

# SYNTHESIS OF UNEQUALLY SPACED LINEAR MICRO STRIP RECTANGULAR PATCH ANTENNA ARRAY USING IMPROVED LOCAL SEARCH PARTICLE SWARM OPTIMIZATION

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## ABSTRACT

Antenna array systems with low side lobe levels are essential for today wireless communication systems. This paper presents the synthesis of unequally spaced linear rectangular micro strip antenna array with minimum side lobe levels using the novel evolutionary algorithm known as improved local search particle swarm optimization (ILSPSO). ILSPSO is a modified version of particle swarm optimization (PSO), in which Gaussian distribution is used to enhance the local search of the PSO. In this paper, ILPSO is applied to optimize the positions of the micro strip antenna elements to suppress the peak side lobe level (PSLL) along with PSO and differential evolution (DE) algorithms. The steps involved in problem formulation along with design examples illustrating the performance of the ILPSO in minimizing the side lobe levels are demonstrated. A 20 and 32 element linear micro strip rectangular patch antenna (MSRPA) element are considered to show the effectiveness of the proposed method. The optimized micro strip antenna array is simulated using high frequency structure simulator (HFSS). The synthesis results demonstrate that the ILSPSO outperforms PSO and DE in terms of producing lower PSLL and convergence rate. The flexibility and ease of implementation of the ILSPSO algorithm is obvious from this paper, showing the algorithms usefulness in other array synthesis problems.

**KEYWORDS:** Antenna Array, Peak Side Lobe Level, Particle Swarm Optimization, Differential Evolution, Gaussian Distribution, Micro Strip Rectangular Patch Antenna, HFSS

## 1. INTRODUCTION

Low side lobe and high directive antenna array systems are need to be designed for enhancing the effectiveness of the communication systems [1, 2]. These have been used for different applications in satellite communication, Radars, wireless communications, mobile communications systems respectively. Systems need to maintain low side lobe levels for interference less communications systems. Side lobe levels are the major concern in design of highly efficient antenna array systems. In transmission mode, energy wasted through the side lobe levels in unwanted directions where as in reception mode unwanted signals are entered into our own communication system through the side lobe levels. So it is required to develop antenna arrays with low side lobes for better communication.

The radiation pattern of the antenna array is depends on the amplitude & phase excitation of the antenna elements, positions of the antenna elements and the radiation pattern of the individual antenna element. So, controlling the side lobe levels of the radiation pattern can be achieved by optimizing the position between the elements, amplitude and phase weights of the antenna elements. Antenna array synthesis has been studied from the last 50 years. Several evolutionary algorithms such as genetic algorithm (GA) [5-9], simulated annealing [10], particle swarm optimization (PSO) [11-16],

differential evolution (DE) [17, 18] and cat swarm optimization (CSO) [19] etc. have been successfully applied to antenna array synthesis problems. GA and PSO have been extensively used for antenna array problems. But PSO has its own disadvantages. It has been trapped in local optima while solving complex multimodal problems.

In order to overcome the above mentioned problems, a novel improved local search particle swarm optimization algorithm (ILPSO) is proposed in this paper to solve antenna array synthesis problems. The Gaussian distribution [20] is adopted to enhance the local convergence. In this paper micro strip rectangular patch antenna is used as the antenna element. The micro strip rectangular patch antenna is simulated using HFSS. The simulation results for the return loss and gain are recorded.

The paper is organized as follows. The detail description of the ILPSO algorithm is discussed in Section 2. In Section 3, brief description of the micro strip rectangular patch antenna with HFSS simulated results are discussed. The linear antenna array factor and the problem formulation are discussed in Section 4. Numerical illustrations is illustrated in Section 5. Finally the conclusions are discussed in Section 6.

## 2. PARTICLE SWARM OPTIMIZATION (PSO)

The Particle swarm optimization (PSO) [15], a simple and robust stochastic evolutionary algorithm. It has been applied for solving various optimization problems in electromagnetic applications since last 10 years. It has been developed by Eberhart and Kennedy in 1995 who obtained motivation from the migration and aggregation of bird flock when they seek for food. PSO is simple to understand and implement compared to other stochastic algorithms. PSO algorithm explores the search path according to the velocity and current position of particle which changes according to its own best position and other particles best position. PSO have been shown superior performance over traditional DE and genetic algorithm (GA) in many applications in terms of convergence time, memory occupation and has less parameters to adjust.

A swarm of particles  $P$  is randomly initialized in a pre-defined search space. Initialize the velocities for each particle. Each row of the position matrix swarm represents a possible solution. In each generation, each particle is updated by the velocity of that particle. The velocity of the particle is changed according to the two best values known as personal best position ( $P_{best}$ ) and global best position ( $G_{best}$ ). The personal best position of the  $i^{th}$  particle is represented as  $P_{besti} = (P_{besti1}, P_{besti2}, \dots, P_{bestiD})$ , the global best position vector defines the position in the solution space at which the best fitness value was achieved by all particles, and is defined as  $G_{besti} = (G_{besti1}, G_{besti2}, \dots, G_{bestiD})$

The particle velocity and position are updated by the following equations [14,16]

$$V_t = \omega V_{t-1} + c_1 r_1 (P_{t-1} - X_{t-1}) + c_2 r_2 (G_{t-1} - X_{t-1}) \quad (1)$$

$$X_t = X_{t-1} + V_t \quad (2)$$

Where  $\omega$  is a inertial weight (0.9),  $r_1$  and  $r_2$  are the random numbers in the interval 0 and 1. The parameters  $c_1$  and  $c_2$  specifies the relative weight of the pbest versus and gbest and both the values are chosen as 2.

### 2.1. Improved Local Search Particle Swarm Optimization (ILPSO)

The main disadvantage of the PSO is that it traps in local optima while solving complex multimodal problems because of poor local search capabilities. To enhance the local search capabilities Gaussian distribution with mean zero and

standard distribution of 1 is adopted while updating the  $G_{best}$  [21-22]. The mechanism is that, after updating the  $G_{best}$  in PSO, 'M' number of particles are generated around the  $G_{best}$  using the Gaussian distribution to enhance the local search capabilities. Update the new  $G_{best}$  after producing 'M' number of particles around the  $G_{best}$ .

$$New\ G_{best} = G_{best} + Gaussian\ Distribution(0,1) \tag{3}$$

The flow chart of ILSPSO is shown in Figure 1.

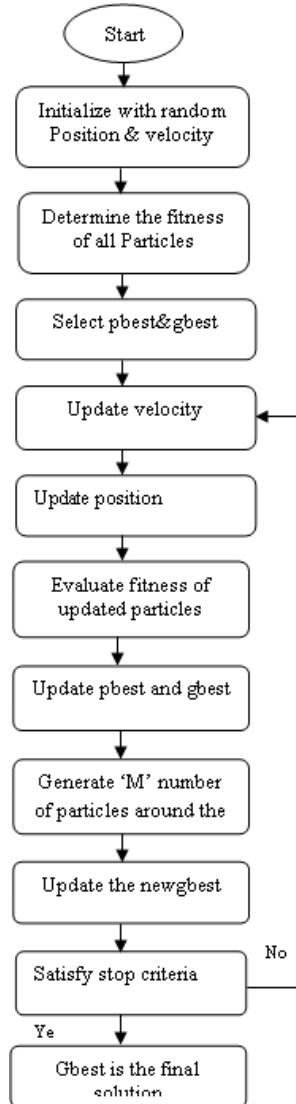


Figure 1: Flow Chart of the ILSPSO

### 3. MICRO STRIP RECTANGULAR PATCH ANTENNA (MSRPA)

Micro strip antennas [2-6] are also called patch antennas as they are manufactured by photo etching the radiating elements on the dielectric substrate. The radiating element may be a rectangular, circular, or any other configuration. A rectangular patch antenna is a commonly used Micro strip antenna because of many reasons like compact size, low weight and can be easily printed on printed circuit board as a result the array made of these elements would be occupying less space compared to the 3-D antennas like dipole, horn antenna etc. A rectangular patch antenna consists of a patch on one side and the ground plane on the other side of the dielectric substrate with the ground plane having the same dimensions of

that of the substrate. In the design of rectangular patch antenna we have employed the substrate Rogers RT/Duroid 5880 with relative permittivity ( $\epsilon_r$ ) 2.2 and thickness ( $T$ ) 1.588 mm with the type of feed being Co-axial, matching the 50 ohm impedance. The Schematic diagram of a coaxial probe fed rectangular Micro strip patch antenna is shown in Figure 2. The antenna is designed at 2.4GHz. The design equations of the rectangular micro strip patch antenna is given below.

$$\text{Free Space Wavelength: } \lambda_0 = \frac{C_0}{f_0} \quad (4)$$

Where ' $C_0$ ' represents velocity of light in vacuum and ' $f_0$ ' represents the resonant frequency

$$\text{Width of the patch: } W_p = \frac{C_0}{2f_0} \sqrt{\frac{2}{(1+\epsilon_r)}} \quad (5)$$

$$\text{Effective Dielectric constant : } \epsilon_{\text{eff}} = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \left[ 1 + 12 \frac{T}{W_p} \right]^{-1} \quad (6)$$

$$\text{Extra Length of the Patch due to fringing: } \Delta L_p = 0.412h \frac{(\epsilon_{\text{eff}} + 0.3) \left( \frac{W_p}{T} + 0.264 \right)}{(\epsilon_{\text{eff}} - 0.258) \left( \frac{W_p}{T} + 0.8 \right)} \quad (7)$$

$$\text{Length of the Patch: } L_p = \frac{C_0}{2f_0 \sqrt{\epsilon_{\text{eff}}}} - 2\Delta L_p \quad (8)$$

$$\text{Impedance of the Patch: } Z_p = 90 \frac{\epsilon_r - 1}{\epsilon_r + 1} \left( \frac{L_p}{W_p} \right)^2 \quad (9)$$

$$\text{Width of the Ground: } W_g = W_p + 6T \quad (10)$$

$$\text{Length of the Ground: } L_g = L_p + 6T \quad (11)$$

$$\text{Feed position } (X_f, Y_f): Z_0 = \sqrt{50 * Z_p} \quad (12)$$

$$Y_0 = \frac{1}{\pi} \cos^{-1} \sqrt{\frac{50}{Z_0}}$$

$$Y_f = Y_0 - \Delta L_p$$

$$X_f = \frac{W_p}{2}$$

The rectangular micro strip patch antenna is simulated using HFSS. The simulated return loss is shown in Figure 3. The obtained return loss at operating frequency 2.4GHz is -17dB. The three dimensional radiation patterns is shown in Figure 4. The maximum gain of the antenna is 7.76dB. The radiation pattern at  $\theta = 0^\circ$  plane is shown in Figure 5.

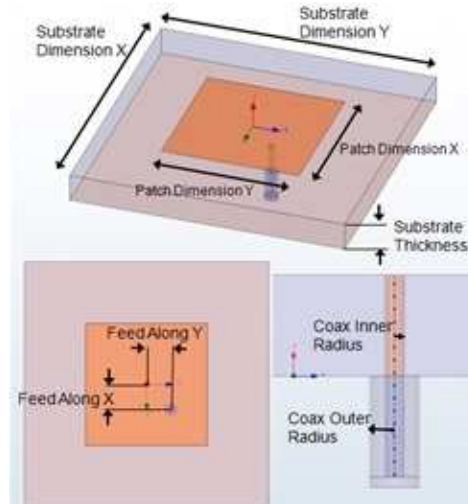


Figure 2: Schematic Diagram of a Coaxial Probe Fed Rectangular Micro Strip Patch Antenna

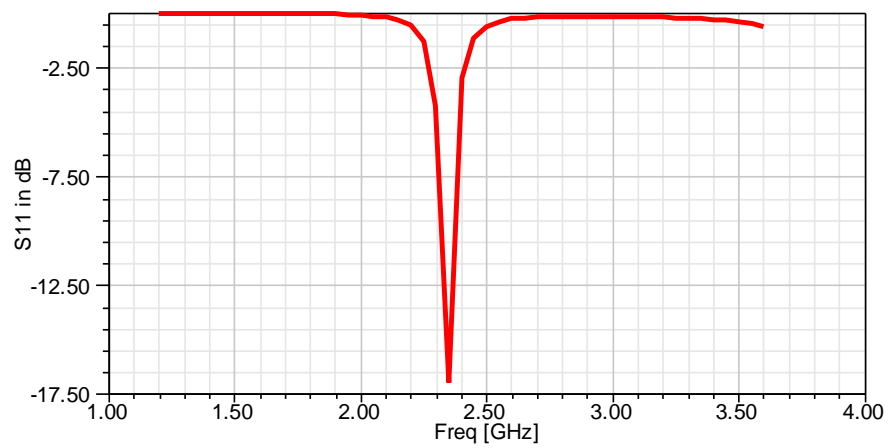


Figure 3: Return Loss (S11) of the Coaxial Probe Fed Rectangular Micro Strip Patch Antenna at 2.4 GHz

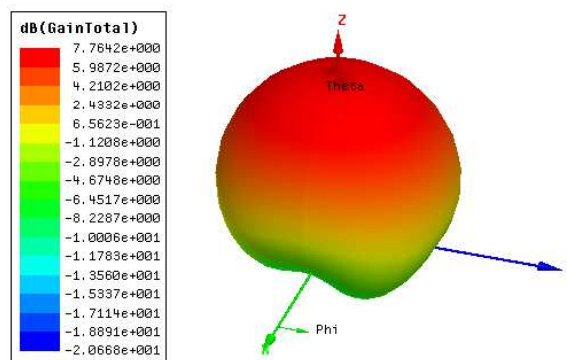


Figure 4: Gain of the Coaxial Probe Fed Rectangular Micro Strip Patch Antenna at 2.4 GHz

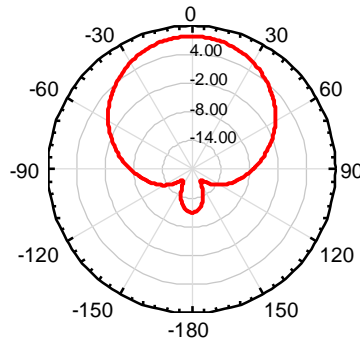


Figure 5: Radiation Pattern at  $\theta = 0^\circ$

#### 4. PROBLEM FORMULATION FOR MINIMIZING THE SIDE LOBE LEVELS

The geometry of  $2N$  element uniformly placed symmetric linear antenna array along  $x$  axis shown in Figure 6 is considered.

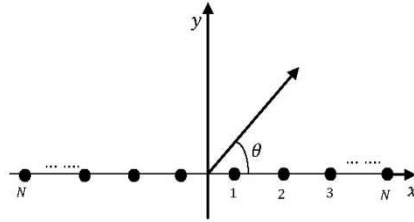


Figure 6: Schematic Diagram of  $2N$ -Element Linear Antenna Array

The array factor of the linear antenna array [1] is

$$AF(\theta) = \sum_{n=1}^{2N} I_n \cos[kx_n \cos(\theta) + \varphi_n] \quad (13)$$

Where  $k = 2\pi/\lambda$ ,  $I_n$ ,  $\varphi_n$  and  $x_n$  are the excitation amplitude, phase and position of element  $n$  respectively.

For the uniform amplitude and phases, we considered as  $I_n = 1$  and  $\varphi_n = 0$ .

$$AF(\theta) = \sum_{n=1}^{2N} I_n \cos[kx_n \cos(\theta)] \quad (14)$$

The main of this paper is to minimize the peak side lobe level by employing non uniform positions to individual elements of the antenna array, i.e., by varying  $x_n$ . For that, the fitness function [10, 15] is formulated as

$$Fitness = \max \left( \frac{AF(\theta)}{AF_{max}} \right) \quad (15)$$

Where  $AF_{max}$  is the main beam peak and the fitness is valid in the side lobe region of  $\theta$ .

#### 5. NUMERICAL ILLUSTRATIONS: 20 AND 32 ELEMENT MSRPA ARRAY

One example is selected to illustrate the method of ILSPSO, PSO and DE to optimize the antenna positions for minimum side lobe level. The first example illustrates the synthesis of 20 element rectangular micro strip patch antenna array for minimum PSLL in the side lobe region. The ILSPSO, PSO and DE algorithm's parameters are given in Table 1. Table 2 shows the optimized element positions obtained by using ILSPSO, PSO and DE. To obtain the average performance, all the algorithms are performed for 50 trials. All the simulations are performed using MATLAB and HFSS.

**Table 1: Initial Parameters of the ILSPSO, PSO and DE**

ILSPSO		PSO		De	
Parameters	Values	Parameters	Values	Parameters	Values
Number of particles	50	Number of particles	50	Number of particles	50
Number of generations	500	Number of generations	500	Number of generations	500
$c_1$	2	$c_1$	2	SF	0.9
$c_2$	2	$c_2$	2	CR	0.5
$\omega$	Linearly varies from 0.9- 0.4	$\omega$	0.9	-	-
M	20	-	-	-	-

The obtained radiation pattern using ILSPSO, PSO and DE are shown in Figure 7. It can be observed that the ILSPSO produces lower PSLL compared to PSO and DE. ILSPSO produces PSLL of -21.77dB, PSO produces PSLL of -20.11dB and DE produces PSLL of -16.82dB. The convergence plots for the 20 element micro strip rectangular patch antenna array using ILSPSO, PSO and DE is shown in Figure 8. It can be seen from Figure 8 that, ILSPSO outperforms PSO and DE in terms of low fitness value. Also ILSPSO converges faster than PSO and DE.

**Table 2: Optimized Positions Obtained Using ILSPSO, PSO and DE and Their PSLL's and Beam Width for 20 and 32 Element MSRPA Arrays**

Array Type	Algorithm	Optimized Positions (Since Linear Antenna Array is Symmetric, So Half of the Positions are Given Below)	PSLL Db	Beam Width Deg.
20 Element MSRPA	Periodic Array	$\pm 0.2500\lambda \pm 0.7500\lambda \pm 1.2500\lambda \pm 1.7500\lambda \pm 2.2500\lambda \pm 2.7500\lambda$ $\pm 3.2500\lambda \pm 3.7500\lambda \pm 4.2500\lambda \pm 4.7500\lambda$	-13.23	11.2
	ILSPSO	$\pm 0.2500\lambda \pm 0.7500\lambda \pm 1.2500\lambda \pm 1.7500\lambda \pm 2.3431\lambda \pm 2.8431\lambda$ $\pm 3.4736\lambda \pm 4.3129\lambda \pm 5.1038\lambda \pm 6.0016\lambda$	-21.77	11.2
	PSO	$\pm 0.2500\lambda \pm 0.7500\lambda \pm 1.2500\lambda \pm 1.7500\lambda \pm 2.2500\lambda \pm 2.7500\lambda$ $\pm 3.3879\lambda \pm 4.1404\lambda \pm 4.9346\lambda \pm 5.7431\lambda$	-20.11	11.2
	DE	$\pm 0.2500\lambda \pm 0.7500\lambda \pm 1.2500\lambda \pm 1.7500\lambda \pm 2.2500\lambda \pm 2.7500\lambda$ $\pm 3.2500\lambda \pm 3.7500\lambda \pm 4.2500\lambda \pm 5.5238\lambda$	-16.82	11.6
32 Element MSRPA	Periodic Array	$\pm 0.2500\lambda \pm 0.7500\lambda \pm 1.2500\lambda \pm 1.7500\lambda \pm 2.2500\lambda \pm 2.7500\lambda$ $\pm 3.2500\lambda \pm 3.7500\lambda \pm 4.2500\lambda \pm 4.7500\lambda \pm 5.2500\lambda \pm 5.7500\lambda$ $\pm 6.2500\lambda \pm 6.7500\lambda \pm 7.2500\lambda \pm 7.7500\lambda$	-13.23	6.4
	ILSPSO	$\pm 0.2501\lambda \pm 0.7501\lambda \pm 1.2501\lambda \pm 1.8062\lambda \pm 2.3222\lambda \pm 2.9080\lambda$ $\pm 3.4296\lambda \pm 3.9964\lambda \pm 4.6524\lambda \pm 5.1980\lambda \pm 5.9067\lambda \pm 6.7303\lambda$ $\pm 7.6492\lambda \pm 8.4497\lambda \pm 9.5328\lambda \pm 10.2499\lambda$	-21.95	6.4
	PSO	$\pm 0.2500\lambda \pm 0.7500\lambda \pm 1.2500\lambda \pm 1.7500\lambda \pm 2.2500\lambda \pm 2.7693\lambda$ $\pm 3.4408\lambda \pm 4.1010\lambda \pm 4.7127\lambda \pm 5.2361\lambda \pm 5.8974\lambda \pm 6.6713\lambda$ $\pm 7.4011\lambda \pm 8.3914\lambda \pm 9.2818\lambda \pm 10.0949\lambda$	-20.70	6.4
	DE	$\pm 0.2500\lambda \pm 0.7500\lambda \pm 1.2500\lambda \pm 1.7500\lambda \pm 2.2500\lambda \pm 2.7500\lambda$ $\pm 3.2500\lambda \pm 3.7500\lambda \pm 4.2500\lambda \pm 4.7500\lambda \pm 5.2500\lambda$ $\pm 5.7500\lambda \pm 6.4227\lambda \pm 7.2446\lambda \pm 8.8783\lambda \pm 9.5211\lambda$	-19.23	6.8

The second example illustrates 32 element MSRPA array. The optimized positions and their performance metrics are given Table 2. The obtained radiation pattern using ILSPSO, PSO and DE are shown in Figure 9. It can be observed that the ILSPSO produces lower PSLL compared to PSO and DE. ILSPSO produces PSLL of -21.95dB, PSO produces PSLL of -20.70dB and DE produces PSLL of -19.23dB. The convergence plots for the 32 element MSRPA array using ILSPSO, PSO and DE are shown in Figure 10. It can be seen from Figure 10 that, ILSPSO outperforms PSO and DE in terms of low fitness value. Also ILSPSO converges faster than PSO and DE.

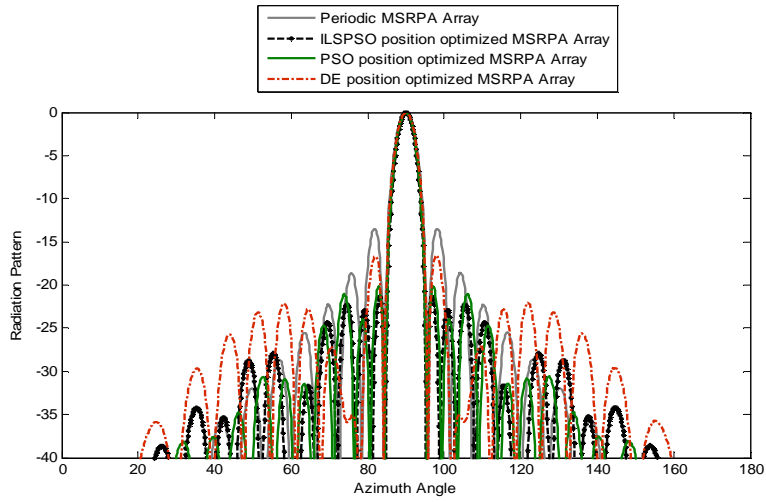


Figure 7: Radiation Pattern of the ILSPSO, PSO and Optimized 20 Elements MSRPA Array along with the Periodic MSRPA Array

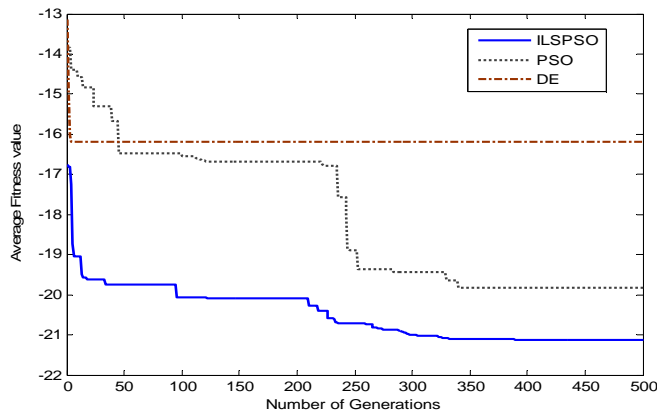


Figure 8: ILSPSO, PSO and DE Convergence Plots for the Synthesis of the 20 Element MSRPA Array

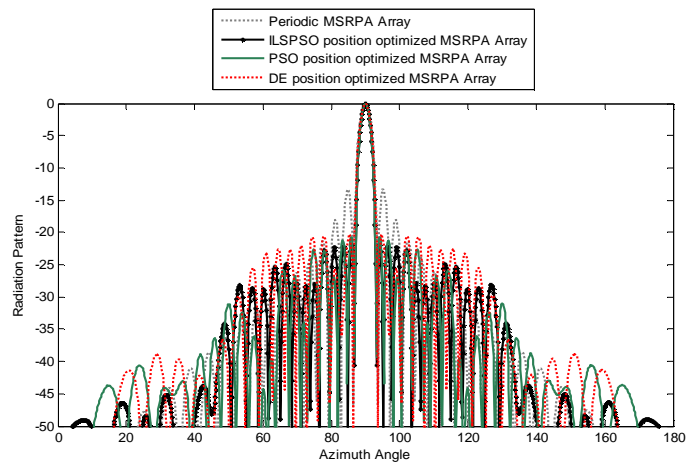


Figure 9: Radiation Pattern of the ILSPSO, PSO and Optimized 32 Elements MSRPA Array along with the Periodic MSRPA Array



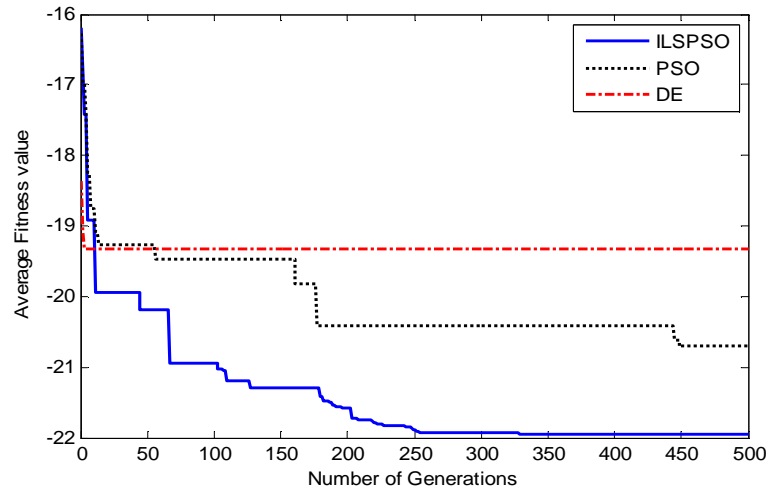


Figure 10: ILSPSO, PSO and DE Convergence Plots for the Synthesis of the 32 Element MSRPA Array

## 6. CONCLUSIONS

An improved local search particle swarm optimization is proposed for the synthesis of the unequally spaced linear micro strip antenna array. Gaussian distribution is adopted to enhance the local and global search capabilities of ILSPSO. ILSPSO is simple like PSO, at the same time it is more robust than the PSO. Minimization of side lobe level of a 20 and 32 element linear MSRPA array is illustrated using ILSPSO, PSO and DE algorithms. ILSPSO, PSO and DE are applied to optimize the optimal positions of the MSRPA element positions. ILSPSO, PSO and DE are successfully applied to suppress the side lobe levels. The obtained optimal arrays are simulated through MATLAB and HFSS. Synthesis results demonstrates that the ILPSO produces low side lobe antenna arrays with better convergence rates compared to PSO and DE algorithms. These antenna arrays are useful in interference less communications and as well as in Jamming conditions. ILSPSO is also useful in other electromagnetic problems due to its attractive properties as compared to PSO and DE.

## REFERENCES

1. C. A. Balanis, 'Antenna Theory', John Wiley, 'Analysis and design', 2nd Ed., 1997.
2. Ramesh G, Prakash B, Inder B, and Ittipiboon A. (2001) Microstrip antenna design handbook, Artech House.
3. K. KarunaKumari, Dr.P.V.Sridevi, 'Performance Evaluation of Circular Microstrip Patch Array with Difference Dielectric Substrate Materials', International Journal of Electronics and communication Engineering & Technology 4(1) 2013,pp236–249
4. K. KarunaKumari, Prof.P.V.Sridevi, 'Design and Analysis of Microstrip Antenna Array Using CST Software', IJESC. Vol. 62016, pp. 5977-5982.
5. R. L. Haupt. 'Introduction to Genetic Algorithms for Electromagnetics', IEEE Antenna and propagation Magazine. Vol. 37. pp. 7-15. 1995.
6. K. K. Yan, Y. Lu. 'Sidelobe reduction in array pattern synthesis using genetic algorithm' 1997; 45:1117-22.
7. K.KarunaKumari, Dr.P.V.Sridevi, 'Side lobe level optimization of circular microstrip array antenna using Genetic Algorithm', IJECIERD 4(1) January-Feb-2014pp 9–18

8. Yahya. Rahmat-Samii, Eric. Michielessen, 'Electromagnetic optimization by genetic algorithm'. Wiley Series in Microwave and Optical Engineering, 1999.
9. D. Marcano, F. Duran, 'Synthesis of Antenna Arrays Using Genetic Algorithms'. IEEE Antenna and propagation Magazine. Vol. 42. NO. 3. June 2000.
10. V. Murino, A. Trucco, C. S. Regazzoni. 'Synthesis of equally spaced arrays by simulated annealing'. IEEE Trans. Signal Processing 1996; 44:119-12.
11. K. KarunaKumari, Dr.P.V.Sridevi, 'Pattern Synthesis of non uniform amplitude equally spaced microstrip array antenna using GA, PSO and DE Algorithms', International Journal Advanced Research in Engineering and Technology Vol. 7 2016, pp. 132–147
12. D.W. Boeringer, D. H. Werner, 'Particle swarm optimization versus genetic algorithms for phased array synthesis' IEEE Trans. Antennas Propagation 2004; 52: 771-79.
13. James Kennedy, Russel Eberhart, 'Particle swarm optimization. Proceedings of IEEE conference on Neural networks', 1995. p. 1942-48.
14. Majid M. Khodier, Christos G. Christodoulou, 'Linear array geometry synthesis with minimum side lobe level and null controlling using particle swarm optimization'. IEEE transactions on antennas and propagation 2005; 53: 2674-79.
15. Robinson. J, Y. Rahmat-Samii, 'Particle Swarm optimization in electromagnetics'. IEEE transactions on antennas and propagation 2004; 52: 397-407.
16. James Kennedy, Russel Eberhart, 'Particle swarm optimization. Proceedings of IEEE conference on Neural networks, 1995. p. 1942-48.
17. Kurup, D.G., Himidi, M., Rydberg, A. 'Synthesis of uniform amplitude unequally spaced antenna arrays using the differential evolution algorithm', IEEE Trans. Antennas Propag., 2003, 51, (9), pp. 2210–2217.
18. L. Zhang Y.-C. Jiao B. Chen and F.-S. Zhang, Synthesis of linear aperiodic arrays using a selfadaptive hybrid differential evolution algorithm, IET Microwaves, Antenna and Propagation, vol. 5, 2011, pp. 1524-1528.
19. Pappula, L., Ghosh, D, 'Linear antenna array synthesis using cat swarm optimization', AEU-Int. Journal of Electronics and Communications, 2014, 68, pp. 540-549
20. Chellapilla, K.: 'Combining Mutation Operators in Evolutionary Programming', IEEE Trans. Evol. Comput., 1998, 2, (3), pp. 91–96.
21. Liu, Q.-Y. Feng, W.-B. Wang, and X. Yu Synthesis of unequally spaced antenna array by using Inheritance learning Particle Swarm Optimization', Progress In Electromagnetics Research, Vol. 118, 205{221, 2011
22. Junying Chen, Zheng Qin, Yu Liu, and Jiang Lu, ' Particle Swarm Optimization with Local Search' IEEE Trans. 2005. pp 481-484.