REDUCTION OF ACTIVE POWER LOSS BY VOLITION PARTICLE SWARM OPTIMIZATION

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Abstract

This paper projects Volition Particle Swarm Optimization (VP) algorithm for solving optimal reactive power problem. Particle Swarm Optimization algorithm (PSO) has been hybridized with the Fish School Search (FSS) algorithm to improve the capability of the algorithm. FSS presents an operator, called as collective volition operator, which is capable to auto-regulate the exploration-exploitation trade-off during the algorithm execution. Since the PSO algorithm converges faster than FSS but cannot auto-adapt the granularity of the search, we believe the FSS volition operator can be applied to the PSO in order to mitigate this PSO weakness and improve the performance of the PSO for dynamic optimization problems. In order to evaluate the efficiency of the proposed Volition Particle Swarm Optimization (VP) algorithm, it has been tested in standard IEEE 30 bus test system and compared to other reported standard algorithms. Simulation results show that Volition Particle Swarm Optimization (VP) algorithm is more efficient then other algorithms in reducing the real power losses with control variables are within the limits..

Keywords: Optimal Reactive Power; Transmission Loss; Particle Swarm Optimization; Fish School Search Algorithm.


1. Introduction

Optimal reactive power problem is a multi-objective optimization problem that minimizes the real power loss and bus voltage deviation. Various mathematical techniques like the gradient method [1-2], Newton method [3] and linear programming [4-7] have been adopted to solve the optimal reactive power dispatch problem. Both the gradient and Newton methods have the complexity in managing inequality constraints. If linear programming is applied then the input- output function has to be uttered as a set of linear functions which mostly lead to loss of accuracy. The problem of voltage stability and collapse play a major role in power system planning and operation [8]. Global optimization has received extensive research awareness, and a great number of methods have been applied to solve this problem.
Evolutionary algorithms such as genetic algorithm have been already proposed to solve the reactive power flow problem [9, 10]. Evolutionary algorithm is a heuristic approach used for minimization problems by utilizing nonlinear and non-differentiable continuous space functions. In [11], Genetic algorithm has been used to solve optimal reactive power flow problem. In [12], Hybrid differential evolution algorithm is proposed to improve the voltage stability index. In [13] Biogeography Based algorithm is projected to solve the reactive power dispatch problem. In [14], a fuzzy based method is used to solve the optimal reactive power scheduling method. In [15], an improved evolutionary programming is used to solve the optimal reactive power dispatch problem. In [16], the optimal reactive power flow problem is solved by integrating a genetic algorithm with a nonlinear interior point method. In [17], a pattern algorithm is used to solve ac-dc optimal reactive power flow model with the generator capability limits. In [18], F. Capitanescu proposes a two-step approach to evaluate Reactive power reserves with respect to operating constraints and voltage stability.

In [19], a programming based approach is used to solve the optimal reactive power dispatch problem. In [20], A. Kargarian et al present a probabilistic algorithm for optimal reactive power provision in hybrid electricity markets with uncertain loads. In general, swarm algorithms are inspired in groups of animals, such as flocks of birds, schools of fish, hives of bees, colonies of ants, etc. Although a lot of swarm-based algorithms were already proposed, just some few were designed to tackle dynamic problems. One of the most used swarm intelligence algorithms is the Particle Swarm Optimization (PSO). Despite the fast convergence capability, the vanilla version of the PSO cannot tackle dynamic optimization problems.

It occurs because the entire swarm often increases the exploitation around a good region of the search space, reducing the overall diversity of the population. However, some variations of the PSO have been created in order to increase the capacity to escape from regions in the search space where the optimum is not located anymore [21-25]. On the other hand, another swarm intelligence algorithm proposed in 2008, the Fish School Search algorithm (FSS) [26-28], presents a very interesting feature that can be very useful for dynamic environments. FSS presents an operator, called collective volition operator, which is capable to auto-regulate the exploration-exploitation trade-off during the algorithm execution. Since the PSO algorithm converges faster than FSS but cannot auto-adapt the granularity of the search, & the FSS collective volition operator can be applied to the PSO in order to mitigate this PSO weakness and improve the performance of the PSO for dynamic optimization problems. In order to evaluate the efficiency of the proposed Volition Particle Swarm Optimization (VP) algorithm, it has been tested in standard IEEE 30 bus test system and compared to other reported standard algorithms. Simulation results show that Volition Particle Swarm Optimization (VP) algorithm is more efficient then other algorithms in reducing the real power losses with control variables are within the limits.

2. Problem Formulation

The optimal power flow problem is treated as a general minimization problem with constraints, and can be mathematically written in the following form:

Minimize f (x, u)  

(1)
subject to $g(x,u)=0$ \hspace{1cm} (2)

and

$h(x, u) \leq 0$ \hspace{1cm} (3)

where $f(x,u)$ is the objective function, $g(x,u)$ and $h(x,u)$ are respectively the set of equality and inequality constraints. $x$ is the vector of state variables, and $u$ is the vector of control variables.

The state variables are the load buses (PQ buses) voltages, angles, the generator reactive powers and the slack active generator power:

$$x = (P_{g1}, \theta_2, \ldots, \theta_N, V_{L1}, \ldots, V_{LNL}, Q_{g1}, \ldots, Q_{gn})^T$$ \hspace{1cm} (4)

The control variables are the generator bus voltages, the shunt capacitors/reactors and the transformers tap-settings:

$$u = (V_g, T, Q_c)^T$$ \hspace{1cm} (5)

or

$$u = (V_{g1}, \ldots, V_{gn}, T_1, \ldots, T_N, Q_{c1}, \ldots, Q_{cn})^T$$ \hspace{1cm} (6)

Where $ng$, $nt$ and $nc$ are the number of generators, number of tap transformers and the number of shunt compensators respectively.

### 3. Objective Function

**Active Power Loss**

The objective of the reactive power dispatch is to minimize the active power loss in the transmission network, which can be described as follows:

$$F = PL = \sum_{k\in\text{Nbr}} g_k \left( V_i^2 + V_j^2 - 2V_i V_j \cos \theta_{ij} \right)$$ \hspace{1cm} (7)

Or

$$F = PL = \sum_{i\in\text{Ng}} P_{gi} - P_d = P_{gstack} + \sum_{i\text{slack}}^{Ng} P_{gi} - P_d$$ \hspace{1cm} (8)

Where $g_k$: is the conductance of branch between nodes $i$ and $j$, $\text{Nbr}$: is the total number of transmission lines in power systems, $P_d$: is the total active power demand, $P_{gi}$: is the generator active power of unit $i$, and $P_{gstack}$: is the generator active power of slack bus.

**Voltage Profile Improvement**

For minimizing the voltage deviation in PQ buses, the objective function becomes:

$$F = PL + \omega \nu \times VD$$ \hspace{1cm} (9)
Where $\omega_v$ is a weighting factor of voltage deviation.

VD is the voltage deviation given by:

$$VD = \sum_{i=1}^{N_{pq}} |V_i - 1|$$  \hspace{1cm} (10)

**Equality Constraint**

The equality constraint $g(x, u)$ of the Optimal reactive power problem is represented by the power balance equation, where the total power generation must cover the total power demand and the power losses:

$$P_G = P_D + P_L$$  \hspace{1cm} (11)

This equation is solved by running Newton Raphson load flow method, by calculating the active power of slack bus to determine active power loss.

**Inequality Constraints**

The inequality constraints $h(x, u)$ reflect the limits on components in the power system as well as the limits created to ensure system security. Upper and lower bounds on the active power of slack bus, and reactive power of generators:

$$P_{g\text{slack}}^{\text{max}} \leq P_{g\text{slack}} \leq P_{g\text{slack}}^{\text{min}}$$  \hspace{1cm} (12)

$$Q_{gi}^{\text{min}} \leq Q_{gi} \leq Q_{gi}^{\text{max}}, i \in N_g$$  \hspace{1cm} (13)

Upper and lower bounds on the bus voltage magnitudes:

$$V_i^{\text{min}} \leq V_i \leq V_i^{\text{max}}, i \in N$$  \hspace{1cm} (14)

Upper and lower bounds on the transformers tap ratios:

$$T_i^{\text{min}} \leq T_i \leq T_i^{\text{max}}, i \in N_T$$  \hspace{1cm} (15)

Upper and lower bounds on the compensators reactive powers:

$$Q_c^{\text{min}} \leq Q_c \leq Q_c^{\text{max}}, i \in N_c$$  \hspace{1cm} (16)

Where $N$ is the total number of buses, $N_T$ is the total number of Transformers; $N_c$ is the total number of shunt reactive compensators.

**4. Particle Swarm Optimization (PSO)**

Particle Swarm Optimization (PSO) is a population-based optimization algorithm inspired by the behaviour of flocks of birds. The standard approach is composed by a swarm of particles, where each one has a position within the search space $\vec{x}_i$ and each position represents a solution for the problem. The particles fly through the search space of the problem searching for the best solution,
according to the current velocity $v_i$ the best position found by the particle itself ($P_{\text{best}_i}$) and the best position found by the entire swarm during the search so far ($G_{\text{best}}$). According this approach is also called inertia PSO & the velocity of a particle $i$ is evaluated at iteration’s of the algorithm by using the following equation,

$$v_i(t + 1) = \omega v_i(t) + c_1 r_1 (P_{\text{best}_i} - x_i(t)) + c_2 r_2 (G_{\text{best}} - x_i(t))$$  \hspace{1cm} \text{(17)}$$

Where $r_1$ and $r_2$ are numbers randomly generated in the interval $[0, 1]$. The inertia weight ($\omega$) controls the influence of the previous velocity and balances the exploration-exploitation behaviour along the process. It generally decreases from 0.9 to 0.4 during the algorithm execution. $c_1$ & $c_2$ are called cognitive and social acceleration constants, respectively, and weights the influence of the memory of the particle and the information acquired from the neighbourhood. The position of each particle is updated based on the velocity of the particle, according to the following equation:

$$x_i(t + 1) = x_i(t) + v_i(t + 1)$$  \hspace{1cm} \text{(18)}$$

The communication topology defines the neighbourhood of the particles and, as a consequence, the flow of information through the particles. There are two basic topologies: global and local. In the former, each particle shares and acquires information directly from all other particles, i.e. all particles use the same social memory, called Gbest. In the local topology, each particle only shares information with two neighbours and the social memory is not the same within the whole swarm. This approach, called Lbest, helps to avoid a premature attraction of all particles to a single spot point in the search space.

Since the standard PSO cannot tackle dynamic problems due to the low capacity to increase the diversity after the entire swarm has converge to a single region of the search space, many efforts to overcome this weakness have been made. The simplest idea is to restart the particles every time the search space changes. However, all the previous information obtained from the problem during the search process is lost in this case. An interesting approach is utilizing the idea of electrostatic charges. Some particles are charged (they repeal themselves) and some others are neutral. In general, the neutral particles tend to exploit towards a single sub-region of the search space, whereas the charged particles never converges to a unique spot. Nevertheless, the charged particles are constantly exploring in order to maintain diversity. In order to consider the effect of the charged particles, the velocity equation receives a fourth term, as shown in the equation (20). This term is defined as the acceleration of the particle $i$($\vec{a}_i$) and can be seen in equation (20).

$$\vec{v}_i(t + 1) = \omega \vec{v}_i(t) + c_1 r_1 (\vec{P}_{\text{best}_i} - \vec{x}_i(t)) + c_2 r_2 (\vec{G}_{\text{best}} - \vec{x}_i(t)) + \vec{a}_i(t)$$  \hspace{1cm} \text{(19)}$$

$$\vec{a}_i(t) = \begin{cases} \sum_{j \neq i} \frac{Q_i Q_j}{||\vec{r}_{ij}(t)||^2} \vec{r}_{ij}(t), \text{if } R_e \leq ||\vec{r}_{ij}(t)|| \leq R_p \\ 0, \text{otherwise} \end{cases}$$  \hspace{1cm} \text{(20)}$$

Where $\vec{r}_{ij}(t) = \vec{x}_i(t) - \vec{x}_j(t)$, $Q_i$ is the charge magnitude of the particle $i$ , $R_e$ is the core radius and $R_p$ is the perception limit of the particle . Neutral particles have charge value equal to zero, i.e. $Q_i = 0$. 


5. Fish School Search (FSS)

The Fish School Search (FSS) is an optimization algorithm based on the gregarious behaviour of oceanic fish. In the FSS, each fish represents a solution for the problem. The success of a fish during the search process is indicated by its weight. The FSS has four operators, which are executed for each fish of the school at each iteration: (i) individual movement, which is responsible for local search stepind; (ii) feeding, which updates the fish weights indicating the degree of success or failure during the search process so far; (iii) collective-instinctive movement, which makes all fish moves toward a resultant direction; and (iv) collective volition operator, which controls the granularity of the search. In this paper, as we are dealing with dynamic environments, only the feeding and collective volition movement operators are used to build the proposed algorithm.

Feeding Operator
The feeding operator determines the variation of the fish weight at iteration’s. One should notice that a fish can increase or decrease its weight depending, respectively, on the success or failure during the search process. The weight of the fish is evaluated according to the following equation:

\[ W_i(t + 1) = W_i(t) + \frac{\Delta f_i}{\max(|\Delta f|)} \]

Where \( W_i(t) \) is the weight of the fish, \( \Delta f_i \) is the variation of the fitness function between the new position and the current position of the fish, and \( \max(|\Delta f|) \) is the absolute value of the greatest fitness variation among all fish. There is a parameter \( W_{scale} \) that limits the maximum weight of the fish. The weight of each fish can vary between 1 and \( W_{scale} \) and has an initial value equal to \( W_{scale}/2 \).

Collective-Volitive Movement Operator
This operator controls the granularity of the search executed by the fish school. When the whole school is achieving better results, the operator approximates the fish aiming to accelerate the convergence toward a good region. On the contrary, the operator spreads the fish away from the barycenter of the school and the fish have more chances to escape from a local minimum. The fish school expansion or contraction is applied as a small drift to every fish position regarding the school barycenter, which can be evaluated as shown below:

\[ \bar{B}(t) = \frac{\sum_{i=1}^{N} x_i(t)W_i(t)}{\sum_{i=1}^{N} W_i(t)} \]

We use equation (23) to perform the fish school expansion (use sign +) or contraction (use sign −).

\[ \bar{x}_i(t + 1) = \bar{x}_i(t) + \text{step}_v \cdot r_1 \frac{x_i(t) - \bar{B}(t)}{d(x_i(t), \bar{B}(t))} \]

Where \( r_1 \) is a number randomly generated in the interval [0, 1]. \( d(x_i, \bar{B}) \) Evaluates the euclidean distance between the particles i and the barycenter. stepvol is called volition step and controls the step size of the fish. The stepvol is bounded by two parameters (stepvol_min and stepvol_max) and decreases linearly from stepvol max to stepvol_min along the algorithm iterations. It helps the
algorithm to initialize with exploration behaviour and change dynamically to exploitation behaviour.

6. Volition Particle Swarm Optimization (VP) For Solving Optimal Reactive Power Problem

Particle Swarm Optimization algorithm (PSO) has been hybridized with the Fish School Search (FSS) algorithm to improve the capability of the algorithm. Proposed approach includes two FSS operators in the Inertia PSO, the feeding and the collective-Volition movement. In the PSO, each particle becomes a weighted particle, where the weight is used to indicate the collective-Volition movement, resulting in expansion or contraction of the school. In our proposal, the stepvol does not decrease linearly; it decreases according to equation (24). The parameter Volition step decay percentage (decayvol) must be in the interval [0, 100].

$$step_{vol}(t + 1) = step_{vol}(t) \frac{100 - decay_{vol}}{100}$$

(24)

The stepvol is reinitialized to stepvol_max when a change in the environment is detected. The fitness of the sentry particle is evaluated in the end iteration’s and in the beginning of the next iteration.

Initialize parameters and particles;
While the stop condition is not reached do
For each particle of the swarm do
Evaluate the fitness of the particle;
Evaluate($P_{besti}$)and ($L_{besti}$)
End
if an environment change is detected then
Initialize stepvol;
End
For each particle of the swarm do
Update the velocity and the position of the particle;
Evaluate the fitness of the particle;
End
Execute feeding operator;
Execute collective-Volition movement operator;
For each particle of the swarm do
Evaluate($P_{besti}$) and($L_{besti}$);
End
Update stepvol and w;
End

7. Simulation Results

Validity of the proposed Volition Particle Swarm Optimization (VP) algorithm has been verified by testing in IEEE 30-bus, 41 branch system and it has 6 generator-bus voltage magnitudes, 4 transformer-tap settings, and 2 bus shunt reactive compensators. Bus 1 is taken as slack bus and 2,
5, 8, 11 and 13 are considered as PV generator buses and others are PQ load buses. Control variables limits are given in Table 1.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Min.</th>
<th>Max.</th>
<th>category</th>
</tr>
</thead>
<tbody>
<tr>
<td>Generator Bus</td>
<td>0.95</td>
<td>1.1</td>
<td>Continuous</td>
</tr>
<tr>
<td>Load Bus</td>
<td>0.95</td>
<td>1.05</td>
<td>Continuous</td>
</tr>
<tr>
<td>Transformer-Tap</td>
<td>0.9</td>
<td>1.1</td>
<td>Discrete</td>
</tr>
<tr>
<td>Shunt Reactive Compensator</td>
<td>-0.11</td>
<td>0.31</td>
<td>Discrete</td>
</tr>
</tbody>
</table>

In Table 2 the power limits of generators buses are listed.

<table>
<thead>
<tr>
<th>Bus</th>
<th>Pg</th>
<th>Pgmin</th>
<th>Pgmax</th>
<th>Qgmin</th>
<th>Qmax</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>96.00</td>
<td>49</td>
<td>200</td>
<td>0</td>
<td>10</td>
</tr>
<tr>
<td>2</td>
<td>79.00</td>
<td>18</td>
<td>79</td>
<td>-40</td>
<td>50</td>
</tr>
<tr>
<td>5</td>
<td>49.00</td>
<td>14</td>
<td>49</td>
<td>-40</td>
<td>40</td>
</tr>
<tr>
<td>8</td>
<td>21.00</td>
<td>11</td>
<td>31</td>
<td>-10</td>
<td>40</td>
</tr>
<tr>
<td>11</td>
<td>21.00</td>
<td>11</td>
<td>28</td>
<td>-6</td>
<td>24</td>
</tr>
<tr>
<td>13</td>
<td>21.00</td>
<td>11</td>
<td>39</td>
<td>-6</td>
<td>24</td>
</tr>
</tbody>
</table>

Table 3 shows the proposed Volition Particle Swarm Optimization (VP) algorithm successfully kept the control variables within limits. Table 4 narrates about the performance of the proposed Volition Particle Swarm Optimization (VP) algorithm. Table 5 list out the overall comparison of the results of optimal solution obtained by various methods.

<table>
<thead>
<tr>
<th>Control Variables</th>
<th>VP</th>
</tr>
</thead>
<tbody>
<tr>
<td>V1</td>
<td>1.0386</td>
</tr>
<tr>
<td>V2</td>
<td>1.0392</td>
</tr>
<tr>
<td>V5</td>
<td>1.0184</td>
</tr>
<tr>
<td>V8</td>
<td>1.0226</td>
</tr>
<tr>
<td>V11</td>
<td>1.0684</td>
</tr>
<tr>
<td>V13</td>
<td>1.0382</td>
</tr>
<tr>
<td>T4,12</td>
<td>0.00</td>
</tr>
<tr>
<td>T6,9</td>
<td>0.01</td>
</tr>
<tr>
<td>T6,10</td>
<td>0.90</td>
</tr>
<tr>
<td>T28,27</td>
<td>0.91</td>
</tr>
<tr>
<td>Q10</td>
<td>0.10</td>
</tr>
<tr>
<td>Q24</td>
<td>0.10</td>
</tr>
<tr>
<td>Real power loss</td>
<td>4.2542</td>
</tr>
<tr>
<td>Voltage deviation</td>
<td>0.9086</td>
</tr>
</tbody>
</table>
Table 4: Performance of VP algorithm

<table>
<thead>
<tr>
<th>Iterations</th>
<th>Time taken (secs)</th>
<th>Real power loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>29</td>
<td>8.42</td>
<td>4.2542</td>
</tr>
</tbody>
</table>

Table 5: Comparison of results

<table>
<thead>
<tr>
<th>Techniques</th>
<th>Real power loss (MW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SGA(Wu et al., 1998) [29]</td>
<td>4.98</td>
</tr>
<tr>
<td>PSO(Zhao et al., 2005) [30]</td>
<td>4.9262</td>
</tr>
<tr>
<td>LP(Mahadevan et al., 2010) [31]</td>
<td>5.988</td>
</tr>
<tr>
<td>EP(Mahadevan et al., 2010) [31]</td>
<td>4.963</td>
</tr>
<tr>
<td>CGA(Mahadevan et al., 2010) [31]</td>
<td>4.980</td>
</tr>
<tr>
<td>AGA(Mahadevan et al., 2010) [31]</td>
<td>4.926</td>
</tr>
<tr>
<td>CLPSO(Mahadevan et al., 2010) [31]</td>
<td>4.7208</td>
</tr>
<tr>
<td>HSA (Khazali et al., 2011) [32]</td>
<td>4.7624</td>
</tr>
<tr>
<td>BB-BC (Sakthivel et al., 2013) [33]</td>
<td>4.690</td>
</tr>
<tr>
<td>MCS(Tejaswini sharma et al., 2016) [34]</td>
<td>4.87231</td>
</tr>
<tr>
<td>Proposed VP</td>
<td>4.2542</td>
</tr>
</tbody>
</table>

8. Conclusion

In this paper a novel approach Volition Particle Swarm Optimization (VP) algorithm successfully solved optimal reactive power problem. PSO algorithm converges faster than FSS but cannot auto-adapt the granularity of the search, & the FSS collective volition operator can be applied to the PSO in order to mitigate this PSO weakness and improve the performance of the PSO for dynamic optimization problems. In order to evaluate the efficiency of the proposed Volition Particle Swarm Optimization (VP) algorithm, it has been tested in standard IEEE 30 bus test system and compared to other reported standard algorithms. Simulation results show that Volition Particle Swarm Optimization (VP) algorithm is more efficient than other algorithms in reducing the real power losses with control variables are within the limits.

References


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