



## Modified Artificial Bee Colony Optimization Technique with Different Objective Function of Constraints Optimal Power Flow

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**Abstract:** Artificial Bee Colony (ABC) simulates the behaviour of intelligent foraging for a honeybee swarm. This article deals with one of the best swarm-based algorithms that has been used to solve the Optimal Power Flow (OPF) problem. Minimization of the objecting function can be satisfied by choosing a suitable optimal control variable while maintaining an acceptable system performance of the state variables in terms of their limits. The control variables that used in this article are the magnitude voltage of the generator, the tap changer of the transformer, the injection reactive power of compensative devise and the active power of the generator except the slack generator. The state variables are the reactive power of the generator, the load bus voltage and slack generator active power. The proposed algorithm modifies the classical Artificial bee colony by replacing the worst solutions obtained from the employee bees' phase and the onlooker bees' phase by the best solutions in the swarm size. The percentage of swarm sources that have been selected for the worst solutions is 33%, 50%, and randomly selection from the total source of the swarm size. This update contributes to improve the quality of solutions and determine the optimal settings of OPF control variables. The propose algorithm deals with minimization four different objective functions, the total fuel cost of the thermal units, the total active power losses in the transmission lines, the total emission caused by fossil-fueled thermal units and the total voltage deviation at the load buses. The modified ABC reduced the fuel cost by 11.34%, active power losses by 49.26%, voltage deviation by 91.34% and the emission by 16.70% satisfying all the constraint of the state variables in their limits. The proposed algorithm has been applied on the IEEE 30 bus system and gives good result when compare with other optimization techniques.

**Keywords:** Artificial bee colony, Optimal power flow, Fuel cost minimization, Active power losses minimization, Emission minimization, Voltage deviation minimization.

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### 1. Introduction

One of the most common problems in operating and planning of power system is the Optimal Power Flow (OPF). It was presented by Dommel and Tinney [1]. In the recent years, the optimal power flow problem as usual abundant attention because of its ability to find the optimal solutions to consider the system security [2]. Finding the optimal power system control variables is the main goal of OPF problem to minimize a certain objective function that's sufficient from several equality and inequality constraints. Real power generation levels, voltage magnitude of the generator, tap changer of the transformer and shunt capacitor outputs are the most

important control variables of the power system that has been composed. There are two type of optimization techniques that used to solve the OPF problem, the first one is the classical algorithm and second is the modern or artificial intelligence algorithm. To solve the OPF problem and to overcome the limitations of classical optimization techniques, created an evolutionary optimization technique. Many of heuristic optimization techniques was applied such as Simulated Annealing (SA) [3], Genetic Algorithm (GA) [4, 5], Particle Swarm Optimization (PSO) [6], Tabu Search [7], Moth-Flame Optimizer (MFO) [8], Ant Lion [9], and Differential Evolution algorithm(DE) [10]. The results reported in the literature were promising and encouraging for further research in this direction.

Artificial Bee Colony (ABC) algorithm is one of the recently heuristic optimization algorithms based on the intelligent behavior of honeybees. It was presented by Karaboga in 2005 [11]. Three phases are involved for each cycle: employed bees phase, onlooker bees phase, and scout bees phase [12–15]. In benchmark problems, ABC is faster and more efficient than heuristic algorithms as have shown Comparative studies. As a result of its features, ABC algorithm have been effectively used in many power system problems such as optimal reactive power dispatch [16], Enhancing system loadability with multiple FACTS devices [17], Optimal location of UPFC to improve power system voltage stability [18], Optimal power flow in UPFC [19], Economic Dispatch in  $n$  power generation [20] and so on.

The formulation and objectives are varied in the OPF problem. So, no optimal algorithm produces for the best solutions for all OPF problems, and therefore there is a continuous need to create a new algorithm to solve the OPF problem with more efficiency.

The goal of using the ABC algorithm is simplicity, robustness, fewer parameters such as crossover rate and mutation rate in case GA and DE, the convergency is faster, the combination is easier and both exploration and exploitation.

Various methods that used to improve the ABC algorithm have been approached. In [21, 22], the ABC algorithm was improved by replacing two types of search operations, mutation and crossover of the DE algorithm. M. Chen proposed an improved artificial bee colony algorithm based on escaped foraging strategy [23].

In this article, the improvement of Artificial Bee Colony ABC is based on replacing the worst swarms by the best swarms in honeybee at each phase (employed bees and onlooker bees). This technique is used to solve the Optimal Power Flow OPF problem with various objective functions such as the total generation fuel costs, the total active power losses, the total amount of emission caused by the fossil-fueled thermal units and the voltage profile improvement. Several runs are carried out on the standard IEEE 30-bus test system.

The rest of the article is organized as follows: Section 2 present the notation list of the variables that used in this article. Section 3 describes the mathematical problem formulation with different objective functions. Section 4 present the Artificial Bee Colony (ABC) algorithm in details. Section 5 explain the modified artificial bee colony. Simulation result and comparison with other optimization techniques are given in section 6. In the last section, the conclusions are drawn from this article.

## 2. Nomenclature and abbreviations

The following notations will used in this paper.

$x^T$	vector of state variables.
$u^T$	vector of control variables.
$N_L$	number of load buses.
$N_G$	number of generating units.
$N_t$	number of regulating transformers.
$N_c$	number of shunt compensators.
$ V_L $	magnitude voltage of the load bus.
$Q_G$	reactive power of the generators.
$P_{Gs}$	active power of the slack generator.
$P_G$	active power of the generator.
$T$	tap changer of the transformer.
$Q_C$	reactive power of shunt injection compensator.
$C_{Gi}$	total fuel cost of thermal generator $i$ .
$a_i, b_i, c_i$	fuel cost coefficients of the $i^{th}$ generator.
$P_{Gi}$	active power of $i^{th}$ generator.
$N_G$	number of generators with the slack bus.
$P_{loss}$	active power losses.
$g_{(i,j)}$	line mutual conductance between buses $i,j$ .
$V_i, V_j$	magnitude voltages of the buses $i,j$ .
$\delta_i, \delta_j$	phase angles of the voltages $V_i$ and $V_j$ .
$V_d$	total voltage deviation at the load buses.
$V_i$	per unit voltage at load bus $i$ .
$N_L$	number of load buses.
$E_{Gi}$	total emission cost (ton/h) of unit $i$ .
$\alpha_i, \beta_i, \gamma_i$	emission coefficients of the $i^{th}$ unit.
$N_B$	total number of buses except slack bus.
$N_L$	total number of load buses.
$P_i$	active power injection into $i^{th}$ bus.
$Q_i$	reactive power injection into $i^{th}$ bus.
$P_{Gi}$	active generated at bus $i$ .
$Q_{Gi}$	reactive power generated at bus $i$ .
$P_{di}$	load active power at bus $i$ .
$Q_{di}$	load reactive power at bus $i$ .
$G_{ij}, B_{ij}$	line transfer conductance and susceptance of buses $i,j$ respectively.
$V_{Gi}^{min}$	min. voltage limit of generator $i$ .
$V_{Gi}^{max}$	max. voltage limit of generator $i$ .
$T_{Ti}^{min}$	min. tap changer limit of transformer $i$ .
$T_{Ti}^{max}$	max. tap changer limit of transformer $i$ .
$Q_{Ci}^{min}$	min. reactive power compensative devise at load bus $i$ .
$Q_{Ci}^{max}$	max. reactive power compensative devise at load bus $i$ .
$P_{Gi}^{min}$	min. active power limit of generator $i$ except the slack generator.
$P_{Gi}^{max}$	max. active power limit of generator $i$ except the slack generator.
$V_{Li}^{min}$	min. voltage of the load bus $i$ .
$V_{Li}^{max}$	max. voltage of the load bus $i$ .

$Q_{Gi}^{min}$	min. reactive power of generator $i$ .
$Q_{Gi}^{max}$	max. reactive power of generator $i$ .
$P_{Gs}^{min}$	min. active power of slack generator.
$P_{Gs}^{max}$	max. active power of slack generator.
$rand$	randomly number between $[0, 1]$ .
$x_{i,k}$	randomly chosen solution different $x_{i,j}$ .
$\emptyset_{i,j}$	random number between $[0, 1]$ .
$v_{i,j}$	new solution (food source).
$p_i$	probability value.
$fit_i$	fitness value.
$f_i$	normalized value.

### 3. Problem formulation

The Optimal Power Flow (OPF) can be mathematically formulated as a nonlinear optimization problem. Generally, the OPF problem can be mathematically expressed as follows:

$$\text{Minimize } f(x, u) \quad (1)$$

$$\text{subjected to } g(x, u) = 0 \quad (2)$$

$$h(x, u) \leq 0 \quad (3)$$

where  $f$  is the objective function;  
 $g$  is the equality constraints of the load flow analysis;  
 $h$  is the constraints of system operating.

The two vectors  $x$  and  $u$  are expressed in Eqs. (4) and (5) respectively.

$$x^T = [ |V_{L1}|, \dots, |V_{LN_L}|, Q_{G1} \dots Q_{GN_G}, P_{Gs} ] \quad (4)$$

$$u^T = [ P_{G2}, \dots, P_{GN_G}, |V_{G1}|, \dots, |V_{GN_G}|, T_1, \dots, T_{N_t}, Q_{C1}, \dots, Q_{CN_C} ] \quad (5)$$

The generators active powers (except slack bus) and generators bus voltages are continuous variables, whereas the tap changing transformers settings and the reactive power injection MVar of the shunt capacitors are discrete variables.

### 3.1 Objective functions

Four objective functions in this article are considered separately for each one to demonstrate the efficiency of the proposed algorithm.

#### 3.1.1. Fuel cost minimization

The total fuel cost objective function of the thermal units can be expressed by:

$$C_{Gi} = \sum_{i=1}^{N_G} a_i P_{Gi}^2 + b_i P_{Gi} + c_i \quad (6)$$

where  $a_i, b_i, c_i$  are the fuel cost coefficients of the  $i^{th}$  generator;

#### 3.1.2. The active power losses

The active power losses of the transmission line can be expressed as:

$$P_{loss} = \sum_{k=1}^N g_{(i,j)} (V_i^2 + V_j^2 - 2V_i V_j \cos \delta_{ij}) \quad (7)$$

where  $\delta_{ij} = \delta_i - \delta_j$ ;

#### 3.1.3. Minimization of emission

Due to fossil-fueled thermal units, the atmospheric pollutants product two types of emission gasses, Sulphur oxides  $SO_x$  and Nitrogen oxides  $NO_x$ . However, the total emission cost is defined as bellow [24]:

$$E_{Gi} = \sum_{i=1}^{N_G} 10^{-2} (\alpha_i + \beta_i P_{Gi} + \gamma_i P_{Gi}^2) + \zeta_i \exp(\lambda_i P_{Gi}) \quad (8)$$

where  $E_{Gi}$  is the total emission cost (ton/h) and  $\alpha_i, \beta_i, \gamma_i$ , are the emission coefficients of the  $i$ th unit.

#### 3.1.4. The voltage profile improvement

The voltage profile improvement at load buses can be realized by minimizing the load bus voltage deviation from 1.0 per unit. The load bus voltage deviation can be expressed as:

$$V_d = \sum_{i=1}^{N_L} |V_i| - 1 \quad (9)$$

where  $V_d$  is the total voltage deviation at the load buses;  $V_i$  the per unit voltage at load bus  $i$  and  $N_L$  is the number of load buses [25].

### 3.2 Objective constraints

The objective functions optimization is determined to a number of equality and inequality constraints

### 3.2.1. Equality constraints

The equality constraints represent the equations:

- *Active power balance constraints*

$$\sum_{i=1}^{N_B} P_i = P_{Gi} - P_{di} = V_i \sum_{j=1}^{N_B} V_j [G_{ij} \cos \theta_{ij} + G_{ij} \cos \theta_{ij}] \quad (10)$$

- *Reactive power balance constraints*

$$\sum_{i=1}^{N_L} P_i = P_{Gi} - P_{di} = V_i \sum_{j=1}^{N_L} V_j [G_{ij} \sin \theta_{ij} + G_{ij} \sin \theta_{ij}] \quad (11)$$

where  $\theta_{ij} = \theta_i - \theta_j$ ;

### 3.2.2. Inequality constraints

These constraints have two type

$$V_{Gi}^{min} \leq V_{Gi} \leq V_{Gi}^{max} \quad i = 1, 2, \dots, N_L \quad (12)$$

$$T_i^{min} \leq T_i \leq T_i^{max} \quad i = 1, 2, \dots, N_T \quad (13)$$

$$Q_{Ci}^{min} \leq Q_{Ci} \leq Q_{Ci}^{max} \quad i = 1, 2, \dots, N_C \quad (14)$$

$$P_{Gi}^{min} \leq P_{Gi} \leq P_{Gi}^{max} \quad i = 1, 2, \dots, N_G - 1 \quad (15)$$

- *The inequality constraints on state variable*

$$V_{Li}^{min} \leq V_{Li} \leq V_{Li}^{max} \quad i = 1, 2, \dots, N_L \quad (16)$$

$$Q_{Gi}^{min} \leq Q_{Gi} \leq Q_{Gi}^{max} \quad i = 1, 2, \dots, N_G \quad (17)$$

$$P_{Gs}^{min} \leq P_{Gs} \leq P_{Gs}^{max} \quad (18)$$

## 4. Artificial bee colony (ABC) algorithm

Artificial bee colony is presented by Karaboga for numerical optimization [11]. It simulates the behavior of intelligent foraging for honeybee swarms. It is a robust, simple and population based stochastic optimization algorithm. The food source refers to a

probable solution and the nectar amount of a food source represents the quality (fitness) of the related solution of the problem to be optimized. The number of solutions is equal to the number of employed bees or the onlooker bees.

In the first step, the ABC algorithm produces initial population with randomly distributed in the range of variables (employed bees or onlooker bees)  $x_i$  ( $i = 1, 2, \dots, SN$ ) is a D-dimensional vector, where SN denotes the size of employed bees or onlooker bees. Eq. (19) used to find a new source by using the following expression:

$$x_{i,j} = x_{j,min} + rand[0,1] \times (x_{j,max} - x_{j,min}) \quad (19)$$

where  $x_{j,min}$  and  $x_{j,max}$  are the minimum and maximum limits of variables to be optimized, and *rand* denotes a randomly number between [0, 1].

Secondly, the population of the positions (solutions) is subjected to repeated cycles,  $Y = 1, 2, \dots, MCN$ , of the search processes of the employed, onlooker and the scout bees. Employed bees have many of modification on the position in her memory. It will be produced according to the local information and the nectar amount (fitness value) of the new source. If the new nectar amount has equal or better than that of the previous one, it replaces the previous one in her memory. Otherwise, the old one is retained in her memory. Each employed bee identifies new sources whose amounts are equal to the half of the total sources. In order to produce a new food source from the old one saved in the memory; the following expression is used:

$$v_{i,j} = x_{i,j} + \phi_{i,j} \times (x_{i,j} - x_{i,k}) \quad (20)$$

In Eq. (20),  $k \in \{1, \dots, SN\}$  and  $j \in \{1, \dots, D\}$  are randomly chosen indexes, where, D is the number of optimization parameters; SN denotes the size of employed bees or onlooker bees;  $x_{i,k}$  is a randomly chosen solution different from  $x_{i,j}$ ,  $\phi_{i,j}$  is a random number between [0, 1] and  $v_{i,j}$  denoted the new solution (food source).

In the third step, all food source information will share between employed bees and onlooker bees and select a food source depending on the probability given in Eq. (21)

$$p_i = \frac{fit_i}{\sum_{n=1}^{SN} fit_i} \quad (21)$$

where  $p_i$  and  $fit_i$  are the probability and the fitness value associated with of the solution  $i$ . If the

nectar amount is equal or better than that of the old one, it keeps the new one and abandoned the old one. For simplifying problem, the following expression are used to calculate  $fit_i$  :

$$fit_i = \begin{cases} \frac{1}{1 + f_i} & \text{if } f_i \geq 0 \\ \frac{1}{1 - f_i} & \text{if } f_i < 0 \end{cases} \quad (22)$$

where  $f_i$  represents the normalized value for the objective function. Finally, the scout bees are mainly responsible for a new food source randomly in each colony. They are chosen from the employed bees with taking into consideration the limit parameters. The employed bee will be a scout when the food source is not improved by the predetermined number of trials. The number of incomings and outgoings to a source is an important control parameter and which is called “limit “. The expression which identifies a scout bee is given in Eq. (19).

### 5. Modified artificial bee colony

To achieve optimal optimization performance, the ability of exploration and exploitation must be well balanced. In the ABC algorithm, the onlooker carries out the exploitation process and the exploration process are accomplished by employed and scout bees. This algorithm is modified by determining the best solutions (minimum objective function) and the worst solutions (maximum objective function) in descending order, then delete the worst solutions and replaced by the best solutions for each phase (the employed bee and onlooker bee) at each iteration according to three types of swarm source shown below as followed :

- 1- Type 1: the percentage of the worst solutions of employed bees and onlooker bees is 33% and 67% respectively.
- 2- Type 2: the percentages of the worst solutions of employed bees and the onlooker bee are 50%.
- 3- Type 3: randomly choosing to determine the worst solutions for both bees.

To demonstrate the effectiveness and strength of this technique, the three types of swarm source are used to minimize different objective function depending on the percentage that have been selected from the worst solutions and replacing them with the best solutions in the employee bees phase and the onlooker bees phase in the swarm size.

Fig. 1 illustrates the flow chart of proposed MABC algorithm.

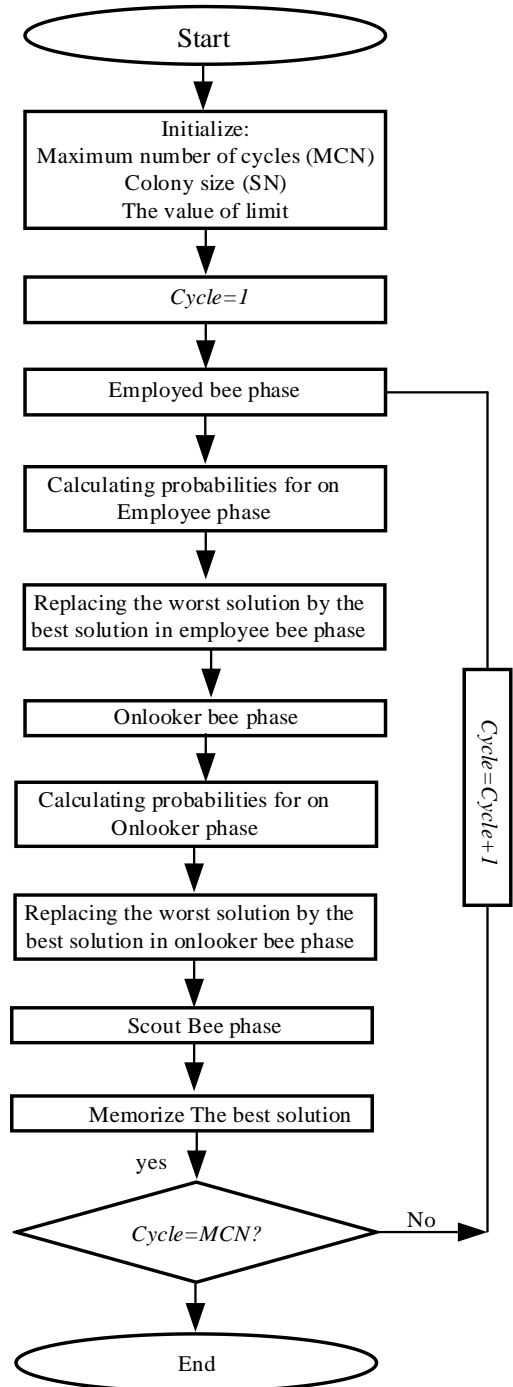


Figure. 1 Flowchart of proposed MABC algorithm

### 6. Simulation result

Applying the artificial bees algorithm to solve the OPF problem was carried out on the IEEE-30 bus systems and compared its simulation results with those of GA, PSO, DE, ABC, TSA, SCA, SFLA and JA [5, 10, 16, 25-40]. The generation cost and emission coefficients of IEEE-30 bus system given in Table 1 and Table 2 respectively. The system contains 6 generation stations with 4 transformers and 41 transmission lines as shown in Fig. 2 [28].

Table 1. Generation cost coefficients for IEEE30 bus

Bus No.	Cost coefficients		
	<i>a</i>	<i>B</i>	<i>C</i>
1	0	2	3.7ee-3
2	0	1.75	1.75e-2
5	0	1	6.25E-2
8	0	3.25	8.3E-3
11	0	3	2.5E-2
13	0	3	2.5E-2

Table 2. Generation emission coefficients for IEEE30 bus

Bus No.	Emission coefficients				
	<i>α</i>	<i>β</i>	<i>γ</i>	<i>ζ</i>	<i>λ</i>
1	4.091	-5.554	6.490	2.0e-4	2.857
2	2.543	-6.047	5.638	5.0e-4	3.33
5	4.258	-5.094	4.586	1.0e-6	8.0
8	5.326	-3.550	3.380	2.0e-3	2.0
11	4.258	-5.094	4.586	1.0e-6	8.0
13	6.131	-5.555	5.151	1.0e-5	6.67

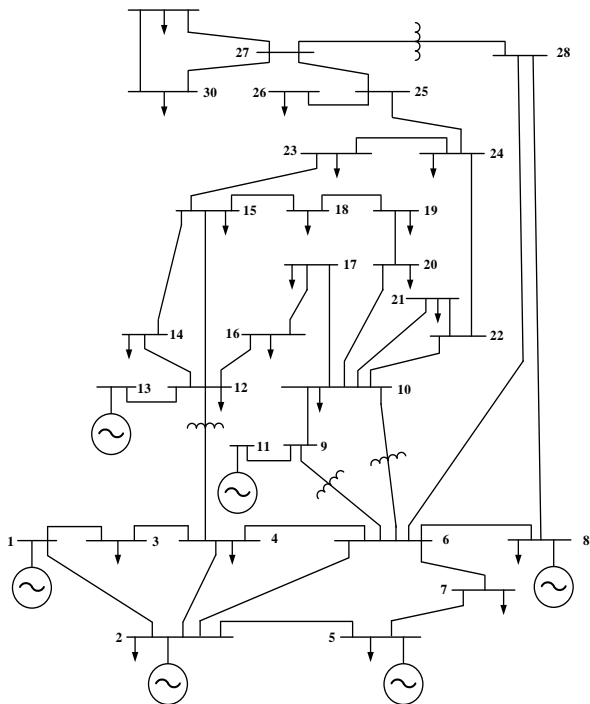


Figure. 2 Single-line diagram of IEEE 30-bus test system

Table 3. Comparison of proportional the swarm source

Types	Objective Function			
	Fuel cost (\$/h)	Active losses (MW)	Emission (ton/h)	Voltage deviation (pu)
Type 1	799.58	2.8864	0.2048	0.1069
Type 2	799.38	2.8969	0.2048	0.1017
Type 3	799.40	2.8894	0.2048	0.1197

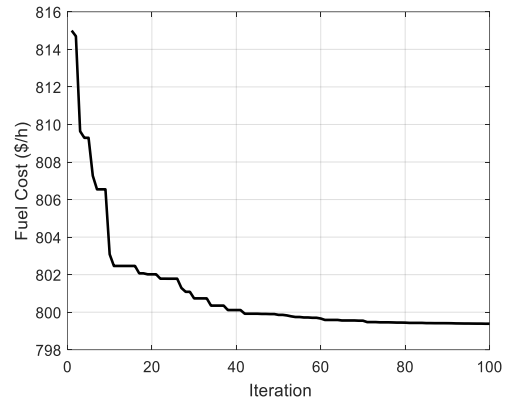


Figure. 3 The convergence plot for fuel cost function

### 6.1 Case 1: Fuel cost minimization

The objective function is to minimize the fuel cost  $C_G$  that defined in Eq. (6). The minimum fuel cost obtained from the modified ABC approach based on the three types of swarm source type 1, type 2 and type 3 was 799.5893 \$/h, 799.3862 \$/h and 799.4071 \$/h respectively as shown in Table 3. Fig. 3 shows the fast convergence to the optimal solution based on type 2 (the best one). Table 4 illustrate control variables of OPF for the best solution. The fuel cost is reduced from the initial value 901.6391 \$/h to optimal value 799.386 \$/h with reduction equal to 11.34%.

### 6.2 Case 2: Active power losses minimization

In this case, the objective function is to minimize the active power losses  $P_{loss}$  that defined in equation (7). According to the three types of the swarm source of the modified ABC type 1, 2 and 3, the minimum active power losses was 2.8864 MW, 2.8969 MW and 2.8894 MW respectively as shown in Table 3. The best solution is given in type 1. Fig. 4 shows the convergence of the minimum active power losses based on type 1 (the best one). The total active power losses are reduced by up to 49.26% compared to the initial active power losses 5.6891 MW as shown in Table 4 where the optimal active power losses for the best type of the swarm source was 2.8864 MW.

### 6.3 Case 3: Emission cost minimization

The total emission minimization of the generators  $E_G$  is defined in Eq. (8). All the three types of swarm source are equally for the best solution as shown in Table 3. The total emission reduced from the initial value 0.239 ton/h to the optimal value 0.2048 ton/h with reduction ratio of 16.7% as given in Table 4. Fig. 5 illustrates the convergence characteristic of the

Table 4. Control variables and result simulation for the best objective functions

Control variables		Limit		Initial	Fuel cost	Active power losses	Voltage deviation	Emission
		Max	Min					
Generator active power (MW)	$P_2$	20	80	80	48.7538	79.9959	33.7391	67.1785
	$P_5$	15	50	50	21.1924	49.994	38.424	49.9998
	$P_8$	10	35	20	21.4388	34.9975	33.6407	34.9997
	$P_{11}$	10	30	20	11.6952	29.9994	29.1491	29.9991
	$P_{13}$	12	40	20	12.0059	39.9997	13.0961	39.9997
Generator Voltage (pu)	$V_1$	0.95	1.1	1.05	1.1	1.0998	1.0188	1.1
	$V_2$	0.95	1.1	1.04	1.0871	1.0969	1.0122	1.0973
	$V_5$	0.95	1.1	1.01	1.0612	1.0773	1.0178	1.0817
	$V_8$	0.95	1.1	1.01	1.0679	1.0855	1.0113	1.0872
	$V_{11}$	0.95	1.1	1.05	1.0996	1.0999	1.0387	1.0989
	$V_{13}$	0.95	1.1	1.05	1.0991	1.1	0.9972	1.0999
Tap Position	$T_{11}$	0.9	1.1	1.078	1.0467	0.9994	0.9532	1.0239
	$T_{12}$	0.9	1.1	1.069	0.9507	1.0232	1.0219	1.0687
	$T_{15}$	0.9	1.1	1.032	1.0988	0.9511	0.9509	0.952
	$T_{36}$	0.9	1.1	1.068	0.9841	0.9822	0.9694	0.9953
Shunt Element (MVar)	$Q_{c10}$	0	5	0	4.9657	4.9375	4.7634	4.4083
	$Q_{c12}$	0	5	0	4.8689	4.9835	2.997	0.0769
	$Q_{c15}$	0	5	0	4.5424	4.6936	4.7707	4.8999
	$Q_{17}$	0	5	0	4.9925	4.9693	0.3197	4.6113
	$Q_{c20}$	0	5	0	4.6231	4.8142	4.937	4.4519
	$Q_{21}$	0	5	0	4.5904	4.9863	4.9909	4.8163
	$Q_{c23}$	0	5	0	4.6889	4.1282	4.9569	4.9561
	$Q_{24}$	0	5	0	4.9371	4.9918	4.9175	4.9868
	$Q_{29}$	0	5	0	2.8721	3.1465	2.9494	2.3209
<b>Fuel cost (\$/h)</b>				901.6391	<b>799.386</b>	967.1569	840.989	943.3064
<b>Power losses (MW)</b>				5.6891	8.6928	<b>2.8864</b>	6.8492	3.0385
<b>Voltage deviation</b>				1.1747	1.4212	0.1499	<b>0.1017</b>	1.6315
<b>Emission</b>				0.239	0.3661	0.2072	0.2833	<b>0.2048</b>
<b>Reduction ratio</b>				-	11.34%	49.26%	91.34%	16.70%
<b>Slack generator active power <math>P_{Gs}</math></b>		<b>20</b>	<b>200</b>	99.23	177.0267	51.3197	142.2207	64.2819

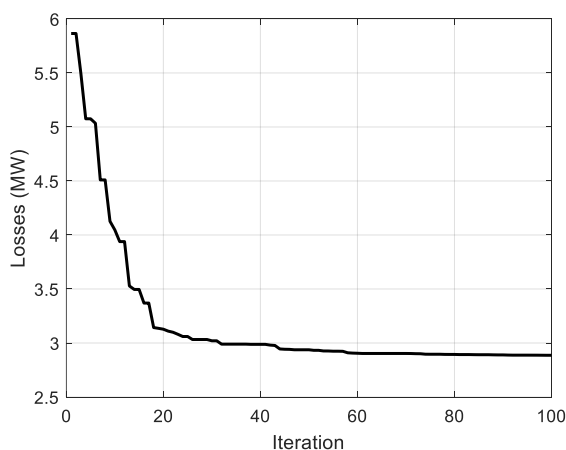


Figure. 4 The convergence plot for power losses function

ABC algorithm to the global optimal solution for the system after 100 iterations.

#### 6.4 Case 4: Voltage profile improvement

In this case, the objective function that taken into consideration is the voltage profile improvement  $V_d$  which can be achieved by minimization the load bus voltage deviations from 1.0 per unit. This objective function can be expressed as in Eq. (9). The best solution of the system voltage profile was 0.1017 p.u based on type 2 of the swarm source as shown in Table 3. Fig. 6 shows the convergence characteristic curve of the system voltage profile based on type 2 of the proposed ABC algorithm. The voltage profile is greatly improved compared with the other pervious objective function, where the total voltage deviations is reduced from the initial value 1.1747 pu to the optimal value 0.1017 pu with a reduction of 91.34% as given in Table 4.

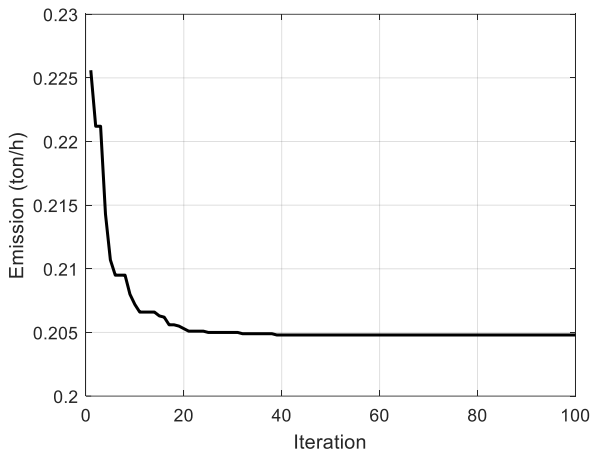


Figure. 5 The Convergence plot for emission function

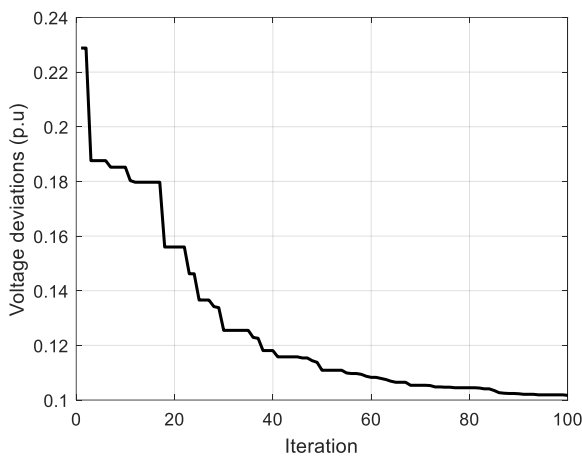


Figure. 6 The Convergence plot for voltage deviation function

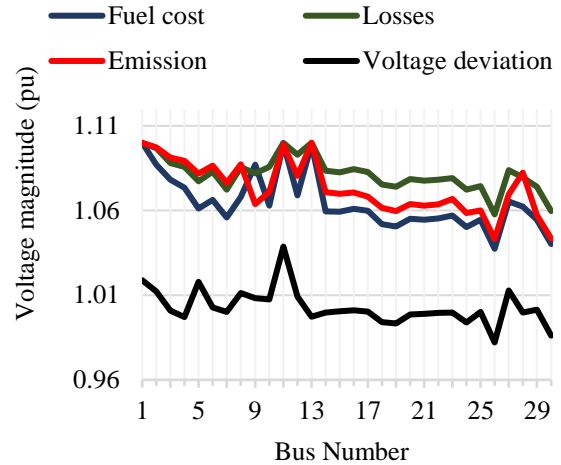


Figure. 7 System voltage profile

The optimal control variables for the best objective function based on the modified ABC are given in Table 4.

Table 5 illustrate the results of comparison among the proposed modified ABC algorithm with the other optimization techniques.

The propose algorithm satisfied the constraint OPF by finding the optimal control variables for best objective functions keeping the state variables of the active power of the slack generator, load voltages and the reactive power of the generators in their maximum and minimum limits as shown in Table 4, Table 6 and Fig. 7 respectively.

Table 5. Comparisons of the results obtained using different optimization techniques

Methods	Fuel cost (\$/h)	Active power losses (MW)	Emission (ton/h)	Voltage profile (pu)
Initial	901.6391	5.830	0.3661	1.1747
IGA [32]	800.805	NA	NA	NA
Gradient [30]	804.853	NA	NA	NA
EGA [34]	NA	3.2008	NA	NA
DE [27]	800.56	3.240	NA	NA
DE [35]	799.365	2.9748	NA	NA
MSLFA [33]	NA	NA	0.2056	NA
PSO [26]	801.66	3.032	NA	NA
SLFA [33]	NA	NA	0.2063	NA
ABC [31]	800.6600	3.1078	0.204826	NA
MSCA [36]	NA	2.9334	NA	0.1031
IABC [37]	NA	3.084	NA	NA
GA [33]	NA	NA	0.21170	NA
Hybrid PSO and GSA [38]	NA	NA	NA	0.12674
Jaya [39]	NA	NA	NA	0.1273
(EGA-DQLF) [40]	NA	NA	NA	0.111
Proposed algorithm ABC	<b>799.3862</b>	<b>2.8864</b>	<b>0.2048</b>	<b>0.1017</b>



Table 6. The state variable of reactive power of the generators of OPF based on modified ABC technique

Unit number	$Q_{G_i}$ (min) (MVar)	$Q_{G_i}$ (max) (MVar)	$Q_{G_i}$ (MVar) for fuel cost	$Q_{G_i}$ (MVar) for active power losses	$Q_{G_i}$ (MVar) for voltage deviation	$Q_{G_i}$ (MVar) for Emission
1	-20	200	-9.939	-3.3563	-17.0454	-7.83
2	-20	100	30.8858	18.5594	20.5652	19.1057
5	-15	80	32.6568	25.5385	54.557	28.1862
8	-15	60	39.8395	35.3486	55.2374	32.932
11	-10	50	7.0163	15.0023	16.641	19.9798
13	-15	60	23.7225	9.6671	-8.3773	16.2358

## 5. Conclusions

This article presented a modifying for the classical Artificial Bee Colony (ABC) to solving Optimal Power Flow problem (OPF). The proposed algorithm demonstrates the robustness, flexibility, effectiveness and successfully applied to solve OPF. To show the effectiveness of this approach, the objective function of fuel cost, active power losses, emission, and voltage deviation have been applied and tested using the IEEE 30-bus system. The modified ABC based on determining the worst solutions for each phase (employed bee phase and onlooker bee phase) then replace its by the best solutions at each iteration to improve the quality of solutions and select the optimal control variables for the best different objective function. The worst solutions that chosen in this algorithm is 33%, 50%, and random selection from the total swarm source. The proposed approach has fast convergence and quality solution when compare with other methods in the literature. The performance of ABC algorithm indicating its effectiveness for solving OPF problems, especially for large systems.

## Conflicts of Interest

The authors identify and declare that there is no any personal circumstances or interest that may be perceived as inappropriately influencing the representation or interpretation of reported research results.

## Author Contributions

Conceptualization, Layeth Al-Bahrani and Murtadha Al-Kaabi; methodology, Layeth Al-Bahrani and Murtadha Al-Kaabi; software, Layeth Al-Bahrani and Murtadha Al-Kaabi; validation, Murtadha Al-Kaabi; formal analysis, Layeth Al-Bahrani and Murtadha Al-Kaabi; investigation, Layeth Al-Bahrani; resources, Murtadha Al-Kaabi; data curation, Murtadha Al-Kaabi; writing—original draft preparation, Murtadha Al-Kaabi; writing—review and editing, Layeth Al-Bahrani; visualization,

Layeth Al-Bahrani, and Murtadha Al-Kaabi; supervision, Layeth Al-Bahrani; project administration, Layeth Al-Bahrani and Murtadha Al-Kaabi; funding acquisition, Layeth Al-Bahrani, and Murtadha Al-Kaabi.

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