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Software Cost Estimation by Optimizing COCOMO Model Using Hybrid BATGSA Algorithm

Deepak Nandal¹* Om Prakash Sangwan¹

¹Department of Computer Science and Engineering, Guru Jambheshwar University of Science and Technology, Hisar, Haryana, India * Corresponding author's Email: dr.deepaknandalgju@gmail.com

Abstract: This paper estimates the effort for software by optimizing the COnstructive COst MOdel (COCOMO) model parameters using hybrid BATGSA (Bat inspired Gravitational Search Algorithm) algorithm. The performance of the COCOMO model completely depends upon its parameters which can be optimized by using meta-heuristic algorithms. This paper uses hybrid BATGSA algorithm which hybrids the improved bat algorithm with the gravitation search algorithm (GSA) to optimize the COCOMO model. The bat algorithm demonstrates the hunting and routing behavior of the bat which is improved by using a random walk in the exploration phase. The exploration phase is further improved by using GSA as gravitation force affects the velocity of the bat. The algorithm has been analyzed on four NASA datasets downloaded from promise repository. The comparison of the algorithm has been made with existing three states of art techniques i.e. COCOMO model, BAT algorithm, Improved BAT(IBAT) algorithm by using normalized error as a parameter. The reduction in error ranges from 2% to 10% on different dataset as compared other state of art algorithms proves the significance of proposed algorithm.

Keywords: NASA project dataset, COCOMO, BAT, GSA, Optimization.

1. Introduction

Software cost estimation is a critical process as it is required to estimate the cost of the project at the initial stage of the project. The cost estimation is required to compute the budget and the resources required for the project [1, 2]. The cost of the project depends upon the efforts done which include the number of reviews. efficiency during implementation and pre-development processing, etc [3]. The Constructive Cost Model (COCOMO) is a model to determine the cost of the software. This model uses a basic regression formula for estimating cost, effort, and schedule for software projects based on features of the project. The model calculates the efforts as $E=a \times (KLOC)b$, here KLOC shows the kilo line of code and a, b are the constants which depends upon the type of software [4]. This model can be optimized by using meta-heuristic algorithm [5]. Different authors have applied the various metaheuristic algorithm to improve the performance of the COCOMO model. The author of [6] has applied a genetic algorithm to optimize the parameters of COCOMO model while the author of [1] has applied differential evolution algorithm for the same. The author of [7] has applied BAT algorithm to improve the performance of cost estimation by COCOMO. The author of [7] shows the reduction in error by optimizing the COCOMO model using BAT algorithm. The BAT algorithm shows the better result as compared other existing state of the art techniques but BAT algorithm search locally in the exploration phase which opens scope for the improvement. This paper optimizes the estimation using COCOMO model by using hybrid BATGSA algorithm. The hybrid BATGSA algorithm has better convergence towards the global optima as it has improved exploration phase as compared to BAT algorithm, resulting in better optimization of COCOMO model. This paper further has been classified in five sections. The next section i.e. section 2 describes the improved BAT algorithm

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which is followed by the description of Gravitation search algorithm (GSA) in section 3. The Hybrid BATGSA algorithm has been described in section 4 while the results and corresponding discussion is done in section 5.

2. Improved BAT algorithm for cost estimation

Bat algorithm performs well for the various applications [8, 9]. This algorithm automatically switches from the exploration phase i.e. global search, to the exploitation phase i.e. local search. The main limitation of the algorithm is that it mainly searches locally even in the exploration phase [7, 9]. In the exploration phase change in the frequency is the parameter for the global search which restricts the search locally mainly. This behavior has been changed by introducing the random move nature to the bat resultant velocity updation is given by Eq. (1). Suppose there are n bats with position vector P[1 : n] and velocity vector V[1 : n] i.e. P_a^t, V_a^t denotes the position and velocity of the ath bat at tth time. Moreover, there is a frequency vector f[1:n]that denotes the frequency of each bat which lies between fmin and fmax The velocity of each bat is adjusted according to frequency using the equation

$$V_{a}^{t} = \begin{cases} V_{a}^{t-1} + (P_{a}^{t-1} - P^{b})f_{a} \\ V_{a}^{t-1} + (P_{a}^{t-1} - P^{r})Xpr \end{cases} \begin{array}{c} pr < 0.5 \\ else \end{cases}$$
(1)

Here pr is the probability which is generated randomly by using a random function and P^r is position at any random time stamp. This updation strength the exploration phase and improves the global search. Correspondingly position update can be given by Eq. (2) to improve the impact of velocity on the position.

$$P_{a}^{t} = \begin{cases} P_{a}^{t-1} + V_{a}^{t} & pr < 0.5\\ P_{a}^{t-1} + V_{a}^{t} f_{a} & else \end{cases}$$
(2)

The Eq. (2) updates the position of the bat according to the velocity update. The local search phase of the algorithm is powerful enough to exploit the search space. The improved bat algorithm is as follow:

IBAT Algorithm (P, V, f, F, emr⁰, L):

Here, P, V, f are the position, velocity and frequency vector for n bats respectively. The F is the fitness function to evaluate the fitness of the solution generated by the corresponding position. The L is the loudness vector and emr^0 is initial emission rate.

- 1. Initiate iteration=1
- 2. $P^{b}=P_{1}$
- 3. For i=2:n a. If $F(P_i) > F(P^b)$ b. $P^b=P_i$ c. End if End
- 4. While iteration<max_iteration

a.
$$f_{iteration} = f_{\min} + (f_{\max} - f_{\min})\alpha$$

- b. pr=rand
- c. r=rand(1,n)

$$\mathbf{d.} \qquad V_{1:n}^{iteration} = \begin{cases} V_{1:n}^{iteration-1} + (P_{1:n}^{iteration-1} - P^{b})f_{a} \\ V_{1:n}^{iteration-1} + (P_{1:n}^{iteration-1} - P^{r})Xpr \end{cases} \begin{array}{c} pr < 0.5 \\ else \end{cases}$$

e.
$$P_{1:n}^{iteration} = \begin{cases} P_{1:n}^{iteration-1} + V_{1:n}^{iteration} \\ P_{1:n}^{iteration-1} + V_{1:n}^{iteration} f_{1:n} \\ else \end{cases} pr < 0.5$$

f. If rand > emr^{iteration-1}

$$P_{1:n}^{iteration} = P_{1:n}^{iteration-1} + \varepsilon L^{iteration}$$

End if

g. If
$$F(P_{1:n}^{iteration}) > F(P_{1:n}^{iteration-1})$$

 $P_{1:n}^{iteration} = P_{1:n}^{iteration-1}$
Else
 $L_{1:n}^{iteration} = L_{1:n}^{iteration-1}\beta$
 $emr_{1:n}^{iteration} = emr_{1:n}^{0}(1 - e^{-\lambda(iteration-1)})$
End if

- h. For i=1:n i. If $F(P_i) > F(P^b)$ ii. $P^b=P_i$ iii. End if End
- i. iteration++ End while

The above algorithm gives the process of improved bat algorithm [10, 11]. This algorithm has been applied to the cost estimation of software by using the objective function given by Eq. (3)

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$$F(P) = \frac{\left(\sum_{i=1}^{n} (actual_{i} - predicted_{i}) / actual_{i}\right)}{n}$$
(3)

which calculates the mean relative error which depends upon the actual and the predicted estimation. The performance of the algorithm can be improved discussed in next section.

3. Gravitational search algorithm

The gravitational search algorithm uses the law of gravity given by Newton [12]. According to Newton every particle attracts another particle with a gravitational force that can be given by Eq. (4).

$$F = G \frac{M_1 M_2}{D^2} \tag{4}$$

Here, G is the gravitational constant, D is the distance between two objects having masses M_1 and M_2 respectively. The details of GSA are as follow. Suppose we have n objects in d dimensions then

position matrix for objects can be given by Eq. (5).

$$O = \begin{bmatrix} O_1^1 & O_1^2 & L & O_1^d \\ O_2^1 & O_2^2 & L & O_2^d \\ M & M & M & M \\ O_n^1 & O_n^2 & L & O_n^d \end{bmatrix}$$
(5)

Here, O_i^j represents the position of ith object in the jth dimension. At a particular time stamp say t the force acting on object p from object q can be given by Eq. (6).

$$F_{pq}^{1:d}(t) = G(t) \frac{M_p^a(t)M_q^p(t)}{D_{pq}(t) + \varepsilon} \Big(O_i^{1:d}(t) - O_j^{1:d}(t) \Big)$$
(6)

Here $M_p^a(t)$, $M_q^p(t)$ are active and passive gravitational masses of object p and q respectively. ε is a small constant with value 2⁻⁵², $D_{pq}(t)$ is the distance between object p and object q which is given by Eq. (7).

$$D_{pq}(t) = \sqrt{\sum_{i=1}^{d} (O_p^i - O_q^i)^2}$$
(7)

Overall the total force acting on any object p can be given by Eq. (8)

$$F_{p}^{1:d}(t) = \sum_{i=1, i \neq p}^{n} F_{pi}^{1:d} Xrand_{i}$$
(8)

So the acceleration is given by Eq. (9).

$$a_{p}^{1:d}(t) = \frac{F_{p}^{1:d}(t)}{O_{p}(t)}$$
(9)

Here, $O_p(t)$ is the inertia mass of object p.

This acceleration is used to update the velocity of the object which affects the position of an object demonstrated by Eqs. (10) and (11).

$$v_{p}^{!:d}(t+1) = v_{p}^{!:d}(t) Xrand + a_{p}^{!:d}(t)$$
 (10)

and

$$O_p^{1:d}(t+1) = O_p^{1:d}(t) + v_p^{1:d}(t+1)$$
(11)

The whole process is repeated for the updated position for the given number of iterations or until fulfilling the stopping criteria. The overall GSA algorithm can be given as follow.

GSA (O, M, Fit)

The algorithm uses O as the object position matrices with M as the mass metric containing mass of each object. Fit is the fitness function.

1. Initiate iteration=1

2.
$$O = \begin{bmatrix} O_1^1 & O_1^2 & L & O_1^d \\ O_2^1 & O_2^2 & L & O_2^d \\ M & M & M & M \\ O_n^1 & O_n^2 & L & O_n^d \end{bmatrix}$$

3. While iteration < max_iteration

| Fit(t) = | | | | |
|------------------|---------------------------------|---|-----------------------|--|
| $Fit(O_1^1(t))$ | $Fit(O_1^2(t))$ | L | $Fit(O_1^d(t))$ | |
| $Fit(O_2^1(t))$ | $Fit(O_1^2(t))$ $Fit(O_2^2(t))$ | L | $Fit(O_2^d(t))$ | |
| М | $M \\ Fit(O_n^2(t))$ | М | M Fit $(O_n^d(t))$ | |
| Fit $(O_n^1(t))$ | $Fit(O_n^2(t))$ | L | $Fit(O_n^d(t))$ | |

b.
$$D_{pq}(t) = \sqrt{\sum_{i=1}^{d} (O_p^i - O_q^i)^2}$$

C.
$$F_{pq}^{1:d}(t) = G(t) \frac{M_p^a(t)M_q^p(t)}{D_{pq}(t) + \varepsilon} \Big(O_i^{i:d}(t) - O_j^{1:d}(t) \Big)$$

d.
$$F_p^{1:d}(t) = \sum_{i=1, i \neq p}^n F_{pi}^{1:d} Xrand_i$$

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e.
$$a_p^{1:d}(t) = \frac{F_p^{1:d}(t)}{O_p(t)}$$

f. $v_p^{1:d}(t+1) = v_p^{1:d}(t) Xrand + a_p^{1:d}(t)$
g. $O_p^{1:d}(t+1) = O_p^{1:d}(t) + v_p^{1:d}(t+1)$
h. If Fit(t)O_p^{1:d}(t+1) = O_p^{1:d}(t)
end
End while

4. Return best(F)

The above algorithm performs the optimization. The fitness has been given by Eq. (3) to determine the software cost estimation. The improved bat

1. Initiate iteration=1

2.
$$P = \begin{bmatrix} P_1^1 & P_1^2 & L & P_1^d \\ P_2^1 & P_2^2 & L & P_2^3 \\ M & M & M & M \\ P_n^1 & P_n^2 & L & P_n^d \end{bmatrix}$$

3.
$$Fit(iteration) = \begin{bmatrix} Fit(P_1^1(iteration)) & Fit(P_1^2(iteration)) & L & Fit(P_1^d(iteration)) \\ Fit(P_2^1(iteration)) & Fit(P_2^2(iteration)) & L & Fit(P_2^d(iteration)) \\ M & M & M \\ Fit(P_n^1(iteration)) & Fit(P_n^2(iteration)) & L & Fit(P_n^d(iteration)) \end{bmatrix}$$

4.
$$P^b = P_1$$

5. For i=2:n
a. If
$$Fit(P_i) > Fit(P^b)$$

b. $P^b=P_i$
c. End if

End

- 6. While iteration<max_iteration
 - a. $f_{iteration} = f_{\min} + (f_{\max} f_{\min})\alpha$

b. pr=rand

c. r=rand(1,n)

algorithm is hybridized by using gravitational search algorithm discussed in next section.

4. Hybrid BATGSA algorithm

In the real-time the gravitational force as the impact the velocity of the BAT. in this work to improve the exploration phase of the algorithm the velocity factor has been affected by the gravitational force also. This improves the global search capability of the algorithm resulting better convergence for optimization. The concept can be easily understood by following algorithm:

BATGSA Algorithm (P, V, M, f, Fit, emr⁰, L)

Here, P, V, M, f are the position, velocity, mass and frequency vector for n bats respectively. The Fit is the fitness function to evaluate the fitness of the solution generated by corresponding position. The L is the loudness vector and emr⁰ is initial emission rate.

d.
$$V_{1:n}^{iteration} = \begin{cases} V_{1:n}^{iteration-1} + (P_{1:n}^{iteration-1} - P^b) f_a \\ V_{1:n}^{iteration-1} + (P_{1:n}^{iteration-1} - P^r) Xpr \end{cases} \begin{vmatrix} pr < 0.5 \\ else \end{vmatrix}$$

e.
$$P_{1:n}^{iteration} = \begin{cases} P_{1:n}^{iteration-1} + V_{1:n}^{iteration} \\ P_{1:n}^{iteration-1} + V_{1:n}^{iteration} f_{1:n} \end{cases} \begin{cases} pr < 0.5 \\ else \end{cases}$$

f. If rand $> emr^{iteration-1}$

$$P_{1:n}^{iteration} = P_{1:n}^{iteration-1} + \varepsilon L^{iteration}$$

End if

$$r q=1:n$$

$$D_{pq}(iteration-1) = \sqrt{\sum_{i=1}^{d} (P_{p}^{i} - P_{q}^{i})^{2}}$$

$$F_{pq}^{1:d}(iteration-1) = G(iteration) \frac{M_{p}^{a}(t)M_{q}^{p}(t)}{D_{pq}(t) + \varepsilon} \left(P_{p}^{i:d}(iteration) - P_{q}^{1:d}(t)\right)$$

End

ii.
$$F_p^{1:d}$$
 (iteration -1) = $\sum_{i=1, i \neq p}^n F_{pi}^{1:d} Xrand_i$

iii.
$$a_p^{1:d}$$
 (iteration -1) = $\frac{F_p^{1:d}$ (iteration)}{P_p(iteration)

iv.
$$v_p^{1:d}(iteration) = v_p^{1:d}(iteration - 1)Xrand + a_p^{1:d}(iteration - 1)$$

v.
$$P_p^{1:d}(iteration) = P_p^{1:d}(iteration-1) + v_p^{1:d}(iteration)$$

End

h. If Fit(
$$P_{1:n}^{iteration}$$
) > Fit($P_{1:n}^{iteration-1}$)
 $P_{1:n}^{iteration} = P_{1:n}^{iteration-1}$
Else

$$L_{1:n}^{iteration} = L_{1:n}^{iteration-1}\beta$$
$$emr_{1:n}^{iteration} = emr_{1:n}^{0}(1 - e^{-\lambda(iteration-1)})$$

End if

i. For i=1:n
i. If
$$F(P_i) > F(P^b)$$

ii. $P^b=P_i$
iii. End if
End

j. iteration++ End while

The above algorithm updates the position of the bat firstly on the basis of frequency of the sound then this position is updated on the basis of the gravitational force on bat for the global search while the local search still depends upon the loudness of the sound. This algorithm produces exploration as well as exploitation search so the optimization must converge towards the global optima. The objective function given in Eq. (3) has been used for the cost estimation. The implementation of algorithm and the result analysis has been discussed in next section.

5. Results and discussion

The algorithm discussed in previous section has been implemented using MATLAB. The analysis has been done on 4 datasets, 2 are the NASA datasets containing 60 and 93 projects respectively and other two are COCOMO81 and kemerer. All datasets has been downloaded from the promise data repository. The actual cost of each software project is available in the dataset which is compared with the estimated cost to calculate the mean relative error for each project. The comparison of the hybrid BATGSA algorithm is done with the COCOMO based cost estimation i.e. cost estimation without optimization [3] with the BAT [7] and improved BAT based optimization [11]. The remaining section of the paper uses Dataset1 for the cocomo81 dataset, Dataset2 for NASA dataset having 60 projects, Dataset3 for NASA dataset with 93 project and Dataset 4 for kemerer dataset. The software effort estimation for Dataset1 has been analyzed in Table1.

The effort estimation for each project in the Dataset1 has been shown in the table 1. The analysis Table 1 shows that the value of the effort converges towards the actual effort but for some project the estimation is producing higher error. This is because the algorithm reduces the mean absolute error in cost estimation by Eq. (8). The mean absolute error in the Dataset1 has been to 433.215 from 437.537(Improved BAT), 444.405 (Bat algorithm) which is reduced from 680.154 in COCOMO model. The normalized error in each project of Dataset1 has been analyzed in figure 1. The normalized error has been calculated by Eq. (12).

$$NE_i = abs(actual_i - predicted_i) / actual_i$$
 (12)

Here, NE_i is the normalized error for i-th project which has been calculated by using actual and predicted effort of the project.

The Fig. 1 clearly shows that normalized error has been reduced by using hybrid BATGSA is more as compared to reduction by improving the bat algorithm and bat algorithm. This is due to the better optimization of COCOMO model by BATGSA algorithm which is due to better exploration phase of BATGSA algorithm.

The software cost/effort estimation for each undertaking in the Dataset2 has been appeared in the table 2. The mean absolute error in the Dataset2 has been to 127.530 from 132.486 in improved BAT and 137.401 (Bat calculation) which is decreased from 400.985 in COCOMO display. The standardized error in each project of Dataset2 has been investigated in Fig. 2 which is computed by Eq. (12).

The Fig. 2 unmistakably connotes that normalized error has been reduced by hybrid BATGSA calculation is higher than the reduction done by improved bat and bat calculation due to avoidance of local minima by the BATGSA algorithm.

The effort estimation for each project in the Dataset3 has been shown in the Table 3. The analysis table 3 shows that the value of the effort converges towards the actual effort but for some project the estimation is producing higher error. This is because the algorithm reduces the mean absolute error in cost estimation by Eq. (3). The mean absolute error in the Dataset1 has been to 355.386 from 356.143(improved BAT), 365.164 (Bat algorithm) which is reduced from 618.412 in COCOMO model.

The Fig. 3 clearly shows that normalized error has been reduced by using hybrid BATGSA is more as compared to reduction by improving the bat algorithm and bat algorithm. This is due to the better optimization of COCOMO model by BATGSA algorithm which is due to better exploration phase of BATGSA algorithm.

The software cost/effort estimation for each undertaking in the Dataset4 has been appeared in the table 4. The mean absolute error in the Dataset4 has been to 2398.141 from 4564.934 in improved BAT and from 5528.158 (Bat calculation) which is decreased from 6804.450 in COCOMO display. The standardized error in each project of Dataset4 has been investigated in figure 4 which is computed by Eq. (12).

The Fig. 4 unmistakably connotes that normalized error has been reduced by hybrid BATGSA calculation is higher than the reduction done by improved bat and bat calculation. This is due to the velocity variation done to explore the search space appropriately. This shows that the hybrid BATGSA algorithm improves the estimation of the software effort.

| Table 1. Analysis of effort estimation on Dataset 1 | | | | | | | |
|---|----------------------------------|----------------------|---------------------|----------|--------|--|--|
| Project Number | Hybrid BATGSA Optimization | IBAT Optimization | BAT Optimization | СОСОМО | Actual | | |
| 1 | 500.0036 | 454.2916 | 474.5296 | 3.134719 | 2040 | | |
| 2 | 1446.034 | 1362.665 | 1443.515 | 3 | 1600 | | |
| 3 | 594.5699 | 543.4377 | 568.9498 | 3 | 243 | | |
| 4 | 246.9118 | 218.9643 | 226.593 | 3.134719 | 240 | | |
| 5 | 56.58902 | 47.70643 | 48.41535 | 3 | 33 | | |
| 6 | 12.0693 | 9.64865 | 9.593832 | 3 | 43 | | |
| 7 | 22.16179 | 18.09085 | 18.13331 | 3 | 8 | | |
| 8 | 80.70177 | 68.86921 | 70.22168 | 3.270061 | 1075 | | |
| 9 | 114.0294 | 98.4732 | 100.8675 | 3 | 423 | | |
| 10 | 109.801 | 94.69864 | 96.95262 | 3 | 321 | | |
| 11 | 122.5342 | 106.0797 | 108.7624 | 3 | 218 | | |
| 12 | 144.0569 | 125.4077 | 128.8548 | 3.270061 | 201 | | |
| 13 | 93.0598 | 79.80509 | 81.52591 | 3 | 79 | | |
| 14 | 8.758434 | 6.925093 | 6.856592 | 3.782814 | 60 | | |
| 15 | 11.73347 | 9.371089 | 9.314369 | 3.782814 | 61 | | |
| 16 | 19.31758 | 15.69484 | 15.70312 | 3 | 40 | | |
| 17 | 10.73201 | 8.54502 | 8.483278 | 3 | 9 | | |
| 18 | 1595.32 | 1508.428 | 1600.005 | 3.270061 | 11400 | | |
| 19 | 6638.286 | 6591.914 | 7125.294 | 3 | 6600 | | |
| 20 | 1479.077 | 1394.886 | 1478.089 | 3.270061 | 6400 | | |
| 21 | 1222.389 | 1145.283 | 1210.54 | 3 | 2455 | | |
| 22 | 524.7245 | 477.5438 | 499.1363 | 3.782814 | 724 | | |
| 23 | 326.0589 | 291.9289 | 303.2134 | 3.782814 | 539 | | |
| 24 | 387.982 | 349.452 | 363.7963 | 3 | 453 | | |
| 25 | 148.4032 | 129.3233 | 132.9303 | 3.270061 | 523 | | |
| 26 | 192.5427 | 169.2959 | 174.6185 | 3.270061 | 387 | | |
| 27 | 31.28028 | 25.83853 | 26.01757 | 3.270061 | 88 | | |
| 28 | 44.8975 | 37.55026 | 37.99172 | 3 | 98 | | |
| 29 | 6.01046 | 4.69124 | 4.621749 | 3.782814 | 7.3 | | |
| 30 | 5.51178 | 4.289229 | 4.220852 | 3.782814 | 5.9 | | |
| 31 | 256.1027 | 227.4003 | 235.4368 | 3 | 1063 | | |
| 32 | 1988.874 | 1894.85 | 2015.761 | 3 | 702 | | |
| 33 | 165.9165 | 145.1403 | 149.4089 | 3 | 605 | | |
| 34 | 84.80089 | 72.49063 | 73.9627 | 3.782814 | 230 | | |
| 35 | 44.8975 | 37.55026 | 37.99172 | 3 | 82 | | |
| 36 | 52.66131 | 44.28563 | 44.90095 | 3.134719 | 55 | | |
| 37 | 246.9118 | 218.9643 | 226.593 | 3 | 47 | | |
| 38 | 52.66131 | 44.28563 | 44.90095 | 3 | 12 | | |
| 39 | 19.67088 | 15.99184 | 16.00411 | 3 | 8 | | |
| 40 | 8.758434 | 6.925093 | 6.856592 | 3 | 8 | | |

Table 1. Analysis of effort estimation on Dataset 1

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| 41 | 16.51591 | 13.34653 | 13.3259 | 3 | 6 |
|----|----------|----------|----------|----------|------|
| 42 | 181.3991 | 159.1714 | 164.0462 | 3.134719 | 45 |
| 43 | 108.1143 | 93.19433 | 95.39297 | 3.134719 | 83 |
| 44 | 116.5742 | 100.7472 | 103.2269 | 3.134719 | 87 |
| 45 | 135.4051 | 117.6252 | 120.7594 | 3.134719 | 106 |
| 46 | 307.2369 | 274.5156 | 284.9027 | 3.134719 | 126 |
| 47 | 84.80089 | 72.49063 | 73.9627 | 3.134719 | 36 |
| 48 | 2413.831 | 2315.072 | 2469.116 | 3.134719 | 1272 |
| 49 | 392.7899 | 353.9322 | 368.5205 | 3 | 156 |
| 50 | 88.92049 | 76.13621 | 77.73109 | 3 | 176 |
| 51 | 33.51367 | 27.74908 | 27.96687 | 3.134719 | 122 |
| 52 | 26.86333 | 22.07421 | 22.18244 | 3 | 41 |
| 53 | 16.51591 | 13.34653 | 13.3259 | 3.270061 | 14 |
| 54 | 13.42202 | 10.76931 | 10.72319 | 3 | 20 |
| 55 | 20.02484 | 16.28958 | 16.30592 | 3 | 18 |
| 56 | 101.3949 | 87.20966 | 89.19133 | 3.270061 | 958 |
| 57 | 60.54499 | 51.1601 | 51.96679 | 3.782814 | 237 |
| 58 | 93.0598 | 79.80509 | 81.52591 | 3 | 130 |
| 59 | 84.80089 | 72.49063 | 73.9627 | 3 | 70 |
| 60 | 21.44701 | 17.48765 | 17.5211 | 3.270061 | 57 |
| 61 | 105.5893 | 90.94392 | 93.06036 | 3 | 50 |
| 62 | 30.16963 | 24.89016 | 25.05064 | 3 | 38 |
| 63 | 33.51367 | 27.74908 | 27.96687 | 3 | 15 |

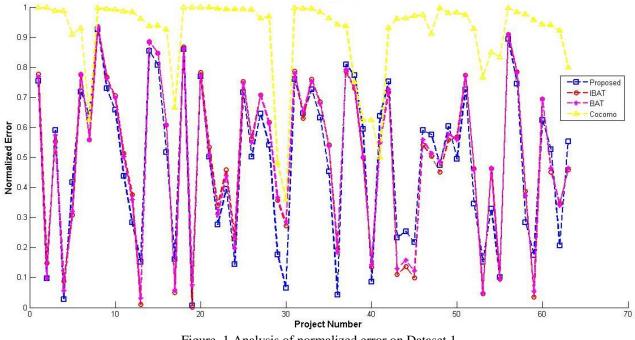
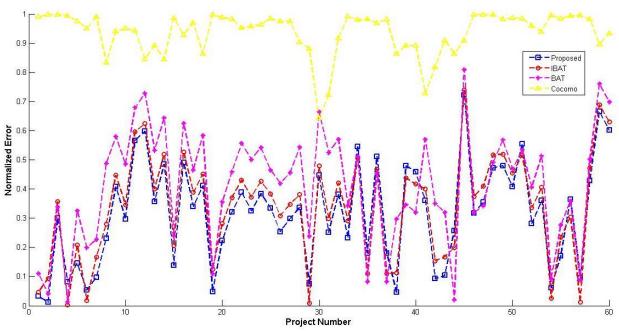


Figure. 1 Analysis of normalized error on Dataset 1

| Project Number | Hybrid BATGSA Optimization | IBAT Optimization | BAT Optimization | СОСОМО | Actual |
|-------------------|----------------------------------|----------------------|---------------------|----------|--------|
| 1 | 287.2043 | 265.0441 | 247.4643 | 3 | 278 |
| 2 | 1167.179 | 1070.171 | 1132.798 | 3 | 1181 |
| 3 | 872.9328 | 801.4547 | 826.5829 | 3 | 1248 |
| 4 | 523.2879 | 481.5761 | 474.4389 | 3 | 480 |
| 5 | 102.5464 | 95.08511 | 80.96048 | 3 | 120 |
| 6 | 63.37579 | 58.8953 | 48.03242 | 3 | 60 |
| 7 | 270.6567 | 249.8417 | 232.0345 | 3 | 300 |
| 8 | 13.85218 | 12.96357 | 9.227148 | 3 | 18 |
| 9 | 29.59828 | 27.60263 | 21.0285 | 3 | 50 |
| 10 | 42.18202 | 39.27361 | 30.88377 | 3 | 60 |
| 11 | 49.45893 | 46.01497 | 36.70414 | 6.520409 | 114 |
| 12 | 16.90391 | 15.80499 | 11.45188 | 6.520409 | 42 |
| 13 | 38.61608 | 35.96821 | 28.06175 | 6.520409 | 60 |
| 14 | 21.65029 | 20.2197 | 14.9788 | 6.520409 | 42 |
| 15 | 387.5022 | 357.109 | 342.4826 | 6.520409 | 450 |
| 16 | 45.79719 | 42.62334 | 33.76551 | 6.520409 | 90 |
| 17 | 138.6684 | 128.3999 | 112.3196 | 6.520409 | 210 |
| 18 | 28.24655 | 26.34772 | 19.98866 | 6.520409 | 48 |
| 19 | 775.5962 | 712.4771 | 727.0806 | 3 | 815 |
| 20 | 185.4654 | 171.5012 | 153.979 | 3 | 239 |
| 21 | 115.5157 | 107.0519 | 92.12647 | 3 | 170 |
| 22 | 37.90906 | 35.31268 | 27.50479 | 3 | 62 |
| 23 | 47.25644 | 43.97509 | 34.93428 | 3 | 70 |
| 24 | 50.56617 | 47.0403 | 37.59643 | 3 | 82 |
| 25 | 127.8651 | 118.441 | 102.8585 | 3 | 192 |
| 26 | 87.81213 | 81.48128 | 68.42088 | 3 | 117.6 |
| 27 | 82.58465 | 76.65239 | 64.01337 | 3 | 117.6 |
| 28 | 20.68617 | 19.32334 | 14.25653 | 3 | 31.2 |
| 29 | 27.23952 | 25.41264 | 19.21672 | 3 | 25.2 |
| 30 | 4.647672 | 4.371511 | 2.821779 | 3 | 8.4 |
| 31 | 8.082867 | 7.58319 | 5.14345 | 3 | 10.8 |
| 32 | 22.29692 | 20.82077 | 15.46477 | 3 | 36 |
| 33 | 270.6567 | 249.8417 | 232.0345 | 3 | 352.8 |
| 34 | 712.3336 | 654.62 | 662.9693 | 6.520409 | 324 |
| 35 | 439.3494 | 404.6549 | 392.4677 | 6.520409 | 360 |
| 36 | 439.3494 | 404.6549 | 392.4677 | 6.520409 | 215 |
| 37 | 439.3494 | 404.6549 | 392.4677 | 6.520409 | 360 |
| 38 | 45.79719 | 42.62334 | 33.76551 | 6.520409 | 48 |
| 39 | 115.0935 | 106.6625 | 91.76123 | 6.520409 | 60 |
| 40 | 110.8853 | 102.7803 | 88.12707 | 6.520409 | 60 |
| 41 | 15.36584 | 14.37324 | 10.32592 | 6.520409 | 24 |

Table 2. Analysis of effort estimation on Dataset 2

| 42 | 32.67584 | 30.45876 | 23.41075 | 6.520409 | 36 |
|----|----------|----------|----------|----------|-------|
| 43 | 64.52773 | 59.96081 | 48.98032 | 6.520409 | 72 |
| 44 | 64.52773 | 59.96081 | 48.98032 | 6.520409 | 48 |
| 45 | 20.04739 | 18.72936 | 13.77956 | 6.520409 | 72 |
| 46 | 1640.226 | 1501.541 | 1638.561 | 6.520409 | 2400 |
| 47 | 2089.383 | 1910.585 | 2130.591 | 6.520409 | 3240 |
| 48 | 1118.321 | 1025.576 | 1081.446 | 6.520409 | 2120 |
| 49 | 192.322 | 177.8117 | 160.1644 | 6.520409 | 370 |
| 50 | 444.5907 | 409.46 | 397.5498 | 10.26826 | 750 |
| 51 | 944.1499 | 866.5265 | 899.9904 | 6.520409 | 420 |
| 52 | 180.9169 | 167.3143 | 149.8864 | 10.26826 | 252 |
| 53 | 68.39128 | 63.53386 | 52.16987 | 6.520409 | 107 |
| 54 | 2450.814 | 2239.436 | 2533.23 | 10.26826 | 2300 |
| 55 | 331.7397 | 305.9395 | 289.3568 | 6.520409 | 400 |
| 56 | 1528.865 | 1400.05 | 1518.225 | 6.520409 | 973 |
| 57 | 1512.239 | 1384.895 | 1500.321 | 6.520409 | 1368 |
| 58 | 326.7409 | 301.3507 | 284.6296 | 10.26826 | 571.4 |
| 59 | 33.02077 | 30.7788 | 23.67897 | 10.26826 | 98.8 |
| 60 | 61.84511 | 57.47932 | 46.77514 | 10.26826 | 155 |





| Project Number | Hybrid BATGSA Optimization | IBAT Optimization | BAT Optimization | СОСОМО | Actual |
|-------------------|----------------------------------|----------------------|---------------------|--------|--------|
| 1 | 99.20243 | 93.56455 | 75.74521 | 3 | 117.6 |
| 2 | 93.74146 | 88.38874 | 71.37792 | 3 | 117.6 |
| 3 | 26.13845 | 24.48804 | 18.69947 | 3 | 31.2 |
| 4 | 28.0106 | 26.25112 | 20.10661 | 3 | 36 |
| 5 | 33.69317 | 31.6061 | 24.4048 | 3 | 25.2 |

Table 3. Analysis of effort estimation on Dataset 3

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| 6 | 6.592658 | 6.133727 | 4.409609 | 3 | 8.4 |
|----------|----------------------|----------|----------|----------------------|-------|
| 7 | 10.98438 | 10.24602 | 7.532536 | 3 | 10.8 |
| 8 | 280.2345 | 265.693 | 225.1002 | 3 | 352.8 |
| 9 | 25.39293 | 23.78613 | 18.14048 | 6.520409 | 72 |
| 10 | 74.65834 | 70.3147 | 56.21907 | 6.520409 | 72 |
| 11 | 19.86814 | 18.58797 | 14.02459 | 6.520409 | 24 |
| 12 | 438.1441 | 416.3439 | 359.7068 | 6.520409 | 360 |
| 12 | 39.85181 | 37.41485 | 29.10324 | 6.520409 | 36 |
| 13 | 438.1441 | 416.3439 | 359.7068 | 6.520409 | 215 |
| 15 | 74.65834 | 70.3147 | 56.21907 | 6.520409 | 48 |
| 16 | 438.1441 | 416.3439 | 359.7068 | 6.520409 | 360 |
| 10 | 684.2813 | 651.6947 | 574.1434 | 6.520409 | 324 |
| 17 | 123.0252 | 116.1592 | 94.92732 | 6.520409 | 60 |
| | | | | | 48 |
| 19 20 | 54.41322 127.3263 | 51.16594 | 40.34614 | 6.520409 6.520409 | 60 |
| | | | 98.41099 | | |
| 21 | 73.42792 | 69.15009 | 55.2477 | 3 | 60 |
| 22 | 280.2345 | 265.693 | 225.1002 | | 300 |
| 23 | 114.4643 | 108.0369 | 88.01115 | 3 | 120 |
| 24 | 54.41322 | 51.16594 | 40.34614 | 6.520409 | 90 |
| 25 | 151.2085 | 142.9179 | 117.8548 | 6.520409 | 210 |
| 26 | 34.84069 | 32.68804 | 25.27728 | 6.520409 | 48 |
| 27 | 56.01076 | 52.67581 | 41.5894 | 3 | 70 |
| 28 | 197.7336 | 187.1444 | 156.1494 | 3 | 239 |
| 29 | 59.6202 | 56.08796 | 44.4047 | 3 | 82 |
| 30 | 45.70538 | 42.94007 | 33.60213 | 3 | 62 |
| 31 | 127.7571 | 120.6499 | 98.76027 | 3 | 170 |
| 32 | 140.307 | 132.5641 | 108.9592 | 3 | 192 |
| 33 | 18.05542 | 16.88392 | 12.68562 | 3 | 18 |
| 34 | 36.37604 | 34.13594 | 26.44682 | 3 | 50 |
| 35 | 50.43812 | 47.40997 | 37.26043 | 3 | 60 |
| 36 | 21.69598 | 20.30703 | 15.38079 | 6.520409 | 42 |
| 37 | 46.49121 | 43.6821 | 34.20833 | 6.520409 | 60 |
| 38 | 390.2161 | 370.5845 | 318.552 | 6.520409 | 444 |
| 39 | 27.26034 | 25.54449 | 19.54213 | 6.520409 | 42 |
| 40 | 58.41479 | 54.94832 | 43.46355 | 6.520409 | 114 |
| 41 | 825.4542 | 786.8871 | 698.9662 | 3 | 1248 |
| 42 | 1477.063 | 1412.18 | 1286.772 | 6.520409 | 2400 |
| 43 | 1370.405 | 1309.713 | 1189.493 | 6.520409 | 1368 |
| 44 | 1384.298 | 1323.059 | 1202.144 | 6.520409 | 973 |
| 45 | 338.1075 | 320.866 | 274.0882 | 6.520409 | 400 |
| 46 | 2139.425 | 2049.264 | 1897.824 | 10.26826 | 2400 |
| 47 | 887.3909 | 846.238 | 754.0714 | 6.520409 | 420 |
| 48 | 193.2555 | 182.885 | 152.4424 | 10.26826 | 252 |
| 49 | 78.77285 | 74.20987 | 59.47296 | 6.520409 | 107 |

| 50 | 000 10 17 | 216 2006 | 270.0011 | 10.00000 | 671.4 |
|----|-----------|----------|----------|----------|--------|
| 50 | 333.4047 | 316.3806 | 270.0911 | 10.26826 | 571.4 |
| 51 | 40.23975 | 37.78091 | 29.40045 | 10.26826 | 98.8 |
| 52 | 71.79028 | 67.60018 | 53.95606 | 10.26826 | 155 |
| 53 | 442.964 | 420.9472 | 363.8582 | 10.26826 | 750 |
| 54 | 1037.398 | 990.0667 | 888.2906 | 6.520409 | 2120 |
| 55 | 204.468 | 193.5508 | 161.7318 | 6.520409 | 370 |
| 56 | 1079.141 | 1030.109 | 925.815 | 3 | 1181 |
| 57 | 296.004 | 280.7215 | 238.4036 | 3 | 278 |
| 58 | 2.467429 | 2.28434 | 1.573054 | 3 | 8.4 |
| 59 | 5388.899 | 5185.847 | 5000.907 | 10.26826 | 4560 |
| 60 | 1737.146 | 1662.194 | 1525.38 | 6.520409 | 720 |
| 61 | 296.004 | 280.7215 | 238.4036 | 6.520409 | 458 |
| 62 | 1311.233 | 1252.883 | 1135.682 | 6.520409 | 2460 |
| 63 | 390.2161 | 370.5845 | 318.552 | 6.520409 | 162 |
| 64 | 159.9815 | 151.2528 | 125.0365 | 6.520409 | 150 |
| 65 | 619.3632 | 589.5723 | 517.151 | 6.520409 | 636 |
| 66 | 684.2813 | 651.6947 | 574.1434 | 6.520409 | 882 |
| 67 | 1677.211 | 1604.562 | 1470.228 | 6.520409 | 444 |
| 68 | 1147.283 | 1095.493 | 987.223 | 6.520409 | 192 |
| 69 | 654.2464 | 622.9494 | 547.741 | 3 | 576 |
| 70 | 689.2988 | 656.4974 | 578.5597 | 3 | 432 |
| 71 | 133.8024 | 126.3883 | 103.6672 | 3 | 72 |
| 72 | 428.5187 | 407.1519 | 351.4232 | 3 | 300 |
| 73 | 366.4468 | 347.901 | 298.2313 | 3 | 300 |
| 74 | 74.65834 | 70.3147 | 56.21907 | 3 | 240 |
| 75 | 491.4179 | 467.2367 | 405.7102 | 3 | 600 |
| 76 | 744.7064 | 709.5443 | 627.4299 | 3 | 756 |
| 77 | 1748.063 | 1672.694 | 1535.436 | 3 | 1200 |
| 78 | 759.8837 | 724.0786 | 640.8482 | 3 | 97 |
| 79 | 249.8547 | 236.7529 | 199.5761 | 10.26826 | 409 |
| 80 | 438.1441 | 416.3439 | 359.7068 | 10.26826 | 703 |
| 81 | 125.1741 | 118.1984 | 96.66707 | 10.26826 | 1350 |
| 82 | 217.9967 | 206.4237 | 172.9731 | 6.520409 | 480 |
| 83 | 164.3846 | 155.4368 | 128.6483 | 6.520409 | 599 |
| 84 | 91.23059 | 86.0095 | 69.37403 | 6.520409 | 430 |
| 85 | 759.8837 | 724.0786 | 640.8482 | 10.26826 | 4178.2 |
| 86 | 272.8409 | 258.6483 | 218.8754 | 10.26826 | 1772.5 |
| 87 | 296.004 | 280.7215 | 238.4036 | 10.26826 | 1645.9 |
| 88 | 204.468 | 193.5508 | 161.7318 | 10.26826 | 1924.5 |
| 89 | 24.46381 | 22.9115 | 17.44494 | 10.26826 | 648 |
| 90 | 1110.544 | 1060.239 | 954.092 | 10.26826 | 8211 |
| 91 | 59.6202 | 56.08796 | 44.4047 | 10.26826 | 480 |
| 92 | 20.59753 | 19.27386 | 14.56507 | 10.26826 | 12 |
| | - | - | - | - | + |

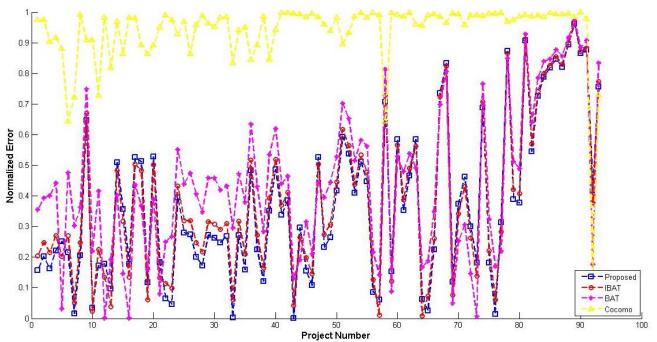


Figure. 3 Analysis of normalized error on Dataset 3

| Project Number | Hybrid BATGSA Optimization | IBAT Optimization | BAT Optimization | СОСОМО | Actual |
|-------------------|----------------------------------|----------------------|---------------------|----------|---------|
| 1 | 2617.821 | 4759.931 | 5605.14 | 8564.197 | 287 |
| 2 | 1102.3 | 1961.087 | 2138.508 | 3213.793 | 82.5 |
| 3 | 6374.61 | 11853.65 | 15106.91 | 17526.39 | 1107.31 |
| 4 | 2255.341 | 4085.472 | 4747.639 | 5266.707 | 86.9 |
| 5 | 4273.649 | 7867.239 | 9676.503 | 9519.336 | 336.3 |
| 6 | 981.854 | 1741.718 | 1879.869 | 2610.139 | 84 |
| 7 | 203.2856 | 346.5822 | 325.2334 | 520.7564 | 23.2 |
| 8 | 2583.915 | 4696.738 | 5524.325 | 6818.744 | 130.3 |
| 9 | 4188.328 | 7706.258 | 9461.534 | 11576.37 | 116 |
| 10 | 570.9059 | 998.9934 | 1027.525 | 1389.818 | 72 |
| 11 | 4332.574 | 7978.464 | 9825.252 | 11723.8 | 258.7 |
| 12 | 1820.726 | 3280.442 | 3740.319 | 5270.448 | 230.7 |
| 13 | 1768.673 | 3184.33 | 3621.389 | 4542.2 | 157 |
| 14 | 3664.985 | 6720.702 | 8154.226 | 9598.281 | 246.9 |
| 15 | 2521.852 | 4581.12 | 5376.708 | 7214.489 | 69.9 |

 Table 4. Analysis of effort estimation on Dataset 4

6. Conclusion

This paper implements the hybrid BATGSA algorithm to optimize the performance of the COCOMO model to estimate the software cost. The algorithm has been analyzed on 4 datasets including two datasets of NASA projects downloaded from promise repository. The comparison of effort valueand normalized error on each dataset has been done with the Improved BAT, BAT and COCOMO model. The normalized error has been reduced by 1% on dataset1, 3.5% on dataset2, 0.33% on dataset3 and 46% on dataset4 by BATGSA algorithm as compared to the improved BAT algorithm. The reduction in the normalized error and the convergence of efforts towards the actual effort of

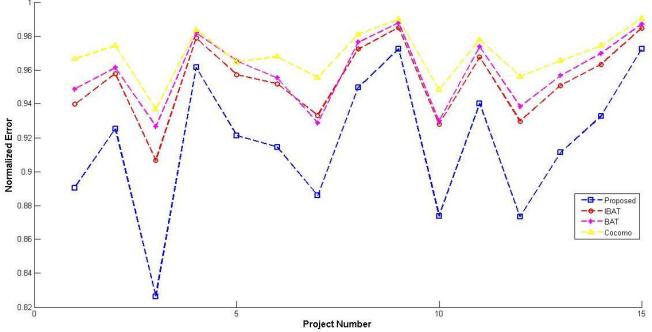


Figure. 4 Analysis of normalized error on Dataset 4

the hybrid BATGSA algorithm as compared to other state of art algorithms proves the significance of the algorithm. In future this algorithm can be applied to optimize different software metrics. Moreover, algorithm can be modified to determine the software quality during the development of software.

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