes of mathematically gifted students and underperforming students. In a study (Choi et al., 2012), eye-movement patterns were analysed to find the differences between average and gifted students. An overview of eye-tracking in education was presented in the book by Was et al. (2016).

#### Eye-Tracking and Graphs

Shah and Hoeffner (2002) stated that graphs are commonly used to represent mathematical functions, show data from social and natural sciences, and specify scientific theories in textbooks and other print media in and out of the classroom.

With the growing emphasis on the development of scientific inquiry skills, work with graphs and the interpretation of data is becoming increasingly important (Glazer, 2011). Graphs are important for understanding scientific data (Shah & Hoeffner, 2002).

Graph interpretation is a fundamental skill that is essential for all students in their everyday lives. According to Glazer (2011), little research in graph interpretation in science (as opposed to mathematics) has been conducted. This statement is consistent with Shah and Hoeffner (2002), who affirmed that graphs are important in understanding scientific data.

Strobel et al. (2016) mentioned that elementary graph reading skills can be observed as early as preschool and middle school (Curcio, 1987) and that these skills develop over time (Lowrie & Diezmann, 2007). Graph literacy, i.e. the ability to understand graphically presented information, may be measured, for example, in the scale developed by Galesic and Garcia-Retamero (2011). However, relatively little information exists about how people extract information from graphs and how graphical design defines or 'nudges' and biases decision making (Vila & Gomez, 2016).

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Previous decades saw the development of many taxonomies comprising highly similar concepts (for example, Bertin (1983); Curcio (1987); Tan and Benbasat (1990) or Wainer (1992)).

Eye-tracking has already been used in several studies concerning graphs. Goldberg and Helfman (2011) introduced the potential of eye-tracking in a study comparing radial and linear graphs. The results showed that linear graphs could better support the initial, dimension-finding stage than radial graphs. A similar comparison of linear and radial graphs (marked as polyline and star glyphs) was conducted in another eye-tracking study by Opach et al. (2017). The results showed that each type of graph was suitable for different types of tasks.

Atkins and McNeal (2018) conducted an eye-tracking study exploring graphs in the context of climate change. Van der Linden et al. (2014) stated that graphs are the most effective way of communicating the climate consensus of researchers. Fifty-eight graduate and undergraduate students were involved in the study, which presented four open-ended tasks testing fact extraction and data interpolation. The results showed that the time spent on different graph features varied between the graduate and undergraduate student groups.

Extracting business information from graphs was examined in a study by Vila and Gomez (2016), who applied the methodology of experimental economics. The authors compared graphs which had numerical information to graphs which had none. The results showed that the inclusion of values appeared to have no impact on the accuracy of the answers, though increased the time required to extract the information from the graph.

Kim et al. (2014) and Kim and Wiseheart (2017) analysed graph reading by dyslexic and non-dyslexic users. Moreno-Esteva et al. (2017) presented a mathematical and computational analysis, partially based on eye-tracking.

The research was focused on the analysis of the use of graphs in physics. Students' comprehension of graphs has been researched in many studies of education in physics. The paper by Susac et al. (2018) contained a comprehensive review of over 30 studies which examined the use of kinematics graphs to explore student graphing abilities. Few of these studies, however, involved eye-tracking.

Susac et al. (2018) compared physics and psychology students' comprehension of graphs. The tasks involved interpreting graph slope and comprehending the area beneath it. The results indicated that area under a graph is a difficult concept and that more attention should be given to it in physics classes. Tai et al. (2006) used eye-tracking to identify problem-solving behaviours in a group of individuals with different levels of expertise in biology, chemistry, and physics.

Kozhevnikov et al. (2007) presented three studies on the relationship between spatial ability and kinematics problem solving. The third study employed eye-tracking analysis, and the authors examined whether students made eye-movements in the correct direction. To test spatial ability, Paper Folding, Form Board, Cube Comparison, and Card Rotation tasks were conducted. The authors argued that spatial ability might be important for visualizing invisible phenomena and processes such as electric or magnetic field lines or electric current.

Madsen et al. (2012) analysed how visual attention differed between those who either correctly or incorrectly answered introductory physics problems. The authors found that top-down processes played an important role in guiding visual attention. Top-down processes are based on the viewer's previous knowledge, task goals, and expectations. Viiri et al. (2017) had a similar aim and explored the differences between students who responded correctly and those who responded incorrectly. Heat maps showed that the students who responded incorrectly more frequently viewed the irrelevant parts of a task. Kekule (2014) performed a similar study dealing with kinematics graphs.

Goldberg and Helfman (2011) described three steps needed to interpret and understand graphs: (1) examining values, (2) comparing values, and (3) appreciating higher level patterns, such as trends and distributions. Bertin (1983) identified three major components of graph reading. The first component involves viewers encoding the visual array and identifying the important visual features. In the second component, viewers relate the graph's visual features to the conceptual relationships represented by those features. The third component is the process of comprehending a graph, in which viewers determine the referent of the quantified concepts and associate those referents to encoded functions (Shah & Hoeffner, 2002). Shah and Hoeffner (2002) highlighted that these three processes imply that three factors play an important role in determining a viewer's interpretation of data: the characteristics of the visual display (bar or line graph), knowledge of graphs (graph schemas), and content (e.g., age vs height, time vs distance).

The present research involved tasks to identify graphs which described certain physical phenomena. The character of the tasks ensured that the third factor would be crucial: participants had to recognize the content, i.e. the physical phenomena, and identify it in the graphs.



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#### **Research Aims**

The aim of the research was to understand how students read graphs and analyse the differences of graph reading according to respondent's groups.

Selecting the research group was consulted with an experienced physics teacher, who was a key person in the experiment. The teacher allocated students into three groups according to cognitive performance. The groups were designated PLUS, AVERAGE and MINUS. The teacher allocated students to these three groups based on experience with the students, long-term observations and the students' previous achievements. The PLUS group showed excellent results in education and was expected to include generally talented students in physics and natural sciences. This means that members of this group should not have had any problems reading graphs. The MINUS group formed the opposite end of this cognitive spectrum, and its members were expected to make the most mistakes in reading graphs. The AVERAGE group separated both extreme groups and should have contained participants with average results.

After allocating the students, the research examined two basic, complementary levels which crossed over in the results. In the first level, the aim was to understand how students from individual groups proceeded when they read graphs and how they were able to solve related tasks displayed on a screen. The aim of the second level was to detect the hidden potential of students present in the research sample, regardless of their particular group. According to Betts and Neihart (1988), such individuals might be expected in groups of students/participants. These designated "underground talent" students (even young students found at primary schools) could not be detected by the teacher from their educational behaviour, which may be intentionally downplayed (Neihart, 2011). Therefore, it is important to study the results of their work examined in this research.

Three research questions were posed:

- 1. Is the statement that students read graphs with difficulty valid?
- 2. Can similar segments be found in the acquired data which shows clusters of similar attitudes between participant groups in solving the given tasks?
- 3. Can students who were incorrectly allocated to a group by the teacher be revealed through the acquired data?

An eye-tracking experiment was created to explore these research questions. The experiment's aim was to highlight the diversity in students' cognitive abilities in physics. Graphs demonstrating mechanics (kinematics), oscillation and waves, and molecular physics phenomena were used as source images. These graphs were selected for their explanatory character.

The PLUS group of participants was selected to formulate the hypotheses. This group represented students with the highest potential for learning in physics:

- H<sub>1</sub>: Group PLUS needs the least amount of time to solve the given tasks.
- H<sub>2</sub>: Group PLUS makes fewer mistakes in task solving.
- H<sub>a</sub>: The correctness of answers is proportional to the number of fixations in an AOI (Area of Interest).
- H<sub>4</sub>: Students who were mistakenly not assigned to the PLUS group can be found by analysing the acquired data.
- H<sub>c</sub>: The teacher's allocation to groups based on cognitive abilities is not always correct.

#### **Research Methodology**

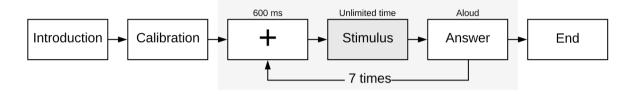
#### Experiment Design

The eye-tracking experiment was conducted at *Gymnázium Nový Jičín* in two sessions at the beginning of 2019 (January 29 and January 31). Three eye-trackers were placed in the classrooms, and the participants came one at a time to the testing venue. Trained technicians introduced the principle of the eye-tracker and explained the organization of the experiment. After calibration, a fixation cross appeared for 600 ms to unify the starting position of eye-movement trajectories. A stimulus was then displayed for an indefinite time. The task required an answer to the question in the upper part of the stimuli. The participants had to select one of the graphs and announce

the answer aloud. The answer was marked into a pre-prepared list by a technician. If a participant responded that they did not know the answer, an "X" was marked into the list instead of the answer. The scheme of the procedure is displayed in Figure 1.

# Figure 1

Scheme of the procedure



### Equipment

A GazePoint 3 eye-tracker with a recording frequency of 60 Hz was used to collect data in this experiment. The eye-tracker was connected to a notebook and placed under a monitor with a resolution of 1280 x 1024 pixels. The device was an inexpensive eye-tracker similar to TheEyeTribe tracker or Tobii EyeX. The accuracy and precision of these devices have been tested in studies by Dalmaijer (2014), Popelka et al. (2016), and Ooms et al. (2015). The results of these studies showed that this kind of device can be applied to scientific use. The GazePoint eyetracker was evaluated only in a study by Janthanasub and Meesad (2015), however it achieved similar results to the TheEyeTribe and DIY eye-trackers.

### Stimuli and Tasks

Basic secondary school physics graphs generally encountered by students during their studies were displayed for reading. The graphs showed principles in mechanics (kinematics), oscillations and waves, and molecular physics. These areas covered secondary school physics over three years of study (mechanics/kinematics – 1st year, molecular and thermal physics – 2<sup>nd</sup> year, oscillations and waves – 3<sup>rd</sup> year). Under the teacher's guidance, students can discover their own as well as recommended strategies for reading graphs and learn to appreciate the clarity and the content of information presented in graphs. During their studies, students encounter many types of these graphs, which represent basic graphical interpretations of the physical processes and phenomena and knowledge of physical areas they study. It is clear that physics teachers work with these graphs in education and students should know them. Moreover, understanding the principles of reading graphs is not based on memorization but comprehension. It is not relevant to refer to distant learning or short-term memory. If comprehension of graph principles exists, the prerequisite of some ability independent of time also exists.

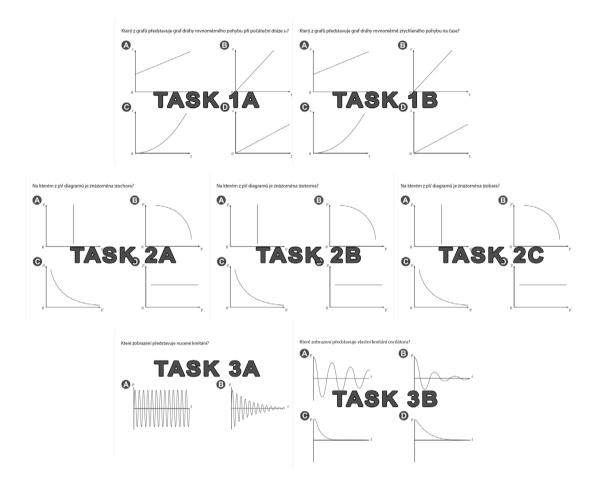
Stimuli were presented in a fixed order. The tasks formed a part of the stimuli, and their English translation is given below. The overview of all tasks and stimuli is displayed in Figure 2.

- 1A/ Which of the graphs represents lines of uniform motion at initial track s<sub>o</sub>?
- 1B/ Which of the graphs represents a track dependent on uniformly accelerated motion in time?
- 2A/Which of the pV diagrams has an isochore?
- 2B/Which of the pV diagrams has an isotherm?
- 2C/Which of the pV diagrams has an isobar?
- 3A/Which image represents forced oscillation?
- 3B/ Which image represents free oscillation of the oscillator?

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### Figure 2

Stimuli used in the experiment



#### Participants

The research was conducted on a sample of 52 high school (*Gymnázium Nový Jičín*) students from the third grade. The students were 16 years old and formed a basic research group. From this primary group, 12 students were removed due to technical problems with the eye-tracker or insufficient calibration results. The experiment was therefore conducted on 40 participants (9 males and 31 females).

The participants were allocated into three groups, PLUS, AVERAGE, and MINUS, according to the opinion of their physics teacher. The results of students' previous studies were used in combination with the teacher's recommendations as a "distribution parameter". Professional diagnostics is more complicated, and not all students are approved in this manner. Few students are ever identified, mainly because of improper allocation and a certain unwillingness to participate in diagnostics.

The teacher allocated students to these three groups based on experience with the students, long-term observations and the students' previous achievements. The PLUS group showed excellent results in education and was expected to include generally talented students in physics and natural sciences. This means that members of this group should not have had any problems reading graphs. The MINUS group formed the opposite end of this cognitive spectrum, and its members were expected to make the most mistakes reading graphs. The AVERAGE group separated both extreme groups and should have contained students with average results.

The PLUS group contained 11 participants. The AVERAGE group was the largest, with a total of 24 participants. The remaining five participants were weak in physics and allocated to the MINUS group. The participants were designated P01–P40.

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### Data Pre-Processing

The data recorded by the eye-tracker required validation before it could be analysed. The recording was conducted in the classroom, and students had only one previous experience with eye-tracking testing. Some of them, therefore, may have been nervous, which may affect the quality of recorded data.

In the first step of data pre-processing, recorded data were exported from the GazePoint Analysis environment into the open-source application OGAMA (Voßkühler et al., 2008) providing more advanced functionality. In OGAMA, the fixation detection algorithm (I-DT) thresholds were set to 20 pixels (distance between points) and 5 (minimum number of samples). The optimal fixation detection algorithm has been described by (Popelka, 2014) in more detail. In the next step, the eye-movement trajectories of all participants were checked visually, and problematic examples were removed from the dataset. Data loss information and off-screen samples were then exported from OGAMA. The value of data loss represents the ratio of samples with coordinates 0;0 (upper-left corner of the stimulus). The second value shows how many samples were recorded with coordinates off the screen. Both values were summarized, and participants with a sum (data loss + off-screen) greater than 15% were removed from the experiment. As mentioned above, the experiment comprised a total of 40 participants with valid data.

#### Methods of Analysis

Several methods of eye-tracking data analyses were applied in the research. Data were statistically analysed in RStudio using the Kruskal–Wallis post hoc Nemenyi test, which is a non-parametric variant of ANOVA. Statistically significant differences (p < .05) were indicated in the boxplots. The Trial Duration metric was selected for the analysis. A longer time required to solve a task indicated a task with greater complexity.

Data were visualized using sequence charts, which represented participants' eye-movement data with coloured bars. The colour of each cell in a bar represented one fixation in a particular Area of Interest (AOI). The sequence chart, therefore, showed the order of visited AOIs, how much time participants spent looking at them, and whether they repeatedly looked at certain AOIs.

Since neither OGAMA nor GazePoint Analysis permits visualizations with sequence charts, the charts were created manually in MS Excel using the PART and conditional formatting functions. Fixations in the indicated AOIs were represented with coloured rectangles.

The final analytical method was a scanpath comparison using the ScanGraph tool. This tool was developed to identify differences in the stimulus reading strategies of different groups of participants (Dolezalova & Popelka, 2016; Popelka et al., 2018). ScanGraph read the order of visited AOIs (the same used to visualize the sequence charts) and calculated the similarity of these strings by employing three different algorithms: Levenshtein distance, the Needleman–Wunsch algorithm and Damerau–Levenshtein distance. Individual participants were visualized as nodes on a graph, and ScanGraph searched for cliques in this graph, i.e. groups of participants who were similar to each other at least to a certain degree. The tool can be used to determine whether the stimulus was read differently, for example, by men or women or by experts or novices.

#### **Research Results**

#### Accuracy of Answers

The first step in the data analysis examined the accuracy of answers. Participants responded aloud, and their answers were recorded into a form by technicians. The data and correct answers are summarized in Table 1. The table shows that the majority of answers were incorrect. Incorrect answers are indicated in the figure in grey. Only 39% (110 out of 280) of the answers were correct. It could be assumed that the easiest tasks were tasks 3A and 3B. However, the higher density of correct answers was a result of participants only selecting between two options in task 3A, while the other tasks had four options (A, B, C and D). In task 3B, both options were correct (A and B).

# Table 1

Correct answers in the experiment

ID	Sex	Group	1A	1B	2A	2B	2C	3A	3B	Correct	Incorrect				
P05	F	Minus	В	В	С	D	С	В	В	1	6				
P16	F	Minus	В	С	В	С	D	А	В	5	2				
P20	F	Minus	В	В	А	D	В	А	А	3	4				
P35	F	Minus	В	В	В	С	А	В	А	2	5				
P40	F	Minus	В	D	С	С	С	А	А	3	4				
P01	F	Average	D	D	С	С	А	А	А	3	4				
P03	F	Average	В	А	С	В	D	В	А	2	5				
P04	М	Average	D	С	С	D	D	А	В	4	3				
P06	F	Average	В	D	В	С	С	А	В	3	4				
P07	F	Average	D	В	А	D	В	В	А	2	5				
P09	F	Average	В	В	С	С	А	А	В	3	4				
P10	F	Average	В	В	D	С	В	А	В	3	4				
P11	F	Average	D	В	С	В	А	А	В	2	5				
P15	F	Average	D	С	В	С	D	А	А	5	2				
P18	F	Average	В	D	В	С	А	А	Х	2	5				
P19	F	Average	D	С	D	А	D	А	В	4	3				
P21	М	Average	D	С	А	D	А	В	В	3	4				
P23	F	Average	В	D	А	D	В	А	В	3	4				
P25	F	Average	D	В	В	С	D	А	В	4	3				
P26	F	Average	В	С	С	D	В	А	В	3	4				
P29	М	Average	D	С	А	D	В	В	А	3	4				
P30	F	Average	В	В	С	В	D	А	А	3	4				
P31	F	Average	D	В	A	D	С	А	А	3	4				
P32	F	Average	В	D	А	С	D	В	А	4	3				
P33	F	Average	D	A	В	A	D	В	В	2	5				
P34	F	Average	D	C	В	A	D	В	A	3	4				
P36	F	Average	D	D	D	A	С	A	A	2	5				
P37	F	Average	В	В	C	C	В	A	A	3	4				
P38	M	Average	В	A	X	X	X	A	В	2	5				
P02	F	Plus	D	D	C	C	C	В	A	2	5				
P08	F	Plus	D	В	D	D	A	A	A	2	5				
P12	F	Plus	D	В	D	A	В	A	В	2	5				
P13	M	Plus	A	C	A	D	A	В	В	4	3				
P14	M	Plus	В	c	X	A	D	В	X	2	5				
P17	M	Plus	В	A	A	D	D	В	В	3	4				
P22	F	Plus	В	C	В	A	D	A	C	3	4				
P24	M	Plus	B	A	A	В	X	В	D	1	6				
P24 P27	F	Plus	B	D	D	A	В	A	B	2	5				
P28	F	Plus	B	C	B	D	A	A	B	2 3	5 4				
P28 P39	F M	Plus Plus	B	A	В	D	A C	B	A	3 1	4 6				
F 99	IVI		В1	12	В 10	13	13	В 25	A 36	I	0				
		Correct	39	28	30	27	27	25 15	4						

306

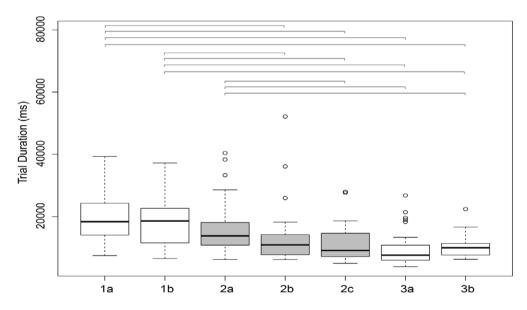
The best results were obtained by the AVERAGE group, with an accuracy of 42.3%. Surprisingly, the PLUS group obtained the worst results, with an accuracy of only 32.5%. It should be noted that the data may have been affected by participants P24 and P39, who solved only one task correctly. The accuracy of the MINUS group was 40%. This group contained only five participants, which may also have affected the results. This group also contained a participant (P05), who solved only one task correctly. Data were statistically analysed, but no statistically significant differences between the groups were found.

# Stimuli as a Whole

At the beginning of the statistical analysis, data recorded for all stimuli were analysed as a whole. In the first step, the differences between the groups were not analysed. The values for Trial Duration for all stimuli are given in Figure 3. Lines in the upper part of the boxplot represent pairs where statistically significant differences were found using the Kruskal–Wallis post hoc Nemenyi test. The boxplot shows that the majority of statistically significant differences were found only in the case of pairs 2A–2C, while a higher Trial Duration value (longer time) was observed in the first task. This is logical, because the participants had to familiarize themselves with the task at the beginning (A), and their work was then faster, as the tasks in each group were similar (B and C). Task 3 indicated the contrary, as solving task 3B took more time than solving 3A. Though in this case, it was because task 3B contained four options and task 3A only two.

# Figure 3

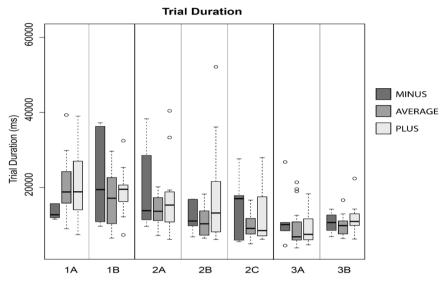
Trial Duration for all tasks. Statistically significant differences are indicated with lines in the upper section



The eye-tracking metrics of the Fixation Count and Scanpath Length had a similar distribution of values to Trial Duration. The Trial Duration values for all three groups are shown in Figure 4. The time required to solve the task varied between the groups. The hypothesis that the PLUS group would need less time to solve the task than the MINUS group was only corroborated in tasks 2C and 3A. Task 1A demonstrated the contrary, i.e. that the MINUS group needed the least amount of time of all three groups. The results were not statistically significant.

# Figure 4

Trial Duration for all three participants groups in all tasks

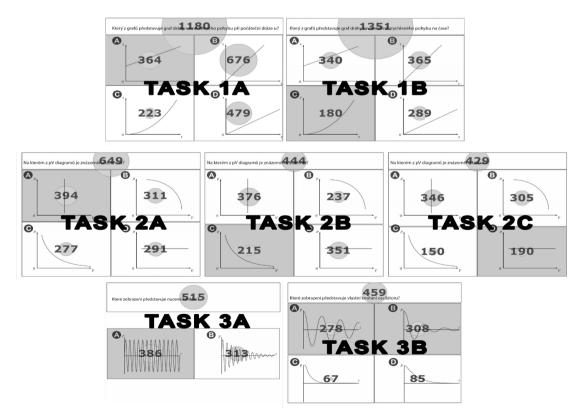


Areas of Interest

In the next step, Areas of Interest (AOIs) were marked in the stimuli on each task and graph. The distribution of AOIs is illustrated in Figure 5. The circles with numbers show the number of fixations recorded at each AOI. Grey rectangles indicate correct answers.

#### Figure 5

Distribution of fixations in AOIs





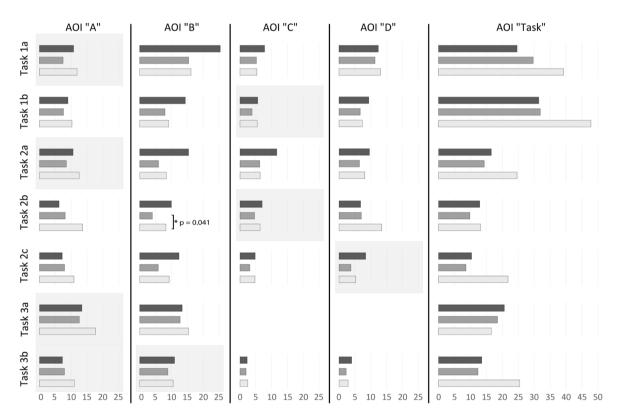
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In many cases, the AOI with a low number of or even the fewest recorded fixations corresponded to the correct answer. Examples are task 1B and 2B. These two tasks recorded the fewest fixations in AOI "C", which was the correct answer in both cases. In task 3B, two options were correct (A and B); and both of these were fixated on extensively. Other answers were fixated on only marginally.

In the next step, the data were explored with respect to differences between groups. The Fixation Count for each AOI and group was calculated. The averages of these values are given in Figure 6. The PLUS group demonstrated the most fixations while reading in almost all tasks (except for task 3B). The difference was not statistically significant, but in task 2A, the difference between the MINUS and AVERAGE groups indicated a significance of p = .086. The only significant difference in the entire dataset was found in task 2B and AOI "B". In this task, the PLUS group demonstrated significantly more fixations.

# Figure 6

Average number of fixations for each AOI, task, and group of participants

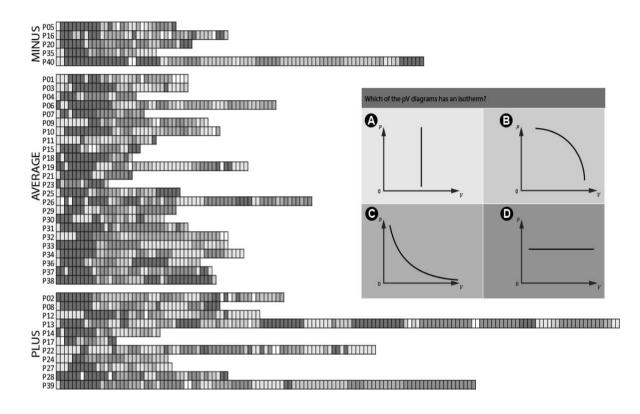


In the next step, the distribution of fixations at particular AOIs in time was visualized. For this type of analysis, a sequence chart was created. Task 2B was selected as an example (Figure 7). This type of data visualization shows how often participants visited each AOI and how much time they spent there. Participants who read the task several times (P13, P16) or ended their eye-movement trajectory in an AOI task (P38, P40) could also be identified.



#### Figure 7

Sequence chart for task 2B



Verifying Allocation to Groups

The ScanGraph tool was used for the next step of data analysis. The tool typically displays groups of participants as a graph, though for the present study, the tool was used in a different manner. One of its options allows the similarities between participants to be exported as a CSV file. Each group was calculated separately for the average similarity between members of the group. The participants with the lowest value of similarity indicated the greatest difference. These results revealed five potential candidates (indicated in grey in Figure 8) who were not assigned correctly to groups. It would be appropriate to focus on these students and learn whether they genuinely belonged to their allocated group. The average similarity of these students to the remaining participants was the least. Similarity with other participants is indicated with circular symbols in Figure 8, these students being P16 from the MINUS group, P11 and P30 from the AVERAGE group, and P13 and P22 from the PLUS group.



Figure 8

Similarity in the groups of participants

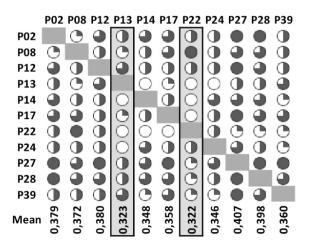
	P05	P16	P20	P35	P40
P05		0			$\bullet$
P16	Ο			Ο	$\bullet$
P20					
P35		$\odot$			
P40	$\mathbf{O}$	$\bullet$		$\bullet$	
Mean	0,330	0,283	0,377	0,348	0,340

	P01	P03	P04	P06	P07	P09	P10	P11	P15	P18	P19	P21	P23	P25	P26	P29	P30	P31	P32	P33	P34	P36	P37	P38
P01					$\bullet$		$\bullet$	0	$\bullet$			$\bullet$	•	•	$\bullet$	$\odot$	$\bullet$	•	$\bullet$	•	$\bullet$	$\bullet$	$\bullet$	•
P03	•		•		$\bullet$	$\bullet$	$\bullet$	$\odot$	$\mathbf{O}$	•	•	$\bullet$	$\bullet$	•	$\bullet$	$\bigcirc$	$\odot$	•	$\bullet$		•	•	$\bullet$	•
P04	•				$\bullet$		$\bullet$	$\bigcirc$	$\mathbf{O}$			$\bullet$	•	$\bullet$	$\bullet$	$\odot$	$\odot$		$\mathbf{O}$	•	$\bullet$		$\bullet$	•
P06	•	•			$\bullet$	$\bullet$	$\bullet$	$\odot$	$\bullet$		•	$\bullet$	•	•	•	$\odot$	$\odot$	•	•	•	•			•
P07	$\bullet$	$\bullet$		$\bullet$		O	$\bullet$	$\bigcirc$	$\bullet$	$\bullet$	$\mathbf{O}$	•	$\bullet$	$\bullet$	$\bullet$	$\bullet$	$\bigcirc$	•	$\bullet$	$\bullet$	•	$\bullet$	$\bullet$	$\bullet$
P09		$\bullet$		$\mathbf{O}$	0		$\mathbf{O}$	$\odot$	$\bullet$	$\bullet$	$\mathbf{O}$	0	$\bullet$	$\bullet$	$\bullet$	$\odot$	$\bullet$	•	$\bullet$	$\bullet$	$\mathbf{O}$	$\bullet$	$\bullet$	0
P10	$\bullet$	•	$\bullet$	$\bullet$	$\bullet$	$\bullet$		$\bullet$		$\bullet$	•	Ο	$\odot$	$\bullet$	$\bullet$			•	O	$\bullet$	$\bullet$	O	$\bullet$	$\bullet$
P11	O	$\odot$	$\bigcirc$	$\odot$	$\bigcirc$	O	•		•	O	$\odot$	$\bigcirc$	$\bigcirc$	$\odot$	$\odot$	$\bullet$		$\odot$	$\odot$	$\bigcirc$	$\odot$	0	0	0
P15	$\bullet$	$\bullet$	$\bullet$	$\bullet$	$\mathbf{O}$	$\bullet$		•		$\mathbf{O}$	•	$\mathbf{O}$	$\bullet$	•	$\bullet$			•	O	$\bullet$	•	$\bullet$	$\bullet$	$\bullet$
P18	•	•	$\bullet$		$\bullet$	$\bullet$	$\bullet$	$\odot$	$\bullet$			$\bullet$	•	•	•	$\odot$	$\odot$		$\bullet$	•	$\bullet$	$\bullet$		$\bullet$
P19	•	•	•	•	$\bullet$	$\bullet$	$\bullet$	$\odot$	•				•		•	$\bullet$	$\odot$		$\bullet$					
P21	$\bullet$	$\bullet$	$\bullet$	$\bullet$		O	$\odot$	$\bigcirc$	$\bullet$	$\mathbf{O}$	•		$\odot$	•	$\bullet$	$\bullet$	$\bigcirc$		$\odot$	•		$\bullet$	$\bullet$	•
P23	•	$\bullet$	•		$\bullet$	$\bullet$	$\odot$	$\bigcirc$	$\bullet$			0		$\mathbf{O}$	$\bullet$	$\bigcirc$	$\odot$		$\bullet$	$\bullet$	$\bullet$	$\bullet$	$\bullet$	•
P25	•	•	$\bullet$		$\bullet$	$\bullet$	$\bullet$	$\odot$	•	•		•	0		$\bullet$	$\odot$	$\odot$		$\bullet$	•	•			•
P26	$\bullet$	$\bullet$	$\bullet$	•	$\bullet$	$\bullet$	$\bullet$	Ο	$\bullet$	•	•	$\mathbf{O}$	$\bullet$	$\bullet$		$\bullet$	$\bigcirc$	•	$\bullet$	$\bullet$	$\bullet$	O	$\bullet$	•
P29	O	$\bigcirc$	$\odot$	$\odot$	$\bullet$	O		$\bullet$		O	$\bullet$	$\bullet$	$\bigcirc$	$\odot$	$\bullet$		$\bullet$	$\odot$	$\odot$	$\odot$	$\bullet$	O	$\bullet$	0
P30	$\bullet$	$\odot$	$\odot$	$\odot$	$\bigcirc$	$\bullet$	$\bullet$		•	O	$\odot$	$\bigcirc$	$\odot$	$\odot$	$\bigcirc$	$\bullet$		$\odot$	$\bigcirc$	$\odot$	$\odot$	O	$\bigcirc$	0
P31	•	•	•	•	•	•	$\bullet$	Ο	•			•	•		$\bullet$	$\odot$	$\odot$		$\bullet$	•		$\mathbf{O}$		•
P32	$\bullet$	$\bullet$	$\bullet$		$\bullet$	$\bullet$	O	Ο	Ο	$\bullet$	$\bullet$	O	$\bullet$	$\bullet$	$\bullet$	$\odot$	$\bigcirc$	$\bullet$		$\bullet$		$\bullet$	$\bullet$	0
P33	•			•	$\bullet$	$\bullet$	$\bullet$	$\bigcirc$	$\bullet$	•		•	$\bullet$	•	$\bullet$	$\odot$	$\odot$	•	$\bullet$		•	•	$\bullet$	
P34	$\bullet$	•		•		$\bullet$	$\bullet$	$\odot$	•	$\mathbf{O}$		•	$\bullet$	•	$\bullet$	$\bullet$	$\odot$		•			•		
P36	$\bullet$	•	•	•	$\bullet$	$\bullet$	O	$\bigcirc$	$\bullet$	$\bullet$	•	$\mathbf{O}$	$\bullet$	•	O	Ο	$\odot$	$\mathbf{O}$	$\bullet$	•	$\bullet$			•
P37	$\bullet$	$\bullet$	$\bullet$	•	$\mathbf{O}$	$\bullet$	$\bullet$	$\bigcirc$	$\bullet$	•	•	$\mathbf{O}$	$\bullet$		$\bullet$	$\bullet$	$\bigcirc$	•	$\bullet$	$\bullet$	•			
P38	•	•	•	•	$\mathbf{O}$	O	$\mathbf{O}$	Ο	$\mathbf{O}$	$\mathbf{O}$		•	•	•	•	$\odot$	$\bigcirc$	•	O		<b>0</b>	•	$\mathbf{O}$	
Mean	0,414	0,413	0,411	0,416	0,388	0,384	0,398	0,323	0,411	0,420	0,447	0,383	0,385	0,428	0,380	0,352	0,338	0,433	0,373	0,417	0,412	0,385	0,396	0,402

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The next step in the eye-movement data analysis incorporated the data of each of these five participants. Students P11 and P30 from the AVERAGE group showed the least values of similarity with others in this group. Figure 7 indicates that participant P11 (female), especially, used a completely different sequence of visited AOIs in task 2B. This participant almost completely omitted the task's text and concentrated directly on the graphs. The data suggest that the students were allocated to the AVERAGE group in the correct manner, but they probably cannot sufficiently read graphs. However, the other question of the relationship between knowledge and its use in reading graphs then arises. It would also be worth determining whether transferring student P11 to the MINUS group would be more appropriate.

Participant P22 (female) was allocated to the PLUS group. Her results (3 correct and 4 incorrect answers) corresponded more to the AVERAGE group (Table 1). The results from ScanGraph (Figure 8) could have been affected by no AOI visit being recorded for this participant in task 3B. Participant P22's inclusion in the PLUS group, therefore, should be reviewed.

Participant P13 (male) was allocated to the PLUS group. He had the best overall result in the PLUS group, achieving four correct answers and three incorrect answers (Table 1). This participant also demonstrated in task 2B (Figure 7) one of the greatest numbers of fixations observed in all the stimuli of the experiment.

A different conclusion applies to participant P16 (female), who was allocated to the MINUS group but obtained the best results of all the participants. After the eye-movement data analysis, the teacher who allocated students into the groups was shown the results. The teacher stated that the girl suffered from partial deafness, which may have led to her being allocated to the MINUS group. Because the tasks were presented on a screen, she was not limited by her medical condition during the experiment and achieved one of the best results.

- Hypothesis 1: This hypothesis was not proved, because task 1A demonstrated the exact opposite, i.e. the MINUS group needed the least amount of time of all three groups (although the results were not statistically significant). The MINUS group also demonstrated a time comparable to the other groups in tasks 2A, 2B, and 3B (Figure 4).
- Hypothesis 2: This hypothesis was not proved. The PLUS group achieved the worst results, their accuracy being only 32.5%.
- Hypothesis 3: This hypothesis was not proved. Tasks 1B and 2B showed the least number of fixations
  recorded in AOI "C", which was the correct answer in both cases. In task 3B, both options were correct
  (A and B), and students fixated on them extensively. Students fixated on other answers only minimally
  (Figure 6).
- Hypothesis 4: This hypothesis was proved. The results from ScanGraph indicated certain individuals who behaved differently to the remainder of their group. These were students P11, P13, P16, P22, and P30.
- Hypothesis 5: This hypothesis was proved, shown in the results in Table 1. In the MINUS group, participant P16 demonstrated results that were appropriate to the level of the PLUS group. In the PLUS group, participant P13 demonstrated results that were appropriate to the AVERAGE group.

Comparing hypotheses H1 and H3 and research questions No. 2 and 3 provides enough information to reveal similar segments in the obtained data. Clusters showing similar attitudes between the groups of participants in solving the given tasks can be observed. The notion that the time required by the participants of a given group to solve certain tasks depends on their specific group category is not valid.

It is also not valid to conclude that the correctness of answers increased as the number of fixations in AOIs increased (Figure 6). From the point of view of didactics, this result is very interesting, because there were fewer fixations for correct answers than incorrect answers (Figures 5 and 6). This was probably due to two factors, one being the specific type of graph involved. Few fixations were recorded for graphs which teachers would use more frequently than others to teach the topic. The fewest fixations in AOIs with correct answers were observed with graphs for mechanics (kinematics) and molecular and thermal physics, which are taught in the first and second grades (tasks 1C and 2B). In higher grades, other subjects may interest students more. The interest in physics may also therefore decline, and students may exhibit less concrete knowledge and be unable to make decisions quickly and correctly.



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#### Discussion

Similar research has been conducted previously. Some studies analyse the use of graphs in physics. McDermott et al. (1987), for example, analysed student's difficulties in connecting graphs with concepts in physics. Some studies have combined this type of analysis with eye-tracking technology. Kekule (2014), for example, analysed students' strategies in examining kinematics graphs. Strobel et al. (2018) used eye-tracking methods for task-irrelevant data to impair the processing of graph reading tasks. Many other authors have investigated graph reading in fields other than physics. Wainer (1992) studied the comprehension of graphs and tables in the field of geography. Vila and Gomez (2016) extracted business information from graphs, etc. However, to the best of our knowledge, no previous eye-tracking research has been conducted with participants allocated to groups according to their abilities. The teacher in the present experiment allocated students into three groups: PLUS, AVERAGE and MINUS.

The results of the eye-tracking experiment demonstrated that this type of division may be problematic. A comparison of hypotheses H2, H4, and H5 and research question No. 3 indicates that the teacher could not appropriately allocate students into groups according to their cognitive abilities. The finding then leads to the recommendation that the information available to teachers about the characteristics displayed by students in certain groups, particularly gifted students, should be improved. The myth that the hardworking and "learned" student is gifted is still perpetuated by teachers, which is certainly disproven in theory and practice. Comparing the connection between hypothesis H5 and research question No. 1 suggests the possibility of recovering students who are incorrectly allocated to a group. Hypothesis H5 and research question No. 1 correlate. For example, participants P24 and P39 (Table 1) in the PLUS group supplied one correct answer and six incorrect answers. These results indicate that the teacher's knowledge for allocating gifted students appropriately may have been insufficient.

During the data analysis, the students demonstrated some interesting behaviour, for which we attempted to find an explanation. The first issue concerned students from the PLUS group spending more time at AOI"B" than the AVERAGE group. This can be seen in the sequence chart in Figure 7. One possible explanation is that this may have been caused by the shape of the curve itself, which could have been appealing to participants in the PLUS group and encouraged thinking about variations in the represented process, which is often typical in gifted individuals.

During the analysis of the recorded data, five participants who were inappropriately assigned to their group were identified. Participant P13 performed the most fixations in all AOIs, as he continuously sought correct answers. This behaviour might imply the effort, care (perhaps pedantic) and responsibility of the student to obtain the correct result. This behaviour could have led the teacher to allocating him to the PLUS group.

By contrast, participant P16, who was allocated to the MINUS group, had the best results of all participants. This student is partially deaf, which may adversely affect her abilities during class and may have led the teacher to allocating her to the MINUS group. During the eye-tracking experiment, however, she did not need to use hearing at all, and she obtained very good results. Another explanation is that she may be a gifted student and belong—according to (Betts & Neihart, 1988) typology—to the group of "underground gifted." Given that this student was female, it is a plausible explanation.

The research studied graph reading in physics. The research offers a comparison of real procedures in reading graphs by individual students. In cooperation with a physics teacher, the graph reading strategies of students allocated to PLUS, AVERAGE and MINUS groups were mapped.

#### Conclusions

The research explored the strategies of students as they solved physics tasks with graphs. The research was conducted on a final sample of 40 grammar school students, who were allocated by their teacher into three groups (PLUS, AVERAGE and MINUS) according to the teacher's observations and the students' previous study results in physics.

The results of the eye-tracking research confirmed that the teacher did not always allocate students correctly into the groups according to their cognitive abilities. In this context, the results also revealed that success in reading graphs in physics is not fundamentally related to allocating students to particular groups. Furthermore, the experiment exposed that the allocation of students into the PLUS group was not related to the time students needed to complete the tasks. Analogically, the experiment revealed that the number of errors made by students from the PLUS group did not relate to their allocation to that group.

The research proved that the results of eye-tracking analysis highlighted the students that were not assigned to an appropriate group by the teacher.

The recommendations based on the research follow two directions. The research confirmed that students could not rely on their ability to work with graphs, which implies that teachers should practice these skills more with students during lessons and employ more graph reading practice in physics education. The second recommendation is that teachers should educate themselves more about talented and gifted students.

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#### References

- Alvino, J., McDonnel, R. C., & Richert, S. (1981). National survey of identification practices in gifted and talented education. Exceptional Children, 48(2), 124-132. https://doi.org/10.1177/001440298104800205
- Andrzejewska, M., Stolińska, A., Błasiak, W., Pęczkowski, P., Rosiek, R., Rożek, B., Sajka, M., & Wcisło, D. (2016). Eye-tracking verification of the strategy used to analyse algorithms expressed in a flowchart and pseudocode. *Interactive Learning Environments*, 24(8), 1981-1995. https://doi.org/10.1080/10494820.2015.1073746
- Atkins, R. M., & McNeal, K. S. (2018). Exploring differences among student populations during climate graph reading tasks: An eye tracking study. *Journal of Astronomy & Earth Sciences Education (JAESE), 5*(2), 85-114. https://doi.org/10.19030/jaese. v5i2.10219
- Beichner, R. J. (1994). Testing student interpretation of kinematics graphs. American journal of Physics, 62(8), 750-762. https://doi.org/10.1119/1.17449
- Bertin, J. (1983). Semiology of graphics: Diagrams, networks, maps. Esri Press.
- Betts, G. T., & Neihart, M. (1988). Profiles of the gifted and talented. *Gifted Child Quarterly*, 32(2), 248-253. https://doi. org/10.1177/001698628803200202
- Bolden, D., Barmby, P., Raine, S., & Gardner, M. (2015). How young children view mathematical representations: a study using eye-tracking technology. *Educational Research*, 57(1), 59-79.
- Clark, B. (1988). Growing up gifted: Developing the potential of children at school and at home. Merrill/Prentice Hall.
- Coleman, L. J., & Cross, T. L. (2005). Being gifted in school: An introduction to development, guidance, and teaching. Prufrock Press.
- Curcio, F. R. (1987). Comprehension of mathematical relationships expressed in graphs. *Journal for Research in Mathematics Education*, *18*(5), 382-393.
- Dalmaijer, E. (2014). Is the low-cost EyeTribe eye tracker any good for research? *PeerJ PrePrints*, 1-35. https://doi.org/10.7287/ peerj.preprints.585v1
- Dolezalova, J., & Popelka, S. (2016). ScanGraph: A novel scanpath comparison method using visualisation of graph cliques. *Journal of Eye Movement Research*, 9(4), Article 5. https://doi.org/10.16910/jemr.9.4.5
- Galesic, M., & Garcia-Retamero, R. (2011). Graph literacy: A cross-cultural comparison. *Medical Decision Making*, 31(3), 444-457. https://doi.org/10.1177/0272989X10373805
- Glazer, N. (2011). Challenges with graph interpretation: A review of the literature. *Studies in Science Education, 47*(2), 183-210. https://doi.org/10.1080/03057267.2011.605307
- Goldberg, J., & Helfman, J. (2011). Eye tracking for visualization evaluation: Reading values on linear versus radial graphs. *Information Visualization*, 10(3), 182-195. https://doi.org/10.1177/1473871611406623
- Choi, H.-D., Shin, W.-S., & Shin, D.-H. (2012). Differences in eye movement pattern during the classification between the gifted and general students in elementary schools. *Journal of Korean Elementary Science Education*, 31(4), 501-512. https://doi. org/10.15267/keses.2015.34.1.142
- Janthanasub, V., & Meesad, P. (2015). Evaluation of a low-cost eye tracking system for computer input. *King Mongkut's University of Technology North Bangkok International Journal of Applied Science and Technology*, 8(3), 185-196. https://doi.org/10.14416/j. ijast.2015.07.001
- Jarodzka, H., Holmqvist, K., & Gruber, H. (2017). Eye tracking in educational science: Theoretical frameworks and research agendas. Journal of Eye Movement Research, 10(1), 1-18.
- Jeřábek, J., Krčková, S., & Hučínová, L. (2016). *Rámcový vzdělávací program pro gymnázia* [Framework educational program for grammar schools]. Výzkumný ústav pedagogický v Praze. http://www.nuv.cz/t/rvp-pro-gymnazia
- Kekule, M. (2014). Students' approaches when dealing with kinematics graphs explored by eye-tracking research method Frontiers in mathematics and science education research conference, FISER, Famagusta, North Cyprus.
- Kim, S., Lombardino, L. J., Cowles, W., & Altmann, L. J. (2014). Investigating graph comprehension in students with dyslexia: An eye tracking study. *Research in Developmental Disabilities*, 35(7), 1609-1622. https://doi.org/10.1016/j.ridd.2014.03.043
- Kim, S., & Wiseheart, R. (2017). Exploring text and icon graph interpretation in students with dyslexia: An eye-tracking study. *Dyslexia*, 23(1), 24-41. https://doi.org/10.1002/dys.1551

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STUDENTS' ABILITY TO WORK WITH GRAPHS IN PHYSICS STUDIES RELATED TO THREE TYPICAL STUDENT GROUPS (P. 298-316)

- Kozhevnikov, M., Motes, M. A., & Hegarty, M. (2007). Spatial visualization in physics problem solving. *Cognitive Science*, 31(4), 549-579. https://doi.org/10.1080/15326900701399897
- Leinhardt, G., Zaslavsky, O., & Stein, M. K. (1990). Functions, graphs, and graphing: Tasks, learning, and teaching. *Review of Educational Research*, 60(1), 1-64.
- Lowrie, T., & Diezmann, C. M. (2007). Solving graphics problems: Student performance in junior grades. *The Journal of Educational Research*, 100(6), 369-378. https://doi.org/10.3200/JOER.100.6.369-378
- Madsen, A. M., Larson, A. M., Loschky, L. C., & Rebello, N. S. (2012). Differences in visual attention between those who correctly and incorrectly answer physics problems. *Physical Review Special Topics-Physics Education Research*, 8(1), 010122. https:// doi.org/10.1103/PhysRevSTPER.8.010122
- McClelland, D. C., Baldwin, A. L., Bronfenbrenner, U., & Strodtbeck, F. L. (1958). *Talent and society: New perspectives in the identification of talent*. Van Nostrand.
- McDermott, L. C., Rosenquist, M. L., & Van Zee, E. H. (1987). Student difficulties in connecting graphs and physics: Examples from kinematics. *American Journal of Physics*, 55(6), 503-513. https://doi.org/10.1119/1.15104
- Moreno-Esteva, E., White, S., Wood, J., & Black, A. (2017). *Identifying key visual-cognitive processes in students' interpretation of graph representations using eye-tracking data and math/machine learning based data analysis* Tenth Congress of the European Society for Research in Mathematics Education (CERME10), Dublin, Ireland.
- Neihart, M. (2011, August 2011). *The revised profiles of the gifted: A research based approach*. World Council for Gifted and Talented Children, Prague.
- Ooms, K., Dupont, L., Lapon, L., & Popelka, S. (2015). Accuracy and precision of fixation locations recorded with the low-cost Eye Tribe tracker in different experimental set-ups. *Journal of Eye Movement Research*, 8(1), 1-24. https://doi.org/10.16910/ jemr.8.1.5
- Opach, T., Popelka, S., Dolezalova, J., & Rod, J. K. (2017). Star and Polyline Glyphs in a Grid Plot and on a Map Display: Which perform better? *Cartography and Geographic Information Science*, 1-20. https://doi.org/10.1080/15230406.2017.1364169 Page, S. E. (2018). *The model thinker: What you need to know to make data work for you*. Hachette UK.
- Popelka, S. (2014). Optimal eye fixation detection settings for cartographic purposes. In. 14th International Multidisciplinary Scientific GeoConference SGEM 2014, (SGEM2014 Conference Proceedings, June 19-25, Book 2, Vol. 1, 705-712 pp.). https://www. sgem.org/sgemlib/spip.php?article4088
- Popelka, S., Dolezalova, J., & Beitlova, M. (2018). New features of scangraph: A tool for revealing participants' strategy from eyemovement data. In *Proceedings of the 2018 ACM Symposium on Eye Tracking Research & Applications (ETRA '18)*. Association for Computing Machinery, New York, NY, USA, Article 103, 1–2. https://doi.org/10.1145/3204493.3208334
- Popelka, S., Stachoň, Z., Šašinka, Č., & Doležalová, J. (2016). EyeTribe Tracker data accuracy evaluation and its interconnection with Hypothesis Software for Cartographic Purposes. *Computational Intelligence and Neuroscience, 2016*, 1-14, Article 9172506. https://doi.org/10.1155/2016/9172506
- Pöschl, R. (2007). Vnímání fyziky středoškolskými studenty–včera dnes a zítra [Perception of physics by high school students... yesterday, today and tomorrow]. 50 let Didaktiky Fyziky v ČR, Prague.
- Renzulli, J. S. (1990). A practical system for identifying gifted and talented students. *Early Child Development and Care, 63*(1), 9-18. https://doi.org/10.1080/0300443900630103
- Rosengrant, D., Thomson, C., & Mzoughi, T. (2009). Comparing experts and novices in solving electrical circuit problems with the help of eye-tracking. In AIP Conference Proceedings, 1179.1, 249-252. https://doi.org/10.1063/1.3266728
- Sajka, M., & Rosiek, R. (2015). Solving a problem by students with different mathematical abilities: A comparative study using eyetracking. In CERME 9 - Ninth Congress of the European Society for Research in Mathematics Education, (Charles University in Prague, Faculty of Education; ERME, Feb 2015, Prague, Czech Republic, pp.1752-1758). https://hal.archives-ouvertes.fr/ hal-01288030
- Shah, P., & Hoeffner, J. (2002). Review of graph comprehension research: Implications for instruction. *Educational Psychology Review*, 14(1), 47-69. https://doi.org/10.1023/A:1013180410169
- Shayan, S., Abrahamson, D., Bakker, A., Duijzer, C. A., & van der Schaaf, M. (2017). Eye-tracking the emergence of attentional anchors in a mathematics learning tablet activity. In C. Was, F. Sansosti, & B. Morris (Eds.), *Eye-tracking technology applications in educational research* (pp. 166-194). IGI Global. https://doi:10.4018/978-1-5225-1005-5.ch009
- Schindler, M., Lilienthal, A. J., Chadalavada, R., & Ögren, M. (2016). Creativity in the eye of the student. Refining investigations of mathematical creativity using eye-tracking goggles. In C. Csíkos, A. Rausch, & J. Szitányi (Eds.), Proceedings of the 40th Conference of the International Group for the Psychology of Mathematics Education (PME). http://urn.kb.se/resolve?urn=ur n:nbn:se:oru:diva-55235
- Strobel, B., Lindner, M. A., Saß, S., & Köller, O. (2018). Task-irrelevant data impair processing of graph reading tasks: An eye tracking study. *Learning and Instruction*, 55, 139-147. https://doi.org/10.1016/j.learninstruc.2017.10.003
- Strobel, B., Saß, S., Lindner, M. A., & Köller, O. (2016). Do graph readers prefer the graph type most suited to a given task? Insights from eye tracking. *Journal of Eye Movement Research, 9*(4), 1-15. https://doi.org/10.16910/jemr.9.4.4
- Susac, A., Bubic, A., Kazotti, E., Planinic, M., & Palmovic, M. (2018). Student understanding of graph slope and area under a graph: A comparison of physics and nonphysics students. *Physical Review Physics Education Research*, 14(2), 1-15. https://doi. org/10.1103/PhysRevPhysEducRes.14.020109
- Škrabánková, J., & Trnová, E. (2015). Researching students gifted in science using the method of eye tracking. *e-Pedagogi-um*, 15(4), 79-93. https://doi.org/10.5507/epd.2015.048

students' ability to work with graphs in physics studies related to three ISSN 1648-3898 /print/ typical student groups (p. 298-316) ISSN 2538-7138 /Online/

Tai, R. H., Loehr, J. F., & Brigham, F. J. (2006). An exploration of the use of eye-gaze tracking to study problem-solving on standardized science assessments. *International Journal of Research & Method in Education*, 29(2), 185-208. https://doi. org/10.1080/17437270600891614

Tan, J. K., & Benbasat, I. (1990). Processing of graphical information: A decomposition taxonomy to match data extraction tasks and graphical representations. *Information Systems Research*, 1(4), 416-439. https://www.jstor.org/stable/23010666 Tuttle Jr, F. B. (1988). *Characteristics and identification of gifted and talented students*. ERIC.

Van der Linden, S. L., Leiserowitz, A. A., Feinberg, G. D., & Maibach, E. W. (2014). How to communicate the scientific consensus on climate change: Plain facts, pie charts or metaphors? *Climatic Change*, 126(1-2), 255-262. https://doi.org/10.1007/ s10584-014-1190-4

Viiri, J., Kekule, M., Isoniemi, J., & Hautala, J. (2017). Eye-tracking the effects of representation on students' problem solving approaches. *FMSERA Journal*, 1(1), 88-98. https://journal.fi/fmsera/article/view/60941

Vila, J., & Gomez, Y. (2016). Extracting business information from graphs: An eye tracking experiment. *Journal of Business Research*, 69(5), 1741-1746. https://doi.org/10.1016/j.jbusres.2015.10.048

Voßkühler, A., Nordmeier, V., Kuchinke, L., & Jacobs, A. M. (2008). OGAMA (Open Gaze and Mouse Analyzer): Open-source software designed to analyze eye and mouse movements in slideshow study designs. *Behavior Research Methods*, 40(4), 1150-1162. https://doi.org/10.3758/BRM.40.4.1150

Wainer, H. (1992). Understanding graphs and tables. *Educational Researcher*, 21(1), 14-23. https://doi.org/10.3102/0013189X021001014 Was, C., Sansosti, F., & Morris, B. (2016). *Eye-tracking technology applications in educational research*. IGI Global. https://doi.

org/10.4018/978-1-5225-1005-5

Wolff, C. E., Jarodzka, H., & Boshuizen, H. P. (2017). See and tell: Differences between expert and novice teachers' interpretations of problematic classroom management events. *Teaching and Teacher Education*, *66*, 295-308.

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